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**Geographic information — Discrete Global Grid Systems
Specifications — Part 1: Core Reference System and
Operations, and Equal Area Earth Reference System**

Publication stage

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Contents

Foreword	iv
Introduction.....	v
1 Scope	1
2 Normative references	1
3 Terms and definitions.....	1
4 Conventions	10
4.1 Abbreviated terms	10
4.2 Universal Resource Identifiers	11
4.3 Unified Modeling Language notation.....	11
4.4 Naming conventions	11
4.5 Attribute and association role status	12
5 DGGs specification overview.....	12
5.1 Package overview	12
6 Common Spatio-temporal Classes package.....	14
6.1 Common Spatio-temporal Classes overview.....	14
6.2 Temporal and Zonal Geometry package	15
6.3 Temporal and Zonal RS using Identifiers package	25
7 DGGs Core package	36
7.1 DGGs Core package conformance classes	36
7.2 Core RS using Zonal Identifiers with Structured Geometry module.....	36
7.3 DGGs Core functions	44
8 Equal-area Earth DGGs	62
8.1 Equal-Area Earth DGGs package	62
Annex A (normative) Abstract test suite	82
Annex B (informative) Equal area DGGs theory	95
Annex C (informative) Background to DGGs	100
Annex D (informative) Temporal geometry, topology, and temporal referencing by named periods — Context for modelling.....	105
Bibliography	107

Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular, the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see www.iso.org/directives).

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights. Details of any patent rights identified during the development of the document will be in the Introduction and/or on the ISO list of patent declarations received (see www.iso.org/patents).

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For an explanation of the voluntary nature of standards, the meaning of ISO specific terms and expressions related to conformity assessment, as well as information about ISO's adherence to the World Trade Organization (WTO) principles in the Technical Barriers to Trade (TBT), see www.iso.org/iso/foreword.html.

This document was prepared by Technical Committee ISO/TC 211, *Geographic information/Geomatics*, in close collaboration with the Open Geospatial consortium (OGC).

A list of all parts in the ISO 19170 series can be found on the ISO website.

Any feedback or questions on this document should be directed to the user's national standards body. A complete listing of these bodies can be found at www.iso.org/members.html.

Introduction

DGGSs (Discrete Global Grid Systems) provide a new way to organise, store and analyse spatio-temporal data. This document contains a normative definition for DGGS and informative annexes. Annex B discusses the theoretical basis for equal area Earth DGGS, and Annex C discusses DGGS's historical background. At the heart of DGGS is a new Referencing system. Spatial and temporal RSs described elsewhere by ISO/TC211 and the OGC (Open Geospatial Consortium) fall into two types:

- 1) Referencing by coordinates ([ISO 19111](#)), and
- 2) Referencing by identifiers (geographic in [ISO 19112](#) & ordinal era in [ISO 19108](#)).

In spatial Referencing by identifiers, the only required geometry is an extent, which may be expressed as a simple bounding box. Formal geometry need not be defined and sometimes follows societal whim. Similarly in ordinal temporal RSs, the topology of ordinal era's are known, but the start and finish times are often only an estimation and are not required by the data model. DGGSs introduce a third type—Referencing by identifiers with structured geometry, illustrated in Figure 1.

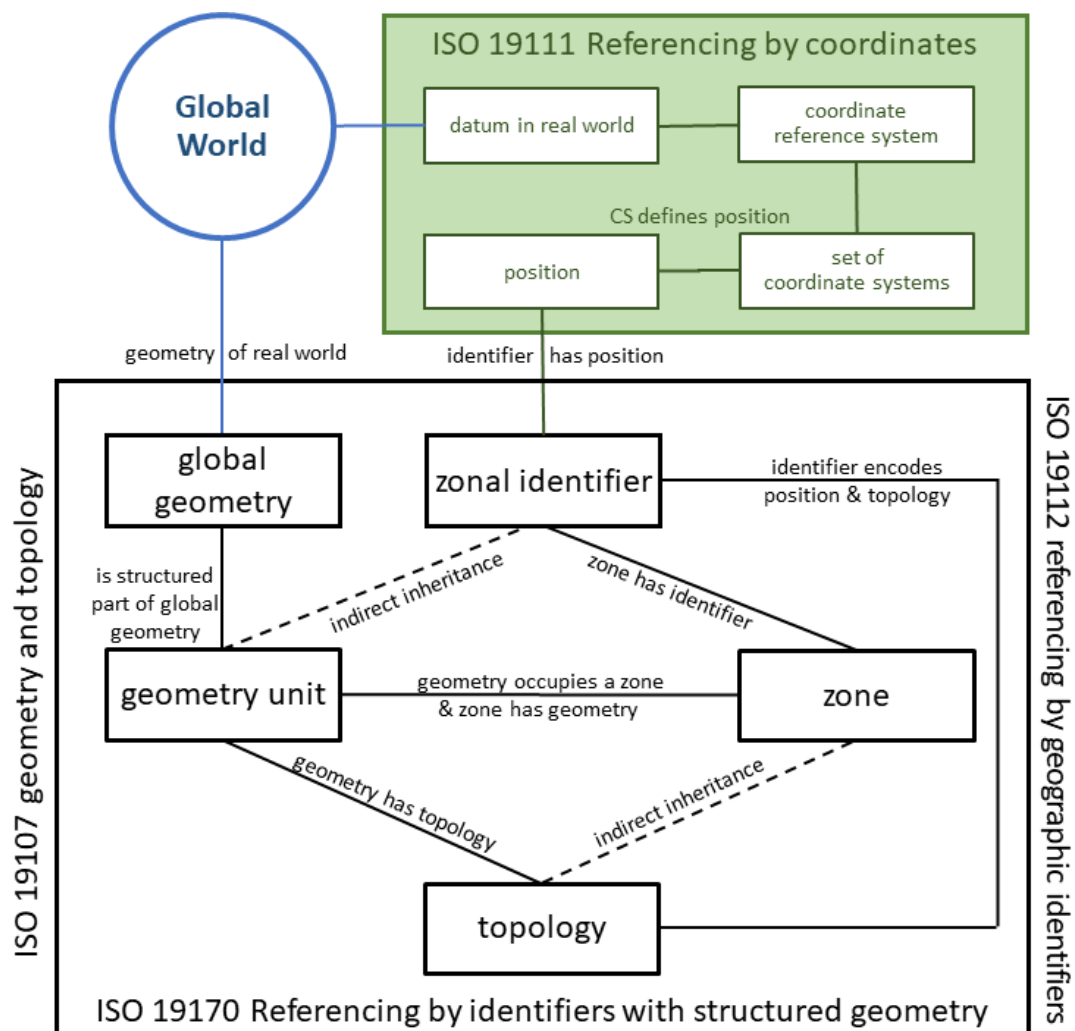


Figure 1 — Referencing by identifiers with structured geometry

A single parent global geometry is chosen to define the dimensionality and orientation of the region of space-time occupied by the DGGS—it's global world. The structure for the DGGS geometry is provided by a strictly controlled process of recursive tessellation of the parent geometry that creates the DGGS RS's units of geometry. The region occupied by each unit of geometry is called a zone. Each zone is given a unique name, called a zonal identifier. Each zonal identifier is associated with a representative spatio-

temporal position in a base CRS (coordinate reference system) defined by a datum for the DGGs's global world. Best practice is for a zonal identifier to be an encoding of both its position and its topology. Referencing by identifiers with structured geometry gives rise to RSs using zonal identifiers with structured geometry. Geographic information is inherently four-dimensional and includes time. So, a unified spatio-temporal data model for coordinate systems, geometry, topology, identifiers and RSs using identifiers is a pre-requisite for spatio-temporal DGGs.

The approach taken in this document to specifying spatio-temporal data classes is to apply the spatio-temporal data model pattern in ISO 19111 to spatial data classes in both ISO 19107 and ISO 19112 to produce their spatio-temporal equivalents. The set of common spatio-temporal classes for geometry, topology, identifiers, and RSs using identifiers specified in this document are therefore consistent with spatio-temporal CRS and coordinate systems in ISO 19111. Like ISO 19111, the temporal data model in this document does not reference ISO 19108. The similarities and differences are described in Annex D.

In this document the spatio-temporal scope is constrained to spatial classes that are invariant through all time, and to temporal classes that are invariant throughout space. While this approach excludes certain spatio-temporal situations, it is flexible enough for a very large body of social and environmental modelling. Oceanic, climate and weather modelling often need geometries with a constant mass of gaseous fluid under changing pressure and temperature. These models can be run outside a DGGs. However, the results coming from these environmental models can be stored in a DGGs for efficient later use with other data.

This document specifies data models for a consistent set of common spatio-temporal classes, a DGGs core built on the common spatio-temporal classes, and a DGGs EAERS (equal-area Earth RS). The Common Spatio-temporal Classes, DGGs Core, and Equal-Area Earth DGGs packages each have their own conformance classes with their associated specifications and requirements.

The DGGs Core package is comprised of a RS, and functions for quantization, topological query and interoperability.

The DGGs Core RS is a RS using zonal identifiers with structured geometry located in its real world by coordinates in a base CRS. The DGGs Core RS is designed to support:

- temporal, surface, volumetric and spatio-temporal DGGs,
- DGGs with different grid constraints,
- DGGs with different refinement strategies, and
- DGGs referencing either the Earth or other celestial bodies.

The RS in Equal-Area Earth DGGs is a specialization of the DGGs Core RS. It describes a RS, comprising:

- a base unit polyhedron,
- a discrete hierarchical sequence of global grids,
- global grids with equal-area zones each with a unique identifier, and
- located in a geodetic CRS, that is typically also a geographic CRS.

This document does not prescribe any specific Earth surface model, base polyhedron or class of polyhedra, but is intended to allow for a range of options that produce DGGs with compatible and interoperable functional characteristics.

Future additions to the ISO 19170 series are intended to cover:

- Part 2: Three-dimensional and equal-volume Earth RS.
- Part 3: Spatio-temporal Earth RS.
- Part 4: Axis-aligned RS with all zone edges parallel to the base CRS's axes.
- Specification for a DGGS-API to formalise client-server, and server-server operations, both between DGGSs and between DGGSs and non-DGGS architectures.
- Creation of a register system for DGGS definitions analogous to the register for CRSs.
- Additions to other specifications, such as for OWS [\[52\]](#), [\[54\]](#) architectures, spatial features and data formats to support DGGS data structures.

Geographic information — Discrete Global Grid Systems Specifications — Core Reference System and Operations, and Equal Area Earth Reference System

1 Scope

This document supports the definition of:

- A DGGs core comprising:
 - a RS using zonal identifiers with structured geometry, and
 - functions providing import, export and topological query,
- Common spatio-temporal classes for geometry, topology, RS using zonal identifiers, zonal identifiers and zones, based on ISO 19111 CRS. The spatio-temporal scope is constrained to
 - spatial elements that are invariant through all time, and
 - temporal elements that are invariant across all space.
- EAERS for equal-area Earth DGGs.

2 Normative references

The following documents are referred to in the text in such a way that some or all of their content constitutes requirements of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

3 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

ISO and IEC maintain terminological databases for use in standardization at the following addresses:

- ISO Online browsing platform: available at <http://www.iso.org/obp>
- IEC Electropedia: available at <http://www.electropedia.org>

3.1

boundary

set that represents the limit of an entity

Note 1 to entry: Boundary is most commonly used in the context of geometry, where the set is a collection of points or a collection of objects that represent those points. In other domains, the term is used metaphorically to describe the transition between an entity and the rest of its domain of discourse.

[SOURCE: [ISO 19107:2019, 3.6](#)]

3.2

cell

<DGGs> spatial, spatio-temporal or temporal unit of geometry with dimension greater than 0, associated with a *zone* ([3.52](#))

Note 1 to entry: All cells within a *DGGS* ([3.13](#)) share the dimensionality of the DGGS's parent global ([3.24](#)) geometry. DGGS with dimensionality of 0, are not supported.

Note 2 to entry: Cells are the unit of geometry in a DGGS, and the geometry of the region of space-time occupied by a zone is a cell.

Note 3 to entry: While the terms cell and zone are often used interchangeably, strictly zone is the preferred term. Cell is entirely appropriate when specifically discussing a zone's geometry or topology.

3.3

cell refinement

<DGGS> process of subdividing *parent cells* ([3.33](#)) into descendant *child cells* ([3.4](#)) using a specified *refinement ratio* ([3.38](#)) and suite of refinement strategies

Note 1 to entry: Iterative application of cell refinements creates a hierarchy of descendant *discrete global grids* ([3.12](#)).

Note 2 to entry: Cell refinement methods may result in *child cells* that each have a single parent or that have multiple parents.

3.4

child cell

child

<DGGS> immediate descendant of a *parent cell* ([3.33](#))

Note 1 to entry: Child cells are either within a single parent cell or overlapped by multiple parent cells

3.5

class

description of a set of objects that share the same attributes, operations, methods, relationships, and semantics

Note 1 to entry: A class may use a set of interfaces to specify collections of operations it provides to its environment. The term was first used in this way in the general theory of object-oriented programming, and later adopted for use in this same sense in UML.

[SOURCE: [ISO 19103:2015, 4.7](#), modified — Note 1 to entry has been added from [ISO 19117:2012, 4.2](#)]

3.6

compound coordinate reference system

compound CRS

coordinate reference system ([3.7](#)) using at least two independent coordinate reference systems

Note 1 to entry: Coordinate reference systems are independent of each other if coordinate values in one cannot be converted or transformed into coordinate values in the other.

[SOURCE: [ISO 19111:2019, 3.1.3](#)]

3.7

coordinate reference system

CRS

coordinate system ([3.8](#)) that is related to an object by a *datum* ([3.10](#))

Note 1 to entry: Geodetic and vertical datums are referred to as reference frames.

Note 2 to entry: For geodetic and vertical datums, the object will be the Earth. In planetary applications, geodetic and vertical reference frames may be applied to other celestial bodies.

[SOURCE: [ISO 19111:2019, 3.1.9](#)]

3.8

coordinate system

set of mathematical rules for specifying how coordinates are to be assigned to points

[SOURCE: [ISO 19111:2019, 3.1.11](#)]

3.9

data type

specification of a *value* ([3.49](#)) domain with operations allowed on values in this domain

EXAMPLE Integer, Real, Boolean, String, Date (conversion of a date into a series of codes).

Note 1 to entry: Data types include primitive predefined types and user-definable types. All instances of a data type lack identity.

[SOURCE: [ISO 19103:2015, 4.14](#), modified — Note 1 to entry has been added from ISO 19156:2011, 4.3]

3.10

datum

reference frame

parameter or set of parameters that realize the positions of the origin, the scale, and the orientation of a *coordinate system* ([3.8](#))

[SOURCE: [ISO 19111:2019, 3.1.15](#)]

3.11

datum ensemble

group of multiple realizations of the same terrestrial or vertical reference system that, for approximate spatial referencing purposes, are not significantly different

EXAMPLE “WGS 84” as an undifferentiated group of realizations including WGS 84 (TRANSIT), WGS 84 (G730), WGS 84 (G873), WGS 84 (G1150), WGS 84 (G1674) and WGS 84 (G1762). At the surface of the Earth these have changed on average by 0.7 m between the TRANSIT and G730 realizations, a further 0.2 m between G730 and G873, 0.06 m between G873 and G1150, 0.2 m between G1150 and G1674 and 0.02 m between G1674 and G1762).

Note 1 to entry: Datasets referenced to the different realizations within a datum ensemble may be merged without coordinate transformation.

Note 2 to entry: ‘Approximate’ is for users to define but typically is in the order of under 1 decimetre but may be up to 2 metres.

[SOURCE: [ISO 19111:2019, 3.1.16](#)]

3.12

discrete global grid

<DGGS> set of *cells* ([3.2](#)) at the same *refinement level* ([3.37](#)), that uniquely and completely cover a *globe* ([3.24](#))

Note 1 to entry: the set of cell *zonal identifiers* ([3.50](#)) comprising a discrete global grid form a single Zone Class with its associated *refinement level* ([3.37](#)).

Note 2 to entry: the configuration of the set of cells comprising a discrete global grid satisfy at least one grid constraint in the DGG_GridConstraint codelist.

3.13

discrete global grid system

DGGS

integrated system comprising a *hierarchy* (3.26) of *discrete global grids* (3.12), *spatio-temporal referencing* (3.42) by *zonal identifiers* (3.50) and functions for *quantization* (3.36), *zonal query* (3.51), and *interoperability* (3.28)

3.14

duration

non-negative quantity of time equal to the difference between the final and initial *instants* (3.29) of a time *interval* (3.30)

Note 1 to entry: The duration is one of the base quantities in the International System of Quantities (ISQ) on which the International System of Units (SI) is based. The term “time” instead of “duration” is often used in this context and also for an infinitesimal duration.

Note 2 to entry: For the term “duration”, expressions such as “time” or “time interval” are often used, but the term “time” is not recommended in this sense and the term “time interval” is deprecated in this sense to avoid confusion with the concept of “time interval”.

Note 3 to entry: The exact duration of a time scale unit depends on the time scale used. For example, the durations of a year, month, week, day, hour or minute, may depend on when they occur [in a Gregorian calendar, a calendar month can have a duration of 28, 29, 30, or 31 days; in a 24-hour clock, a clock minute can have a duration of 59, 60, or 61 seconds, etc.]. Therefore, the exact duration can only be evaluated if the exact duration of each is known.

Note 4 to entry: This definition is closely related to NOTE 1 of the terminological entry “duration” in IEC 60050-113:2011, 113-01-13.

[SOURCE: [ISO 8601-1:2019, 3.1.1.8](#)]

3.15

dynamic coordinate reference system

dynamic CRS

coordinate reference system (3.7) that has a *dynamic reference frame* (3.16)

Note 1 to entry: Coordinates of points on or near the crust of the Earth that are referenced to a dynamic coordinate reference system may change with time, usually due to crustal deformations such as tectonic motion and glacial isostatic adjustment.

Note 2 to entry: Metadata for a dataset referenced to a dynamic coordinate reference system should include coordinate epoch information.

[SOURCE: [ISO 19111:2019, 3.1.19](#)]

3.16

dynamic reference frame

dynamic datum

reference frame (3.10) in which the defining parameters include time evolution

Note 1 to entry: The defining parameters that have time evolution are usually a coordinate set.

[SOURCE: [ISO 19111:2019, 3.1.20](#)]

3.17

error budget

<metric> statement of or methodology for describing the nature and magnitude of the errors which affect the results of a calculation

[SOURCE: [ISO 19107:2019, 3.35](#), modified — Note 1 to entry has been removed]

3.18

feature

abstraction of real-world phenomena

Note 1 to entry: A feature can occur as a type or an instance. In this document, feature instance is meant unless otherwise specified.

[SOURCE: [ISO 19101-1:2014, 4.1.11](#), modified — Note 1 to entry has been added from ISO 19156:2011, 4.6, and modified]

3.19

feature type

class ([3.5](#)) of *features* ([3.18](#)) having common characteristics

[SOURCE: [ISO 19156:2011, 4.7](#)]

3.20

geodetic coordinate reference system

geodetic CRS

three-dimensional coordinate reference system (3.7) based on a geodetic reference frame and having either a three-dimensional Cartesian or a spherical coordinate system

Note 1 to entry: In this document a *coordinate reference system* ([3.7](#)) based on a geodetic reference frame and having an ellipsoidal coordinate system is geographic.

[SOURCE: [ISO 19111:2019, 3.1.31](#)]

3.21

geographic coordinate reference system

geographic CRS

coordinate reference system ([3.7](#)) that has a geodetic reference frame and an ellipsoidal coordinate system

[SOURCE: [ISO 19111:2019, 3.1.35](#)]

3.22

geographic identifier

spatial reference ([3.41](#)) in the form of a label or code that identifies a *location* ([3.31](#))

EXAMPLE “Spain” is an example of a label (country name); “SW1P 3AD” is an example of a code (postcode).

[SOURCE: [ISO 19112:2019, 3.1.2](#)]

3.23

geometric primitive

geometric object representing a single, connected, homogeneous (isotropic) element of space

Note 1 to entry: Geometric primitives are non-decomposed objects that present information about geometric configuration. They include points, curves, surfaces, and solids. Many geometric objects behave like primitives (supporting the same interfaces defined for geometric primitives) but are actually composites composed of some number of other primitives. General collections may be aggregates and incapable of acting like a primitive (such as the lines of a complex network, which is not connected and thus incapable of being traceable as a single line). By

this definition, a geometric primitive is topological open, since the *boundary* (3.1) points are not isotropic to the interior points. Geometry is assumed to be closed. For points, the boundary is empty.

[SOURCE: [ISO 19107:2019, 3.50](#)]

3.24

globe

<DGGS> region of space-time enclosing a celestial body

Note 1 to entry: In this document globe is used in its most general form to refer to any celestial body or region of space-time enclosing a celestial body that may be referenced by a *DGGS* (3.13). When a specific body, such as the Earth is referred to, an explicit term is used.

3.25

grid

network composed of two or more sets of curves in which the members of each set intersect the members of the other sets in an algorithmic way

Note 1 to entry: The curves partition a space into grid cells.

[SOURCE: [ISO 19123:2005, 4.1.23](#)]

3.26

hierarchy

<DGGS> organization and ranking of successive levels of *cell refinement* (3.3) of *discrete global grids* (3.12)

3.27

initial discrete global grid

<DGGS> discrete global grid tessellation created by circumscribing a defined path along the chosen surface model of the Earth between the vertices of the scaled base unit polyhedron

3.28

interoperability

capability to communicate, execute programmes, or transfer data among various functional units in a manner that requires the user to have little or no knowledge of the unique characteristics of those units

Note 1 to entry: In this document, interoperability specifically refers to functions that initiate and process transfers of data from a DGGS (3.13).

[SOURCE: [ISO/IEC 2382:2015, 2121317](#), modified—The original domain and Notes to Entry have been deleted. A Note 1 to entry has been added.]

3.29

instant

<DGGS> temporal geometry primitive representing a point in time

Note 1 to entry: On *temporal coordinate systems* (3.46) as specified in ISO 19107, the temporal *geometric primitives* (3.23) *instant* (3.30) and *interval* (3.30) are the equivalent of points and lines as specified in ISO 19107.

3.30

interval

<DGGS> temporal geometry primitive representing a line in time

Note 1 to entry: On *temporal coordinate systems* (3.46) as specified in ISO 19107, the temporal *geometric primitives* (3.23) *instant* (3.29) and *interval* are the equivalent of points and lines as specified in ISO 19107.

3.31**location**

particular place or position

EXAMPLE “Madrid”, “SW1P 3AD”.

Note 1 to entry: A location identifies a geographic place.

Note 2 to entry: In the context of *DGGS* (3.13), locations have dimension greater than one, and so are not points.

[SOURCE: [ISO 19112:2019, 3.1.3](#), modified — Note two has been added and an additional example provided]

3.32**observation**

act of measuring or otherwise determining the *value* (3.49) of a property

[SOURCE: [ISO 19156:2011, 4.11](#)]

3.33**parent cell**

parent

<DGGS> *cell* (3.2) in a higher refinement level of discrete global grid with immediate descendants

Note 1 to entry: parent cells either overlap or contain their *child cells* (3.4).

3.34**period**

<DGGS> particular era or span of time

Note 1 to entry: Periods are *intervals* (3.30) named with a *period identifier* (3.35)

3.35**period identifier**

<DGGS> temporal reference in the form of a label or code that identifies a *period* (3.34)

Note 1 to entry: Period identifiers are the temporal equivalent of *geographic identifiers* (3.22) as specified in [ISO 19112](#)

3.36**quantization**

<DGGS> function assigning data from external sources to cell values

3.37**refinement level**

<DGGS> numerical order of a *discrete global grid* (3.12) in the tessellation sequence

Note 1 to entry: The tessellation with the smallest number of cells has a refinement level = 0.

3.38**refinement ratio**

<DGGS> ratio of the number of *child cells* (3.4) to *parent cells* (3.33)

Note 1 to entry: A positive integer ratio *n* refinement of *DGGS* (3.13) parent cells yield *n* times as many child cells as parent cells.

Note 2 to entry: For a two-dimensional DGGS (as defined for EAERS in this document) this is the surface area ratio.

Note 3 to entry: In DGGs literature [\[34\]](#) the term aperture has been used instead of refinement ratio. Refinement ratio is preferred because it is clearer in meaning to audiences outside the early DGGs community.

3.39

sibling cell

sibling

<DGGs> *cell* ([3.2](#)) in a discrete global grid with the same *parent cell* ([3.33](#))

Note 1 to entry: all the *child cells* ([3.4](#)) of a parent cell are each-others' sibling cells.

3.40

simple

<topology, geometry> homogeneous (all points have isomorphic neighbourhoods) and with a simple *boundary* ([3.1](#))

Note 1 to entry: The interior is everywhere locally isomorphic to an open disc in a Euclidean coordinate space of the appropriate dimension $D^n = \{P \mid \|P\| < 1.0\}$. The boundary is a dimension one smaller. This essentially means that the object does not intersect nor touch itself. Generally used for a curve that does not cross not touch itself with the possible exception of boundary points. Simple closed curves are isomorphic to a circle.

[SOURCE: [ISO 19107:2019, 3.84](#)]

3.41

spatial reference

description of position in the real world

Note 1 to entry: This may take the form of a label, code or coordinate tuple.

[SOURCE: [ISO 19111:2019, 3.1.56](#)]

3.42

spatio-temporal reference

system for identifying position in the real world that may include time

Note 1 to entry: This may take the form of a label, code or coordinate tuple.

3.43

spatio-temporal coordinate reference system

spatio-temporal CRS

compound coordinate reference system ([3.6](#)) in which one constituent *coordinate reference system* ([3.7](#)) is a spatial coordinate reference system and one is a *temporal coordinate reference system* ([3.47](#))

[SOURCE: [ISO 19111:2019, 3.1.59](#)]

3.44

static coordinate reference system

static CRS

coordinate reference system ([3.7](#)) that has a *static reference frame* ([3.45](#))

Note 1 to entry: Coordinates of points on or near the crust of the Earth that are referenced to a dynamic coordinate reference system do not change with time.

Note 2 to entry: Metadata for a dataset referenced to a static coordinate reference system does not require coordinate epoch information.

[SOURCE: [ISO 19111:2019, 3.1.61](#)]

3.45**static reference frame**

static datum

reference frame (3.10) in which the defining parameters exclude time evolution[SOURCE: [ISO 19111:2019, 3.1.62](#)]**3.46****temporal coordinate system**

<geodesy> one-dimensional coordinate system where the axis is time

[SOURCE: [ISO 19111:2019, 3.1.64](#)]**3.47****temporal coordinate reference system**

temporal CRS

coordinate reference system (3.7) based on a temporal datum

[SOURCE: [ISO 19111:2019, 3.1.63](#)]**3.48****tessellation**

partitioning of a space into a set of conterminous subspaces having the same dimension as the space being partitioned

EXAMPLE Graphic examples of tessellations may be found in Figures 11, 13, 20, and 22 of [ISO 19123:2005](#).

Note 1 to entry: A tessellation composed of congruent regular polygons or polyhedra is a regular tessellation. One composed of regular, but non-congruent polygons or polyhedra is a semi-regular tessellation. Otherwise the tessellation is irregular. Tessellations on curved surfaces cannot be congruent, so all tessellations in DGGS are either semi-regular or irregular.

[SOURCE: [ISO 19123:2005, 4.1.39](#), modified — Note 1 to entry has been modified and new notes to entry have been added.]

3.49**value**

element of a type domain

Note 1 to entry: A value considers a possible state of an object within a *class* (3.5) or type (domain).

Note 2 to entry: A data value is an instance of a datatype, a value without identity.

Note 3 to entry: A value can use one of a variety of scales including nominal, ordinal, ratio and interval, spatial and temporal. Primitive datatypes can be combined to form aggregate datatypes with aggregate values, including vectors, tensors and images.

[SOURCE: [ISO 19156:2011, 4.18](#)]**3.50****zonal identifier**<DGGS> *spatio-temporal reference* (3.42) in the form of a label or code that identifies a *zone* (3.52)

Note 1 to entry: A zonal identifier may be a *geographic identifier* (3.22), *period identifier* (3.35), or a compound of the two.

Note 2 to entry: A zone's ZonalIdentifier provides the coordinates of a representative position for the zone, and spatio-temporal feature geometry is represented by sets of ZonalIdentifiers.

3.51

zonal query

<DGGS> geometry or topology function using a cell's *zonal identifiers* ([3.50](#)) to specify geometry

Note 1 to entry: ISO 19107 specifies a suite of geometry and topology functions in the Query2D and Query3D classes, where geometry elements used in each function's parameters are described by sets of coordinates. In DGGS all geometry can be referenced as sets of *cells* ([3.2](#)) represented solely by a list (or set) of their zonal identifiers. This document specifies ZoneQuery to implement the operations in both Query2D and Query3D using zonal identifiers to reference each operation's source and target geometry.

3.52

zone

<DGGS> particular region of space-time

Note 1 to entry: The primitives of zone are spatial *location* ([3.31](#)) and temporal *period* ([3.34](#)).

Note 2 to entry: A zone may be either a single zonal primitive or a compound zone comprising one spatial location and one temporal period. Zones can be regions of space-time associated with any celestial body.

Note 3 to entry: Zones are the primary container for storing and retrieving data within a DGGS implementation. DGGSs reference zones by their *zonal identifier* ([3.50](#)), for instance in databases or through tile nomenclature.

Note 4 to entry: Each zone's geometry is represented by a cell ([3.2](#)).

4 Conventions

4.1 Abbreviated terms

DE-9IM	Dimensionally Extended 9-Intersection Model
EAERS	equal-area Earth RS
GEM	Geodesic Elevation Model
GIS	geographic information system
GUID	globally unique identifier
HPC	high-performance computing
HPD	high-performance data
ICT	information and communications technology
ISEA	Icosahedral Snyder Equal Area
ISEA3H	Icosahedral Snyder Equal Area Aperture 3 Hexagon
ISO	International Organization for Standardization
OGC	Open Geospatial Consortium

OWS	OGC Web-Service
QTM	Quaternary Triangular Mesh
rHEALPix	rearranged Hierarchical Equal Area isoLatitude Pixelization
RS	reference system
UML	Unified Modeling Language
URI	Uniform Resource Identifier

4.2 Universal Resource Identifiers

The normative provisions in this specification are denoted by the URI:

<http://www.opengis.net/spec/dggs/2.0>

All requirements and conformance tests that appear in this document denoted by partial URIs are relative to this base.

4.3 Unified Modeling Language notation

In this document, the conceptual schema for describing discrete global grid systems are presented in UML. ISO 19103 presents the specific profile of UML used in this document.

The UML diagrams in this document refer to classifiers in five other standards. Each standard has been assigned a colour that is used consistently across all UML diagrams. Each diagram has a key listing the standards referred to in that diagram and their colours. Interface names in the figure have the structure <module-name>::<interface-name>. For reference, Table 1 lists all the module names and the standard they belong to. Both colour and module name can be used as quick reference to a classifier's standard.

4.4 Naming conventions

Where possible, when a classifier represents the common behaviour of a set of defined things from the terms defined in Clause 3, the UML classifier will generally use the defined terms as its name. Since classifier names are capitalized and contain no space, and the defined term may contain several words, the classifier name will separate words using upper-camel-case concatenations (no spaces but each word beginning with a capital with all other letters in lowercase). Similarly, the name may be some simplified key phrase. This "UpperCamelCase" rule is generally followed but may be violated if clarity or consistency with other standards is improved by minor violations. For example:

- Zone identifier values are represented by the interface ZonalIdentifier or stored using the datatype DirectPosition defined in [ISO 19107](#).
- Instances of primitives will realize the interface Primitive in the package Common Spatio-temporal Classes and other interfaces for their specific dimension and interpolation mechanism. For example, Point, Instant, Interval, Line, NodeT, LocationS.
- Any classifier name referenced from another standard retains its original format.

Classifier names for attributes and operations in the UML models may similarly use key phrases in lowerCamelCase (same as UpperCamelCase, but the first word begins in a lowercase letter). For example: parent; child; parentOf; childOf and relatePosition are all used as operation names.

Module and package names can contain spaces. In some situations, a phrase that has an abbreviation is used in its unabbreviated form as a package name. Where a package or module is referred to in the text, both the capitalisation and unabbreviated form are preserved. This distinguishes them from a phrase in general use. For example: DGGs Equal-Area Earth Reference System; Zone and Temporal Geometry; and Reference System defined in this standard and Coordinate Reference Systems defined in [ISO 19111](#).

In summary, the use of capitals for a term in the general text indicates a reference to a classifier from the UML.

4.5 Attribute and association role status

In this document, conceptual schema in Clauses 6–8 are defined by tables. In these tables:

- attributes and association roles are given an **Obligation** status:
 - **M**: mandatory — this attribute or association role shall be supplied.
 - **C**: conditional — this attribute or association role shall be supplied if the condition (given in the description) is true. It may be supplied if the condition is false.
 - **O**: optional — this attribute or association role may be supplied.
- the **Maximum Occurrence** column in the tables indicates the maximum number of occurrences of attribute values that are permissible, with * indicating no upper limit.
- non-navigable associations are not included in the UML diagrams or tables.

The tables provide a summary of the UML diagrams. In particular, association roles, attributes, operations, and constraints that are inherited from another class unchanged are not described in the tables. In the event of any discrepancies between the UML diagrams and text, the UML shall prevail.

5 DGGs specification overview

5.1 Package overview

The specification for DGGs is described in this document in the form of a UML model with supplementary defining tables and text. The UML data model is organised into three primary packages. The Common Spatio-temporal Classes package contains two UML sub-packages, DGGs Core contains four UML sub-packages, and Equal-Area Earth DGGs is a single UML package, as shown in Figure 2.

- a) Common Spatio-temporal Classes package contains
 - 1) Zone and Temporal Geometry package, comprising temporal and spatio-temporal primitives for geometry and topology,
 - 2) Zone, Identifier and RS package, comprising temporal and spatio-temporal RS using identifiers and their primitives.
- b) DGGs Core package contains:
 - 1) Core RS using zonal identifiers with structured geometry package,
 - 2) Core Quantization Functions package,
 - 3) Core Query Functions package,
 - 4) Core Interoperation Functions package.
- c) Equal-Area Earth DGGs package.

In Figure 2, each box represents a package and contains the package name. Each arrowed line shows the dependency of one package upon another package (at the head of the arrow). The Common Spatio-temporal Classes, DGGs Core and Equal-Area Earth DGGs packages are in turn dependent on packages in five other ISO standards.

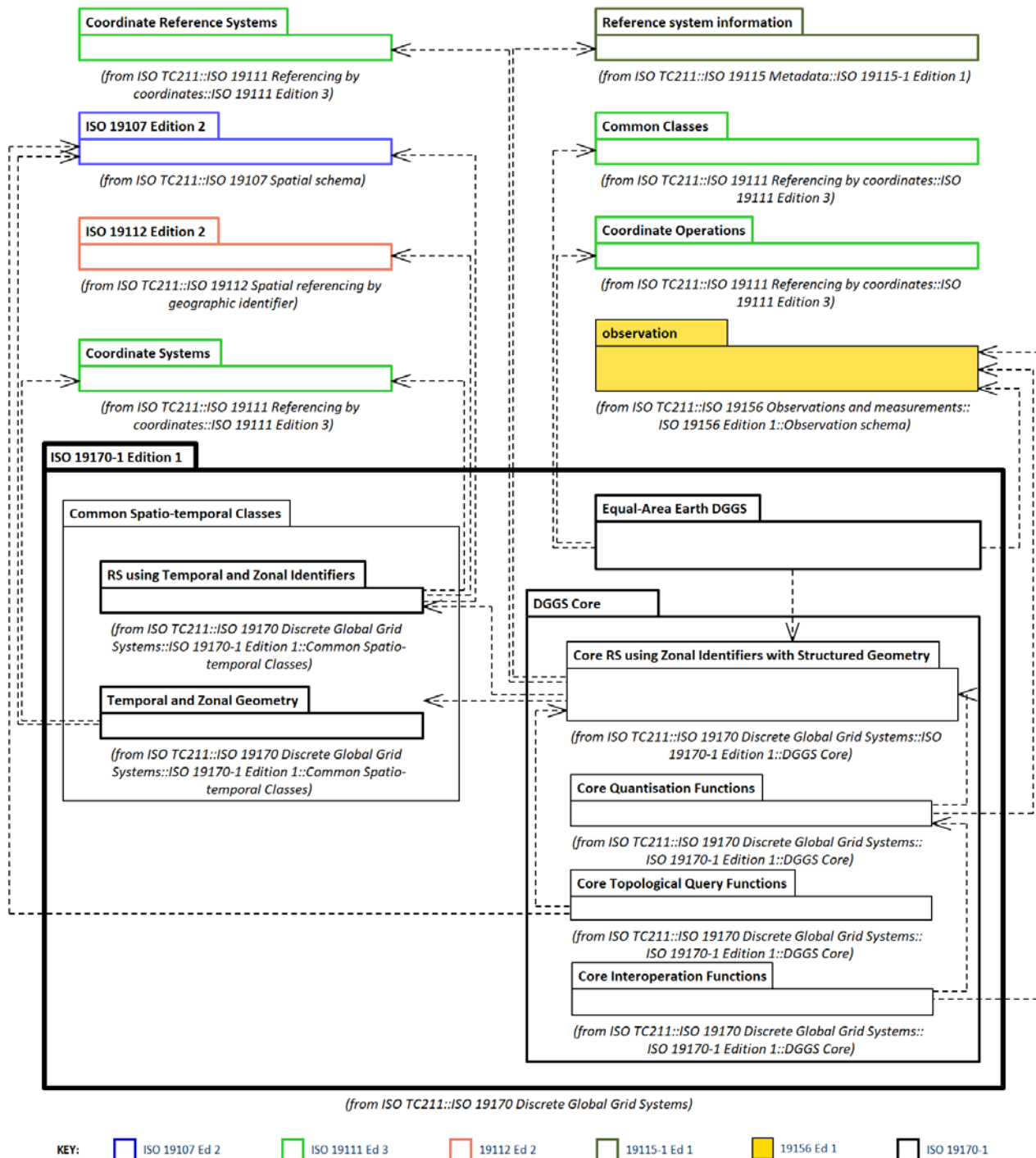


Figure 2 — DGGs Package Diagram

Packages are grouped in a hierarchy of sub-packages, with modules containing interfaces at the leaves of the hierarchy. In the UML diagrams that follow, interface names are often shown as <module-name>::<interface-name>. For reference, Table 1 lists all the module names that are referred to in the diagrams and names the standard they come from.

Table 1 — Module names used in UML diagrams in this document

Standard name		Module name
ISO 19107:2019 Spatial Schema Ed 2		Edge
		Geometry
		Node
		Topology
ISO 19111:2019 Referencing by Coordinates Ed 3		Common Classes
		Coordinates
		Coordinate Operations
		Coordinate Reference System
		Coordinate Systems
ISO 19112:2019 Spatial referencing by geographic identifier Ed 2		ISO 19112 Edition 2
ISO 19115-1:2014 Metadata Ed 1		Reference system information
ISO 19156:2011 Observation and Measurements Ed 1		Observation
ISO 19170-1 Discrete Global Grid Systems Ed 1	Common Spatio-temporal Classes	Temporal Geometry and Topology
		Zonal Geometry and Topology
		Temporal RS using Identifiers
		Spatial Location
		Zonal RS using Identifiers
	DGGS Core	Core RS using Zonal Identifiers with Structured Geometry
		Core Quantization Functions
		Core Topological Query Functions
		Core Interoperation Functions
		Interoperation Query
		Interoperation Broadcast
	Equal-Area Earth DGGS	Equal-Area Earth RS
		Equal-Area Tessellation
		Equal-Area Cell

Conformance classes for the modules in the Common Spatio-temporal Classes, DGGS Core, and Equal-Area Earth DGGS packages are described in [Annex A](#).

One product conformance class is also defined for an Equal-Area Earth DGGS product, that brings modules together as a system.

6 Common Spatio-temporal Classes package

6.1 Common Spatio-temporal Classes overview

This clause specifies the common spatio-temporal classes to support temporal and spatio-temporal geometry, topology, zones, zonal identifiers, zonal query, and RSs using temporal or zonal identifiers.

These classes are defined here in such a way that they can be used in any context which requires an internally consistent set of temporal and spatio-temporal classes for use with spatial classes from ISO 19107:2019, 19111:2019 and 19112:2019. They are further specialised in the DGGS Core for use in DGGS. In this restricted model for spatio-temporal systems, the spatio-temporal scope is constrained to spatial classes that are invariant through all time, and to temporal classes that are invariant throughout space.

The Common Spatio-temporal Classes are organized into two packages with five modules:

- a) Temporal and Zonal Geometry package comprises:
 - 1) Temporal Geometry and Topology module
 - 2) Zonal Geometry and Topology module
- b) RS using Temporal and Zonal Identifiers package comprises:
 - 1) Spatial Location module
 - 2) Temporal RS using Identifiers module
 - 3) Zonal RS using Identifiers module

In each package separate spatial and temporal classes are defined first, followed by spatio-temporal classes that bring temporal and spatial classes together.

6.2 Temporal and Zonal Geometry package

6.2.1 Temporal Geometry and Topology module

6.2.1.1 Context and data model

Temporal geometry is geometry constrained to one of the temporal coordinate systems, defined by TemporalCS in ISO 19111:2019. Temporal geometry primitives instant and interval implement the temporal analogues of point and line respectively in ISO 19107:2019. All geometry has topology, and the temporal topology primitives nodeT and edgeT implement the temporal analogues of node and edge respectively. These are shown in Figure 3.

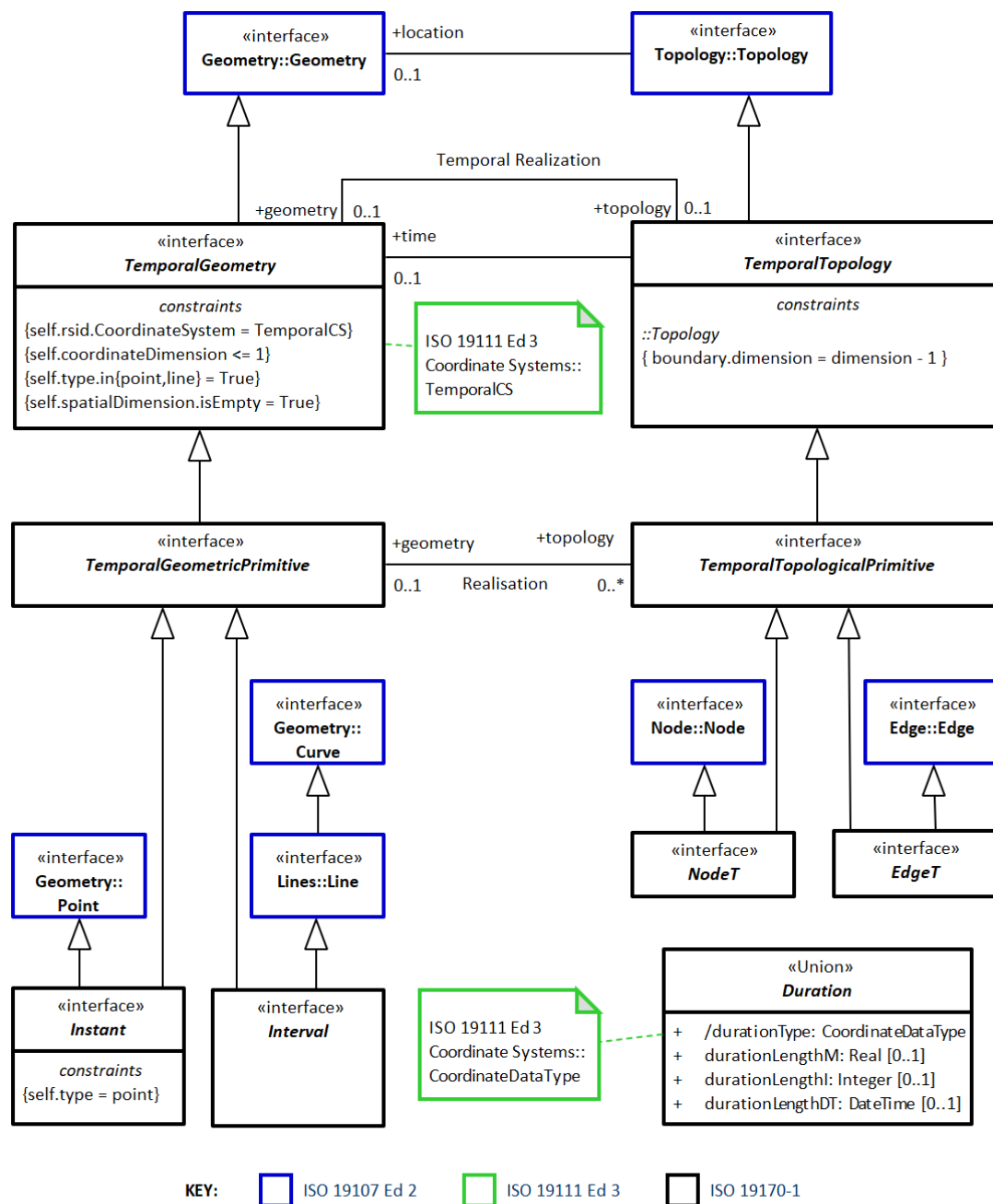


Figure 3 — Primitives of Temporal Geometry and Topology

Temporal interfaces paralleling the spatial geometry and topology interface structure are built from these temporal primitives. Each temporal interface has the same meaning and semantics as their equivalent spatial interface, with the constraint that all temporal interfaces are constrained to the same coordinate system as their temporal primitives. Figure 4 shows the spatial classes on the left and their temporal equivalents on the right.

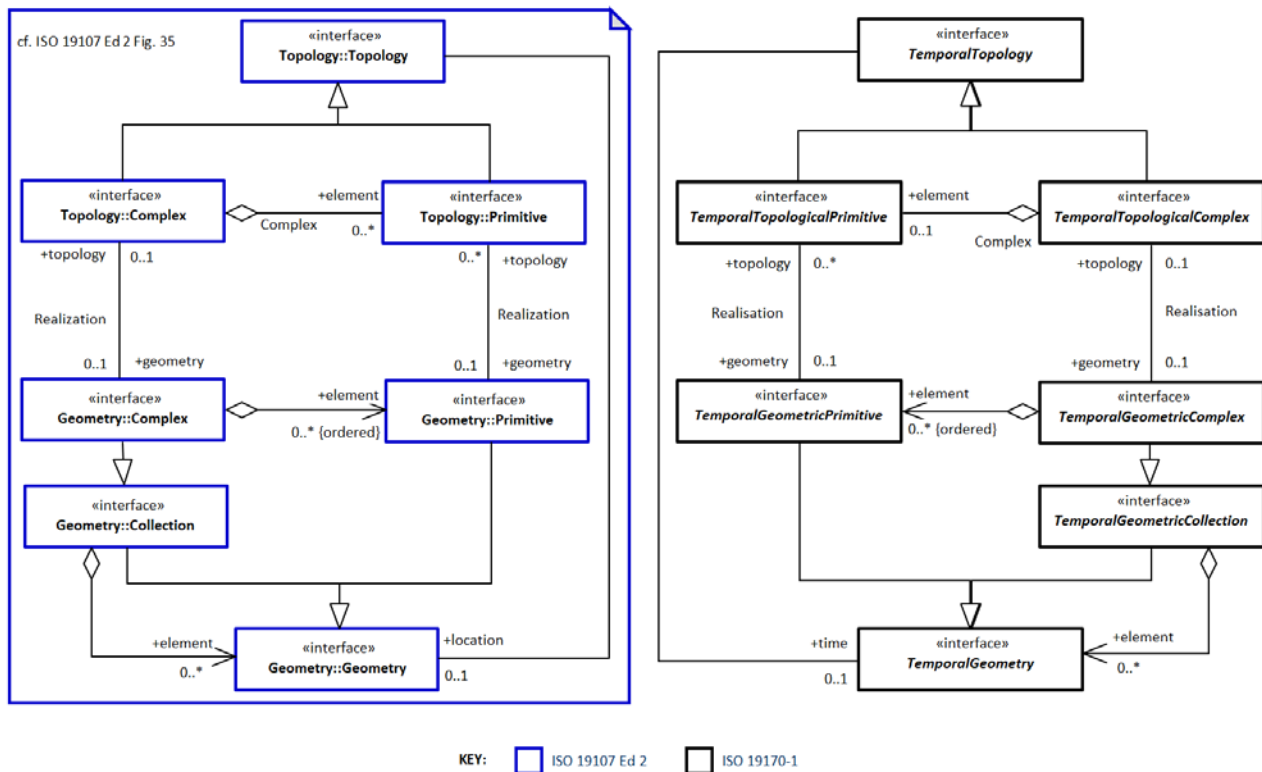


Figure 4 — ISO 19107:2019 Ed 2 Context for Temporal Geometry and Topology

6.2.1.2 Defining tables

- Table 2 Elements of Temporal Geometry and Topology::Duration
- Table 3 Elements of Temporal Geometry and Topology::EdgeT
- Table 4 Elements of Temporal Geometry and Topology::Instant
- Table 5 Elements of Temporal Geometry and Topology::Interval
- Table 6 Elements of Temporal Geometry and Topology::NodeT
- Table 7 Elements of Temporal Geometry and Topology::TemporalGeometricCollection
- Table 8 Elements of Temporal Geometry and Topology::TemporalGeometricComplex
- Table 9 Elements of Temporal Geometry and Topology::TemporalGeometricPrimitive
- Table 10 Elements of Temporal Geometry and Topology::TemporalGeometry
- Table 11 Elements of Temporal Geometry and Topology::TemporalTopologicalComplex
- Table 12 Elements of Temporal Geometry and Topology::TemporalTopologicalPrimitive
- Table 13 Elements of Temporal Geometry and Topology::TemporalTopology

Table 2 — Elements of Temporal Geometry and Topology::Duration

Name:	Duration					
Definition:	Duration implements Length on a Temporal Coordinate System.					
Stereotype:	Union					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	durationLengthDT	Length of time for Duration of type DateTime.		C	1	DateTime
	durationLengthI	Length of time for Duration of type Integer count.		C	1	Integer
	durationLengthM	Length of time for Duration of type Real measure.		C	1	Real
	durationType	Type of unit of measure for time.	true	M	1	CoordinateDataType
Constraints:	(none)					

Table 3 — Elements of Temporal Geometry and Topology::EdgeT

Name:	EdgeT
Definition:	Topological temporal edge, one-dimensional topological primitive.
Stereotype:	Interface
Inheritance from:	TemporalTopologicalPrimitive
Abstract:	true
Associations:	(none)
Public attributes:	(none)
Constraints:	(none)

Table 4 — Elements of Temporal Geometry and Topology::Instant

Name:	Instant
Definition:	Instant implements Point geometry on a Temporal Coordinate System.
Stereotype:	Interface
Inheritance from:	TemporalGeometricPrimitive
Abstract:	true
Associations:	(none)
Public attributes:	(none)
Constraints:	self.type = point

Table 5 — Elements of Temporal Geometry and Topology::Interval

Name:	Interval
Definition:	Interval implements Line geometry on a Temporal Coordinate System.
Stereotype:	Interface
Inheritance from:	TemporalGeometricPrimitive
Abstract:	true
Associations:	(none)
Public attributes:	(none)
Constraints:	(none)

Table 6 — Elements of Temporal Geometry and Topology::NodeT

Name:	NodeT
Definition:	Topological temporal node, zero-dimensional topological primitive, its boundary being empty.
Stereotype:	Interface
Inheritance from:	TemporalTopologicalPrimitive
Abstract:	true
Associations:	(none)
Public attributes:	(none)
Constraints:	(none)

Table 7 — Elements of Temporal Geometry and Topology::TemporalGeometricCollection

Name:	TemporalGeometricCollection			
Definition:	Temporal Geometric Collection implements geometric Collection for Temporal Geometry.			
Stereotype:	Interface			
Inheritance from:	TemporalGeometry			
Generalization of:	TemporalGeometricComplex			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	TemporalGeometry (feature type)	C	*	element
Public attributes:	(none)			
Constraints:	(none)			

Table 8 — Elements of Temporal Geometry and Topology::TemporalGeometricComplex

Name:	TemporalGeometricComplex			
Definition:	Temporal Geometric Complex implements geometric Complex for Temporal Geometry.			
Stereotype:	Interface			
Inheritance from:	TemporalGeometricCollection			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	TemporalGeometricPrimitive (feature type)	C	*	element
	TemporalTopologicalComplex (feature type)	C	1	topology
Public attributes:	(none)			
Constraints:	(none)			

Table 9 — Elements of Temporal Geometry and Topology::TemporalGeometricPrimitive

Name:	TemporalGeometricPrimitive					
Definition:	Temporal Geometric Primitive implements geometric Primitive for Temporal Geometry.					
Stereotype:	Interface					
Inheritance from:	TemporalGeometry					
Generalization of:	Instant, Interval					
Abstract:	true					
Associations:	<i>Association with:</i>			<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	TemporalTopologicalPrimitive (feature type)			C	*	topology
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	spatialDimension	Dimension of its spatial geometry component.		M	1	Integer
	temporalDimension	Dimension of its temporal geometry component.		M	1	Integer
Constraints:	(none)					

Table 10 — Elements of Temporal Geometry and Topology::TemporalGeometry

Name:	TemporalGeometry				
Definition:	Temporal Geometry implements 1D Geometry on a Temporal Coordinate System.				
Stereotype:	Interface				
Inheritance from:	ZoneSimpleGeometry				
Generalization of:	TemporalGeometricCollection, TemporalGeometricPrimitive				
Abstract:	true				
Associations:	<i>Association with:</i>		<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	TemporalTopology (feature type)		C	1	topology
Public attributes:	(none)				
Constraints:	self.coordinateDimension <= 1				
	self.rsid.CoordinateSystem = TemporalCS				
	self.spatialDimension.isEmpty = True				
	self.type.in{point,line} = True				

Table 11 — Elements of Temporal Geometry and Topology::TemporalTopologicalComplex

Name:	TemporalTopologicalComplex				
Definition:	Temporal Topological Complex implements topological Complex for Temporal Topology.				
Stereotype:	Interface				
Inheritance from:	TemporalTopology				
Abstract:	true				
Associations:	<i>Association with:</i>		<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	TemporalTopologicalPrimitive (feature type)		C	1	element
	TemporalGeometricComplex (feature type)		C	1	geometry
Public attributes:	(none)				
Constraints:	(none)				

Table 12 — Elements of Temporal Geometry and Topology::TemporalTopologicalPrimitive

Name:	TemporalTopologicalPrimitive			
Definition:	Temporal Topological Primitive implements topological Primitive for Temporal Topology.			
Stereotype:	Interface			
Inheritance from:	TemporalTopology			
Generalization of:	EdgeT, NodeT			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	TemporalGeometricPrimitive (feature type)	C	1	geometry
Public attributes:	(none)			
Constraints:	(none)			

Table 13 — Elements of Temporal Geometry and Topology::TemporalTopology

Name:	TemporalTopology			
Definition:	Temporal Topology implements 1D Topology for Temporal Geometry.			
Stereotype:	Interface			
Inheritance from:	ZoneSimpleTopology			
Generalization of:	TemporalTopologicalComplex, TemporalTopologicalPrimitive			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	TemporalGeometry (feature type)	C	1	geometry
	TemporalGeometry (feature type)	C	1	time
Public attributes:	(none)			
Constraints:	(none)			

The following requirement applies:

Requirement 19: www.opengis.net/spec/DGGS/2.0/req/cc/temporal/geometry

The common classes for temporal geometry and topology shall conform to the data model in Figure 3 and Figure 4 and defining tables in Table 2–Table 13.

6.2.2 Zonal Geometry and Topology module

6.2.2.1 Context and data model

Referring to Figure 5, ZoneGeometry is either a primitive of ZoneSingleGeometry or a compound of two ZoneSingleGeometry primitives — one spatial and one temporal.

Zones exhibit topology of the same spatio-temporal dimension as their geometry.

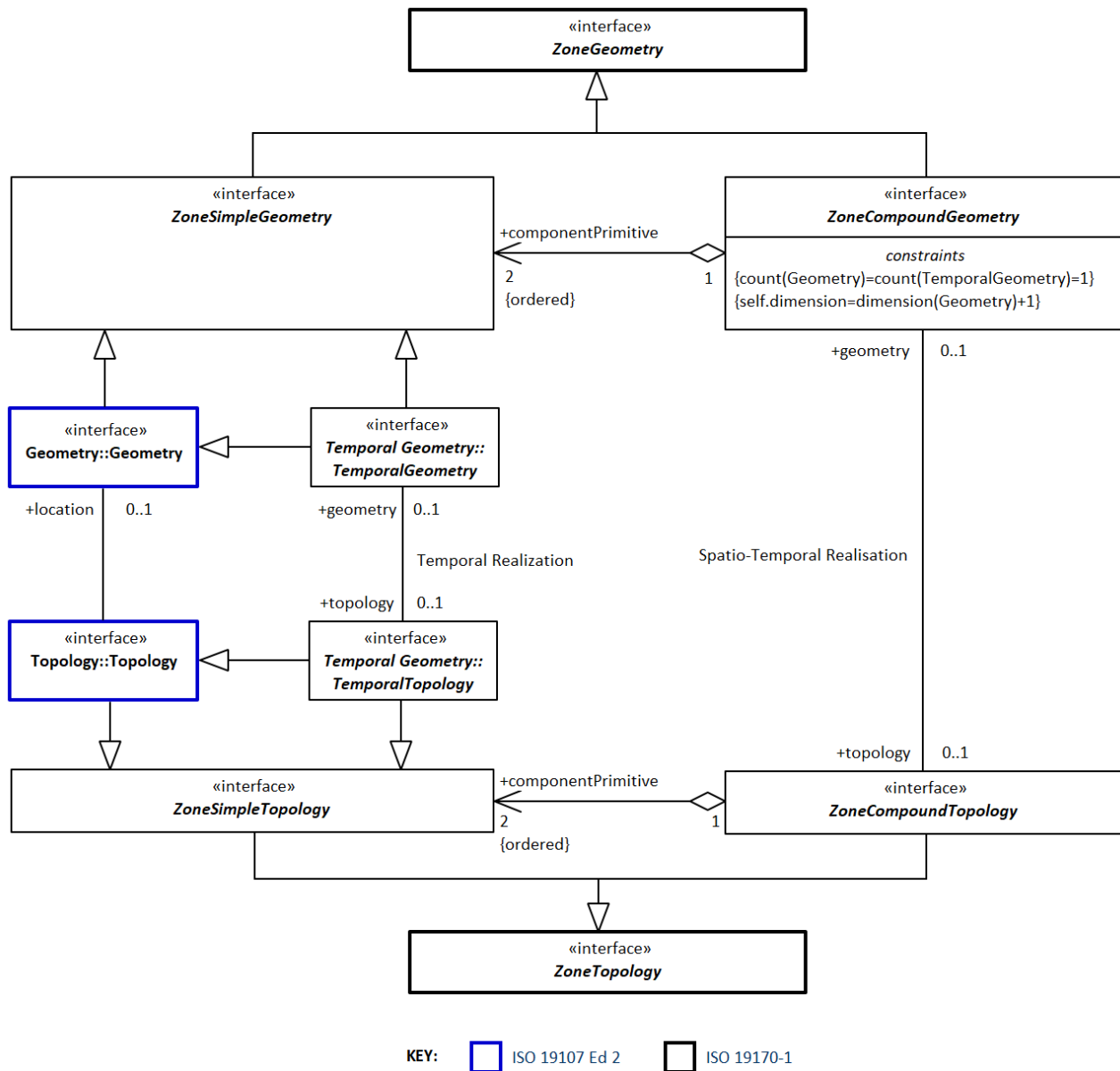


Figure 5 — Components of Zonal Geometry and Topology module

6.2.2.2 Defining tables

- a) Table 14 Elements of Zonal Geometry and Topology::ZoneCompoundGeometry
- b) Table 15 Elements of Zonal Geometry and Topology::ZoneCompoundTopology
- c) Table 16 Elements of Zonal Geometry and Topology::ZoneGeometry
- d) Table 17 Elements of Zonal Geometry and Topology::ZoneSimpleGeometry
- e) Table 18 Elements of Zonal Geometry and Topology::ZoneSimpleTopology
- f) Table 19 Elements of Zonal Geometry and Topology::ZoneTopology

Table 14 — Elements of Zonal Geometry and Topology::ZoneCompoundGeometry

Name:	ZoneCompoundGeometry			
Definition:	ZoneCompoundGeometry is a Compound of two ZoneSimpleGeometry elements, comprising one one-, two- or three-dimensional spatial geometry and one one-dimensional temporal geometry. NOTE This is analogous to an ISO 19111 Compound set of orthogonal space time axes comprising a set of orthogonal spatial axes and one temporal axis orthogonal to the spatial axes. ZoneCompoundGeometry has ZoneCompoundTopology.			
Stereotype:	Interface			
Inheritance from:	ZoneGeometry			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	ZoneSimpleGeometry (feature type)	M	2	componentPrimitive
	ZoneCompoundTopology (feature type)	C	1	topology
Public attributes:	(none)			
Constraints:	count(Geometry)=count(TemporalGeometry)=1			
	self.dimension=dimension(Geometry)+1			

Table 15 — Elements of Zonal Geometry and Topology::ZoneCompoundTopology

Name:	ZoneCompoundTopology			
Definition:	ZoneCompoundTopology exhibits both spatial topology with respect to the spatial component of its geometry and temporal topology with respect to the temporal component of its geometry			
Stereotype:	Interface			
Inheritance from:	ZoneTopology			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	ZoneSimpleTopology (feature type)	M	2	componentPrimitive
	ZoneCompoundGeometry (feature type)	C	1	geometry
Public attributes:	(none)			
Constraints:	(none)			

Table 16 — Elements of Zonal Geometry and Topology::ZoneGeometry

Name:	ZoneGeometry					
Definition:	ZoneGeometry is a ZoneSimpleGeometry or a ZoneCompoundGeometry. It is the root geometry for all spatio-temporal geometry					
Stereotype:	Interface					
Generalization of:	ZoneCompoundGeometry, ZoneSimpleGeometry					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	spatialDimension	topological dimension of the spatial geometry component		M	1	Integer
	temporalDimension	dimension of the temporal geometry component		M	1	Integer
	topologicalDimension	sum dimension of topological primitive		M	1	Integer
Constraints:	(none)					

Table 17 — Elements of Zonal Geometry and Topology::ZoneSimpleGeometry

Name:	ZoneSimpleGeometry					
Definition:	ZoneSimpleGeometry is a 1D, 2D or 3D spatial geometry that is invariant over all time, OR a 1D temporal geometry invariant over all space. A ZoneSimpleGeometry has topology appropriate for its geometry.					
Stereotype:	Interface					
Inheritance from:	ZoneGeometry					
Abstract:	true					
Associations:	(none)					
Public attributes:	(none)					
Constraints:	(none)					

Table 18 — Elements of Zonal Geometry and Topology::ZoneSimpleTopology

Name:	ZoneSimpleTopology					
Definition:	ZoneSimpleTopology is a 1D, 2D or 3D spatial topology that is invariant over all time, OR a 1D temporal topology that is invariant over all space.					
Stereotype:	Interface					
Inheritance from:	ZoneTopology					
Abstract:	true					
Associations:	(none)					
Public attributes:	(none)					
Constraints:	(none)					

Table 19 — Elements of Zonal Geometry and Topology::ZoneTopology

Name:	ZoneTopology
Definition:	ZoneTopology is a ZoneSimpleTopology or a ZoneCompoundTopology
Stereotype:	Interface
Generalization of:	ZoneCompoundTopology, ZoneSimpleTopology
Abstract:	true
Associations:	(none)
Public attributes:	(none)
Constraints:	(none)

The following requirement applies:

Requirement 20: www.opengis.net/spec/DGGS/2.0/req/cc/zone/geometry

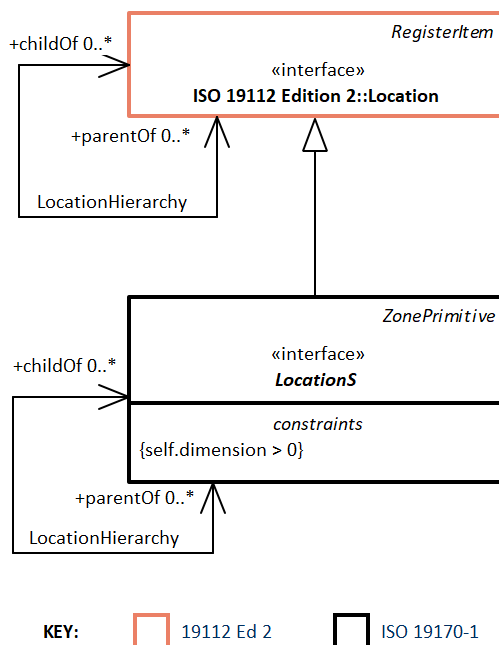
The common classes for zonal geometry and topology shall conform to the data model in Figure 5 and defining tables in Table 14–Table 19.

6.3 Temporal and Zonal RS using Identifiers package

6.3.1 Spatial Location module

6.3.1.1 Context and data model

ISO 19112:2019 describes spatial referencing by geographic identifiers, locations and location classes. The LocationS interface is a specialisation of the Location interface from ISO19112-2019. See Figure 6. In the next section the Period interface is introduced as the temporal equivalent of LocationS.

**Figure 6 — Context for LocationS**

6.3.1.2 Defining tables

a) Table 20 Elements of Spatial Location::LocationS

Table 20 — Elements of Spatial Location::LocationS

Name:	LocationS					
Definition:	Particular place or position. NOTE unlike a Location as specified in ISO 19112:2019, all LocationS are owned and defined by their ReferenceSystem and not by an independent authority.					
Stereotype:	Interface					
Inheritance from:	ZonePrimitive					
Abstract:	true					
Associations:	<i>Association with:</i>			<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	LocationS (feature type)			C	*	childOf
	LocationS (feature type)			C	*	parentOf
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	coordinateTuple	point within the extent of the spatial location		M	1	DirectPosition
	extent	spatial extent of the location	true	M	1	EX_Extent
	identifier	identifier of the spatial location		M	1	GeographicIdentifier
Constraints:	self.dimension > 0					

The following requirement applies:

Requirement 21: www.opengis.net/spec/DGGS/2.0/req/cc/spatial/location

The common classes for spatial location shall conform to the data model in Figure 6 and defining table in Table 20.

6.3.2 Temporal RS using Identifiers module

6.3.2.1 Context and data model

Semantically, the terms period and zone are defined as the temporal and spatio-temporal equivalents of a location. These are represented in the data model by the interfaces Period and Zone.

Referring to Figure 7 showing the spatial classes on the left and the temporal classes on the right, it is noted that Period is augmented by:

- PeriodIdentifier data-type as the temporal equivalent of GeographicIdentifier,
- Period interface as the temporal equivalent of LocationS, see Figure 6,
- PeriodClass interface as the temporal equivalent of LocationClass, and
- TemporalReferenceSystemusingPeriodIdentifiers interface as the temporal equivalent of SpatialReferenceusingGeographicIdentifiers.

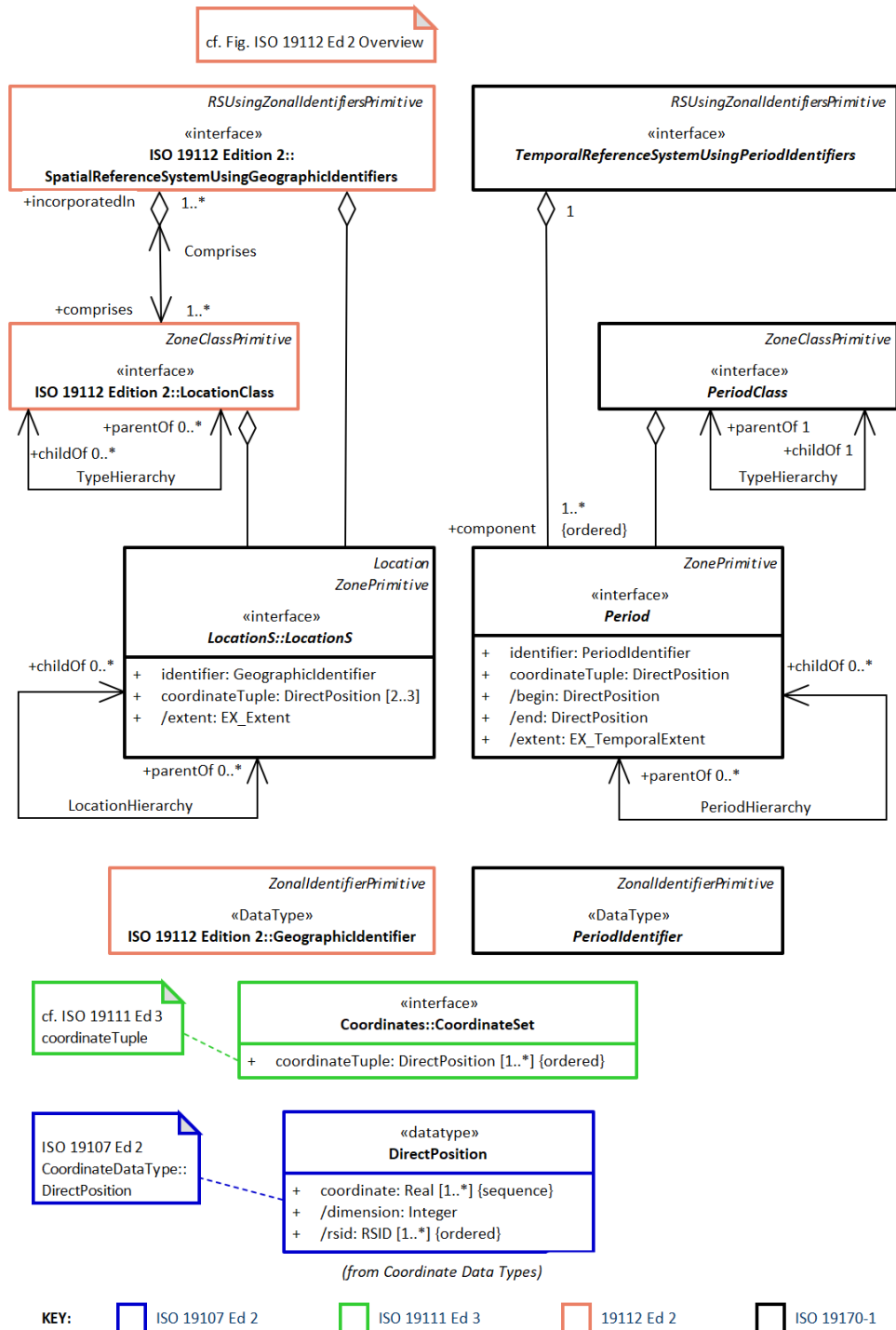


Figure 7 — Context for Temporal RS using Identifiers module

6.3.2.2 Defining tables

- Table 21 Elements of Temporal RS using Identifiers::Period
- Table 22 Elements of Temporal RS using Identifiers::PeriodClass
- Table 23 Elements of Temporal RS using Identifiers::PeriodIdentifier

- d) Table 24 Elements of Temporal RS using
Identifiers::TemporalReferenceSystemUsingPeriodIdentifiers

Table 21 — Elements of Temporal RS using Identifiers::Period

Name:	Period					
Definition:	Particular time span or era between two instants.					
Stereotype:	Interface					
Inheritance from:	ZonePrimitive					
Abstract:	true					
Associations:	<i>Association with:</i>			<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	Period (feature type)			C	*	childOf
	Period (feature type)			C	*	parentOf
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	begin	Instant at the beginning of the period.	true	M	1	DirectPosition
	coordinateTuple	Position within the extent of the period.		M	1	DirectPosition
	end	Instant at the end of the period.	true	M	1	DirectPosition
	extent	Temporal extent of the period.	true	M	1	EX_TemporalExtent
	identifier	Identifier of the period.		M	1	PeriodIdentifier (data type)
Constraints:	(none)					

Table 22 — Elements of Temporal RS using Identifiers::PeriodClass

Name:	PeriodClass				
Definition:	Categorization of Periods.				
Stereotype:	Interface				
Inheritance from:	ZoneClassPrimitive				
Abstract:	true				
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>	
	PeriodClass (feature type)	M	1	childOf	
	TemporalReferenceSystemUsingPeriodIdentifiers (feature type)	M	*	incorporatedIn	
	PeriodClass (feature type)	M	1	parentOf	
Public attributes:	(none)				
Constraints:	(none)				

Table 23 — Elements of Temporal RS using Identifiers::PeriodIdentifier

Name:	PeriodIdentifier				
Definition:	Temporal reference in the form of a label or code that identifies a period				
Stereotype:	DataType				
Inheritance from:	ZonalIdentifierPrimitive				
Abstract:	true				
Associations:	(none)				
Public attributes:	(none)				

Constraints:	(none)
---------------------	--------

Table 24 — Elements of Temporal RS using Identifiers::TemporalReferenceSystemUsingPeriodIdentifiers

Name:	TemporalReferenceSystemUsingPeriodIdentifiers			
Definition:	A temporal RS based on period identifiers.			
Stereotype:	Interface			
Inheritance from:	RSUsingZonalIdentifiersPrimitive			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	Period (feature type)	M	*	component
	PeriodClass (feature type)	M	*	comprises
Public attributes:	(none)			
Constraints:	(none)			

The following requirement applies:

Requirement 22: www.opengis.net/spec/DGGS/2.0/req/cc/temporal/rsupi

The common classes for reference systems using period identifiers shall conform to the data model in Figure 7 and defining tables in Table 21–Table 24.

6.3.3 Zonal RS using Identifiers module

6.3.3.1 Context and data model

Semantically zones are the spatio-temporal equivalent of periods and locations. Zones are represented in the data model by the interface Zone and along with it the following interfaces are also established.

- ZonalIdentifier,
- ZoneClass, and
- RSUsingZonalIdentifiers.

Referring to Figure 8, a ZonalIdentifier is either a zonal identifier primitive or a compound of two zonal identifier primitives, one spatial and one temporal.

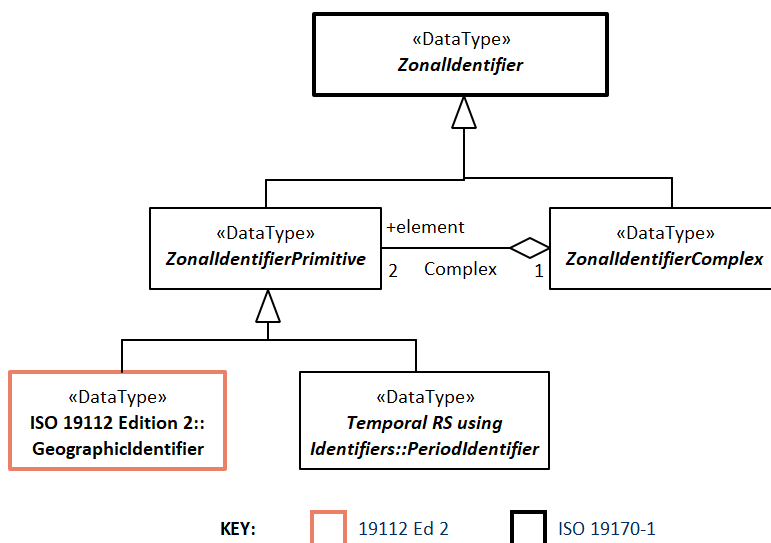


Figure 8 — Primitives of ZonalIdentifier

Referring to Figure 9, a Zone is either a zonal primitive or a compound of two zonal primitives, one spatial and one temporal.

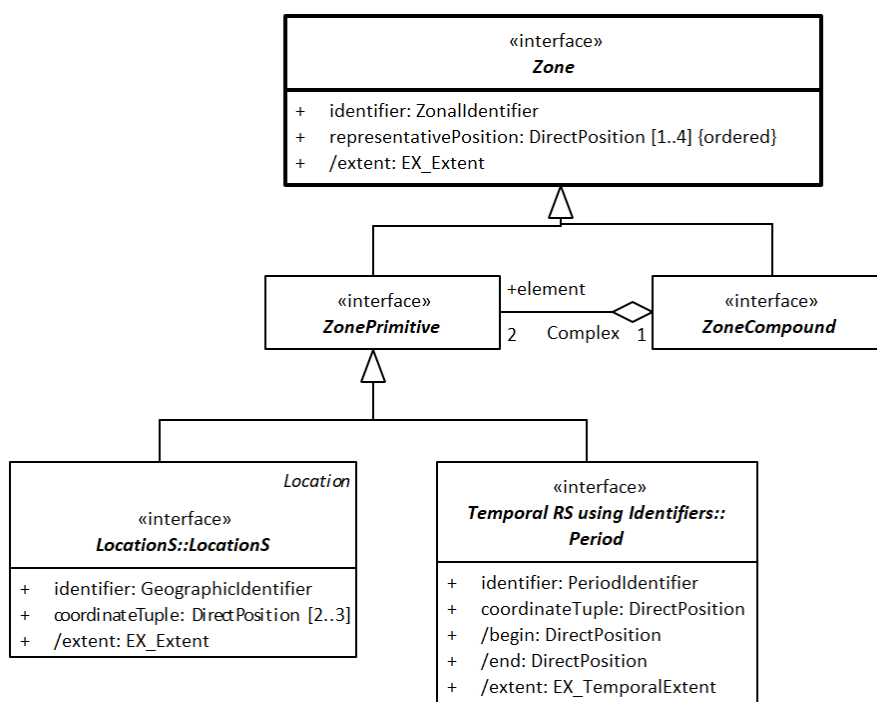


Figure 9 — Primitives of Zone

Referring to Figure 10, a ZoneClass is either a zonal class primitive or a compound of two zonal class primitives, one spatial and one temporal.

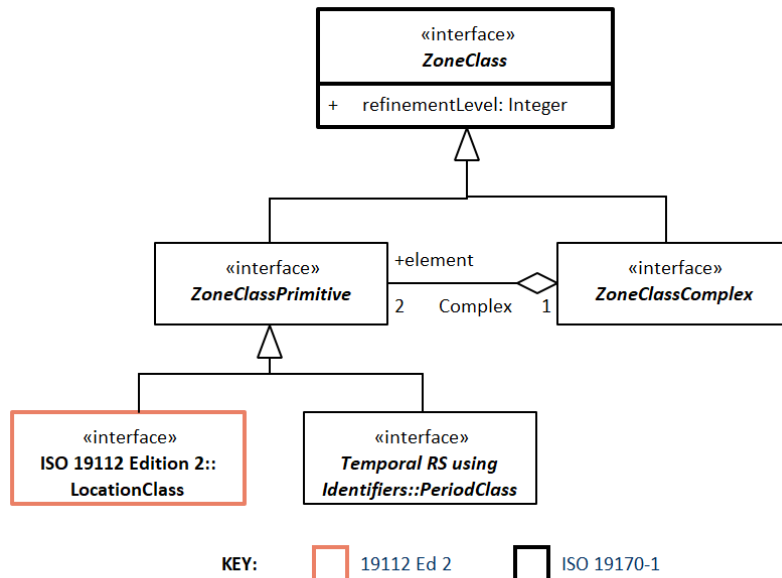


Figure 10 — Primitives of ZoneClass

Referring to Figure 11, an RSUsingZonalIdentifiers is either a zonal RS using identifiers primitive or a compound of two of its primitives, one spatial and one temporal.

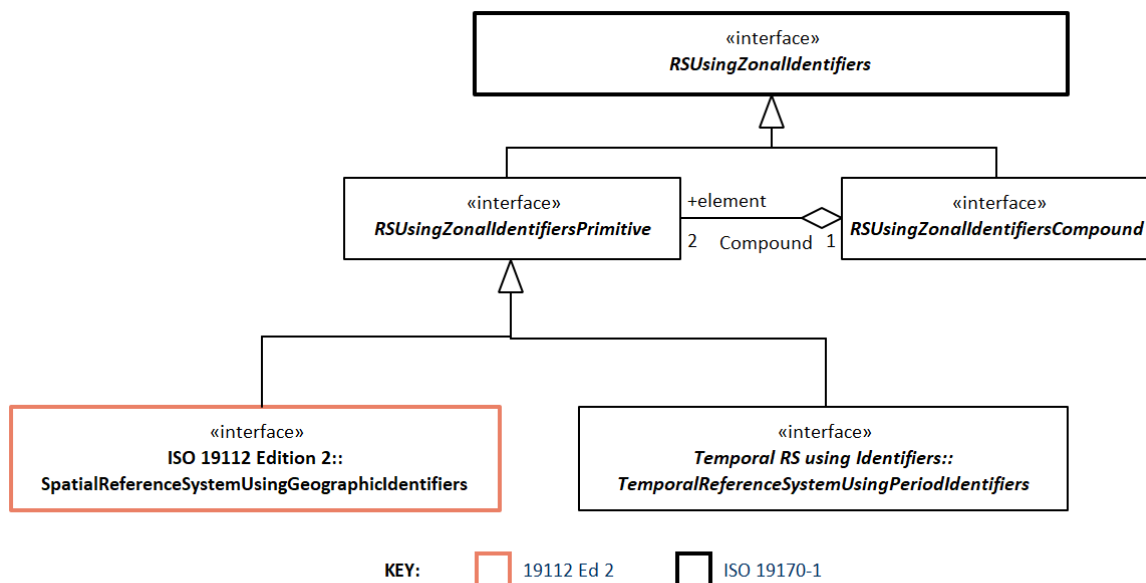


Figure 11 — Primitives of RSUsingZonalIdentifiers

Referring to Figure 12, Zone, ZonalIdentifier and ZoneClass come together to form RSUsingZonalIdentifiers.

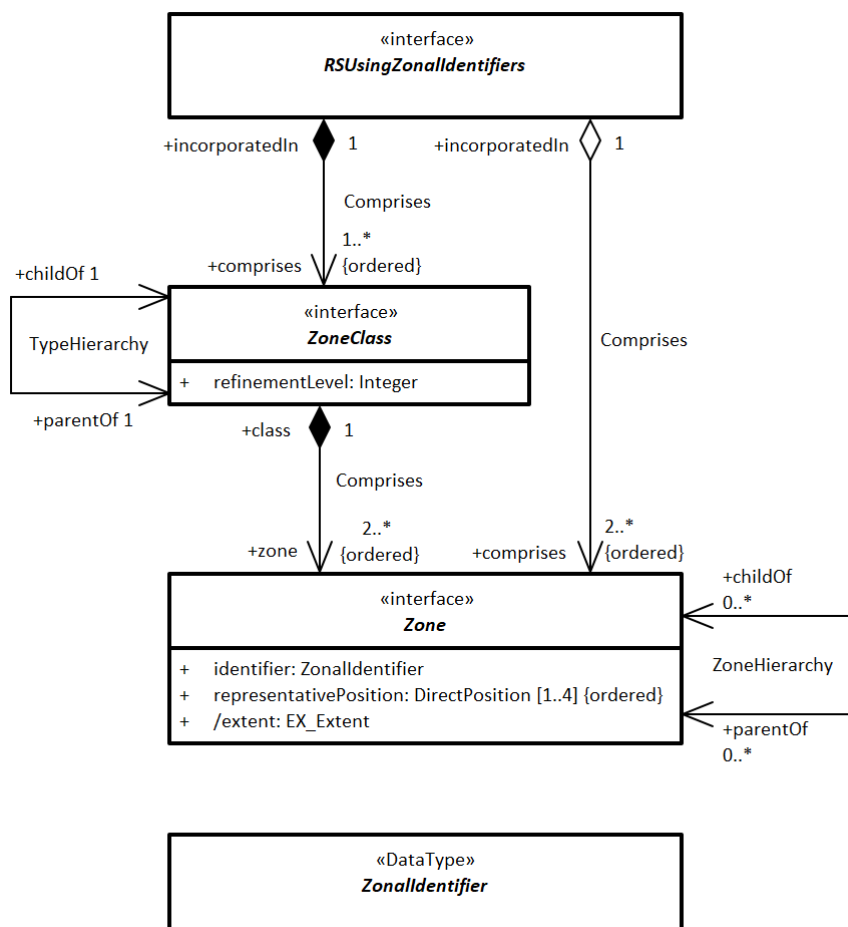


Figure 12 — Components of RSUsingZonalIdentifiers

6.3.3.2 Defining tables

- Table 25 Elements of Zonal RS using Identifiers::RSUsingZonalIdentifiers
- Table 26 Elements of Zonal RS using Identifiers::RSUsingZonalIdentifiersCompound
- Table 27 Elements of Zonal RS using Identifiers::RSUsingZonalIdentifiersPrimitive
- Table 28 Elements of Zonal RS using Identifiers::ZonalIdentifier
- Table 29 Elements of Zonal RS using Identifiers::ZonalIdentifierComplex
- Table 30 Elements of Zonal RS using Identifiers::ZonalIdentifierPrimitive
- Table 31 Elements of Zonal RS using Identifiers::Zone
- Table 32 Elements of Zonal RS using Identifiers::ZoneClass
- Table 33 Elements of Zonal RS using Identifiers::ZoneClassComplex
- Table 34 Elements of Zonal RS using Identifiers::ZoneClassPrimitive
- Table 35 Elements of Zonal RS using Identifiers::ZoneCompound
- Table 36 Elements of Zonal RS using Identifiers::ZonePrimitive

Table 25 — Elements of Zonal RS using Identifiers::RSUsingZonalIdentifiers

Name:	RSUsingZonalIdentifiers			
Definition:	A reference system using zonal identifiers is either a reference system using zonal identifiers primitive or a compound of one spatial reference system using zonal identifiers and one temporal reference system using period identifiers primitives.			
Stereotype:	Interface			
Generalisation of:	RSUsingZonalIdentifiersCompound, RSUsingZonalIdentifiersPrimitive			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	Zone (feature type)	M	*	comprises
		M	*	comprises
Public attributes:	(none)			
Constraints:	(none)			

Table 26 — Elements of Zonal RS using Identifiers::RSUsingZonalIdentifiersCompound

Name:	RSUsingZonalIdentifiersCompound			
Definition:	A reference system using zonal identifiers compound is a compound of one spatial reference system using zonal identifiers and one temporal reference system using zonal identifiers primitives.			
Stereotype:	Interface			
Inheritance from:	RSUsingZonalIdentifiers			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	RSUsingZonalIdentifiersPrimitive (feature type)	M	2	element
Public attributes:	(none)			
Constraints:	(none)			

Table 27 — Elements of Zonal RS using Identifiers::RSUsingZonalIdentifiersPrimitive

Name:	RSUsingZonalIdentifiersPrimitive			
Definition:	A reference system using zonal identifiers primitive is either a spatial reference system using geographic identifiers or a temporal reference system using period identifiers.			
Stereotype:	Interface			
Inheritance from:	RSUsingZonalIdentifiers			
Abstract:	true			
Associations:	(none)			
Public attributes:	(none)			
Constraints:	(none)			

Table 28 — Elements of Zonal RS using Identifiers::ZonalIdentifier

Name:	ZonalIdentifier			
Definition:	Spatial, temporal or spatio-temporal reference in the form of a label or code that identifies a zone.			
Stereotype:	DataType			
Generalization of:	ZonalIdentifierComplex, ZonalIdentifierPrimitive			
Abstract:	true			
Associations:	(none)			

Public attributes:	(none)
Constraints:	(none)

Table 29 — Elements of Zonal RS using Identifiers::ZonalIdentifierComplex

Name:	ZonalIdentifierComplex			
Definition:	Zonal identifier complex is a complex of two zonal identifier primitives, one geographic identifier and one period identifier.			
Stereotype:	DataType			
Inheritance from:	ZonalIdentifier			
Abstract:	true			
Associations:	<i>Association with:</i> ZonalIdentifierPrimitive (feature type)	<i>Obligation</i> M	<i>Maximum occurrence</i> 2	<i>Provides:</i> element
Public attributes:	(none)			
Constraints:	(none)			

Table 30 — Elements of Zonal RS using Identifiers::ZonalIdentifierPrimitive

Name:	ZonalIdentifierPrimitive
Definition:	A zonal identifier primitive is either a geographic identifier or a period identifier.
Stereotype:	DataType
Inheritance from:	ZonalIdentifier
Abstract:	true
Associations:	(none)
Public attributes:	(none)
Constraints:	(none)

Table 31 — Elements of Zonal RS using Identifiers::Zone

Name:	Zone					
Definition:	A zone is a particular spatial, temporal or spatio-temporal place.					
Stereotype:	Interface					
Generalization of:	ZoneCompound, ZonePrimitive					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	extent		true	M	1	EX_Extent
	identifier	name or label for the Zone		M	1	ZonalIdentifier (data type)
	representativePosition	interior position the Zone		M	4	DirectPosition
Constraints:	(none)					

Table 32 — Elements of Zonal RS using Identifiers::ZoneClass

Name:	ZoneClass			
Definition:	Categorisation of zones.			
Stereotype:	Interface			
Generalization of:	ZoneClassComplex, ZoneClassPrimitive			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>

				M	*	zone
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	refinementLevel	refinement level used to define the zone class		M	1	Integer
Constraints:	(none)					

Table 33 — Elements of Zonal RS using Identifiers::ZoneClassComplex

Name:	ZoneClassComplex			
Definition:	A zone class complex is a complex of two zone class primitives, one location class and one period class.			
Stereotype:	Interface			
Inheritance from:	ZoneClass			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	ZoneClassPrimitive (feature type)	M	2	element
Public attributes:	(none)			
Constraints:	(none)			

Table 34 — Elements of Zonal RS using Identifiers::ZoneClassPrimitive

Name:	ZoneClassPrimitive					
Definition:	A zone class primitive is either a location class or a period class.					
Stereotype:	Interface					
Inheritance from:	ZoneClass					
Abstract:	true					
Associations:	(none)					
Public attributes:	(none)					
Constraints:	(none)					

Table 35 — Elements of Zonal RS using Identifiers::ZoneCompound

Name:	ZoneCompound			
Definition:	A zone compound is a compound of two zone primitives, one spatial location and one temporal period.			
Stereotype:	Interface			
Inheritance from:	Zone			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	ZonePrimitive (feature type)	M	2	element
Public attributes:	(none)			
Constraints:	(none)			

Table 36 — Elements of Zonal RS using Identifiers::ZonePrimitive

Name:	ZonePrimitive					
Definition:	A zone primitive is either a spatial location or a temporal period.					
Stereotype:	Interface					
Inheritance from:	Zone					
Abstract:	true					
Associations:	(none)					
Public attributes:	(none)					

Constraints:	(none)
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The following requirement applies:

Requirement 23: www.opengis.net/spec/DGGS/2.0/req/cc/zone/rsuzi

The common classes for reference systems using zonal identifiers shall conform to the data model in Figure 8–Figure 12 and defining tables in Table 25–Table 36.

7 DGGS Core package

7.1 DGGS Core package conformance classes

This clause specifies the DGGS Core RS conformance class and the DGGS Core Functions conformance class. These cover:

- a) DGGS Core RS — comprising parent global geometry, base CRS, and RS using zonal identifiers with structured geometry;
- b) DGGS Core Functions — comprising quantization, topological query, and interoperability.

7.2 Core RS using Zonal Identifiers with Structured Geometry module

7.2.1 Core RS data model and base CRS

The DGGS Core RS shown in Figure 13 is a RS using zonal identifiers with structured geometry for a globe. It is defined by the attributes of the DGG_ReferenceSystem interface Table 37 and its metadata. In the context of the DGGS, and particularly in the DGGS Core, the term globe is used in its most general sense to represent a mathematical model of any planetary body and, depending on need, potentially its surroundings out to the orbit of a planet's outer moons, and for spatio-temporal DGGS over a defined time span. The spatio-temporal extent of the entire globe is referred to as the domain of the DGGS. The DGGS Core itself is dimension agnostic.

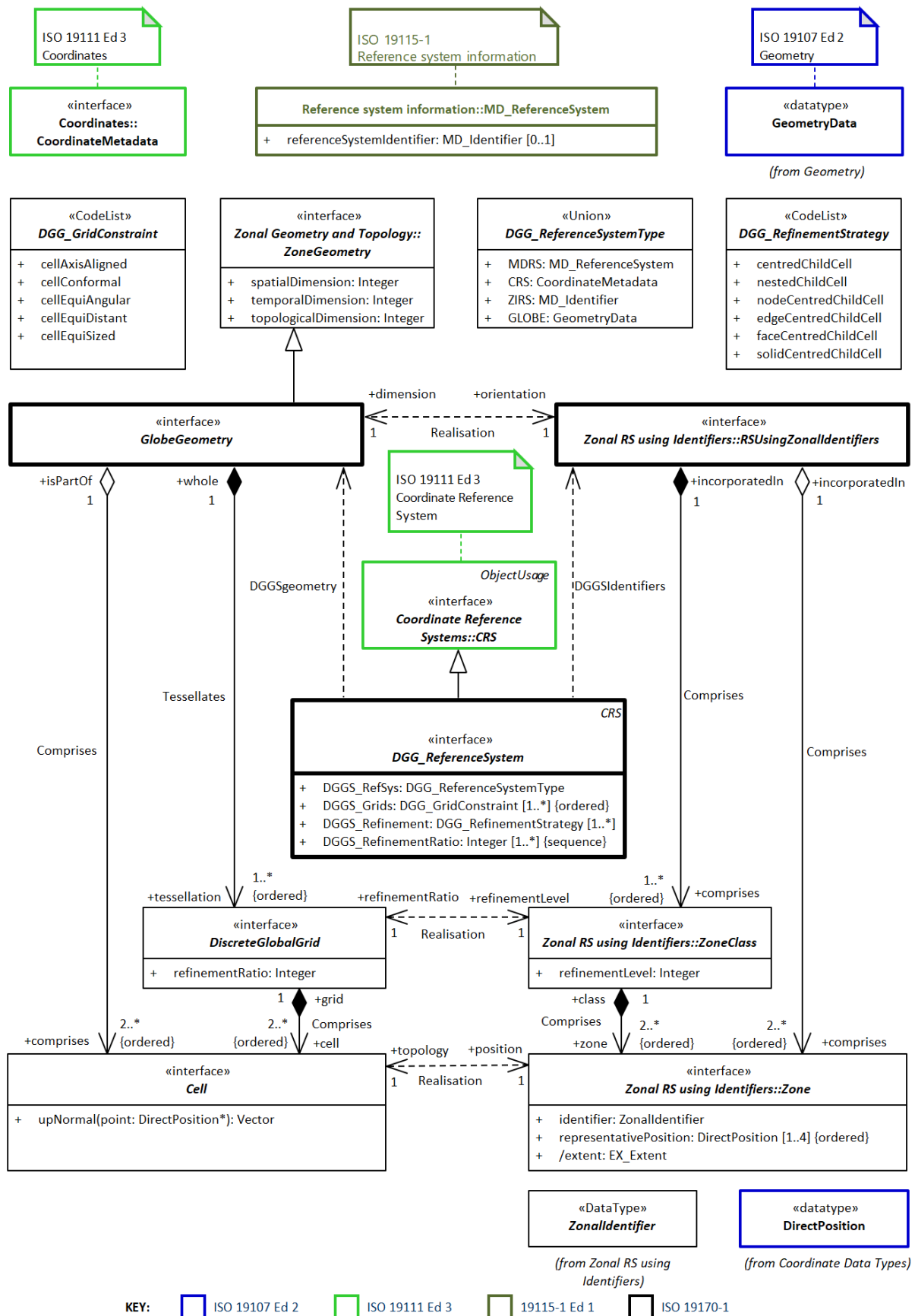


Figure 13 —Core RS using Zonal Identifiers with Structured Geometry module

The DGGs Core RS model in Figure 13 describes a hierarchy of paired elements — at each tier of the hierarchy a geometry element, shown on the left of the figure is paired with the equivalent zonal element, shown on the right of the figure.

At the root of the hierarchy, the globe's reference model and base CRS for the DGGs are defined. A single parent geometry (GlobeGeometry) is defined to coincide with the globe's reference model. The parent geometry's dimensionality governs the dimensionality of the DGGs (See 7.2.3). The parent global geometry is paired with a RS using zonal identifiers (RSUsingZonalIdentifiers).

A sequence of discrete global grids (DiscreteGlobalGrids), each paired with a ZoneClass, define the lower levels of the hierarchy.

Each DiscreteGlobalGrid is made up of Cells. Each Cell occupies a region of space-time (a Zone). The Zones corresponding to Cells in a DiscreteGlobalGrid all belong to the corresponding ZoneClass (See 7.2.5).

Cells provide zones with geometry and topology, and zones provide cells with names in the form of zonal identifiers and representative positions in the base CRS in the form of direct positions (See 7.2.4).

Each cell is the child of one or more parent cells in the parent discrete global grid in the level above in the hierarchy. The cells of a discrete global grid are topologically related to the cells in the parent(s) by the collection of refinement strategies defined in DGG_ReferenceSystem(DGGs_Refinement).

Each cell's geometry, orientation and size is governed by the constraint defined in DGG_ReferenceSystem(DGGs_Grids) and by the sequence of refinement ratios defined in DGG_ReferenceSystem(DGGs_RefinementRatio). If a sequence of refinementRatio is defined, the values are applied to each level in the hierarchy in a recurring sequence starting at the top with the first refinementRatio in the sequence and working down through the levels in order.

7.2.2 Defining tables

- a) Table 37 — Elements of Core RS using Zonal Identifiers with Structured Geometry::Cell
- b) Table 38 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DGG_ReferenceSystem
- c) Table 39 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DGG_ReferenceSystemType
- d) Table 40 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DiscreteGlobalGrid
- e) Table 41 — Elements of Core RS using Zonal Identifiers with Structured Geometry::GlobeGeometry
- f) Table 42 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DGG_GridConstraint
- g) Table 43 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DGG_RefinementStrategy

Table 37 — Elements of Core RS using Zonal Identifiers with Structured Geometry::Cell

Name:	Cell
Definition:	Reference system unit of geometry associated with a Zone. As part of GlobeGeometry, it has the same spatial, temporal and topological dimensionality as GlobeGeometry.
Stereotype:	Interface
Abstract:	true
Associations:	(none)

Public attributes:	(none)
Constraints:	(none)

Table 38 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DGG_ReferenceSystem

Name:	DGG_ReferenceSystem					
Definition:	Defining characteristics of a Reference system using zonal identifiers with structured geometry.					
Stereotype:	Interface					
Abstract:	true					
Associations :	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	DGGS_Grids	List of characteristics that constrain the grid cells in this DGGS in decreasing order of priority.		M	*	DGG_GridConstraint (code list)
	DGGS_Refinement	List of topological relationships between parent and child cells in this DGGS.		M	*	DGG_RefinementStrategy (code list)
	DGGS_RefinementRatio	List of refinement ratios of parent cell size to child cell size, in the order that they are used in constructing child cells in the DGGS. If the list is shorter than the number of discrete global grids in the DGGS, then it is used as a recurring sequence.		M	*	Integer
	DGGS_RefSys	Reference system metadata.		M	1	DGG_ReferenceSystemType (union data type)
Constraints:	(none)					

Table 39 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DGG_ReferenceSystemType

Name:	DGG_ReferenceSystemType					
Definition:	Defining metadata elements of the base CRS for this DGGS					
Stereotype:	Union					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	CRS	Metadata required to reference coordinates.		M	1	CoordinateMetadata
	GLOBE	GeometryData for the chosen GlobeGeometry that specifies geometry, spatial, temporal and topological dimensionality and domain of the globe for this DGGS.		M	1	Geometry::GeometryData
	MDRS	RS information describing this whole DGGS.		M	1	MD_ReferenceSystem
	ZIRS	Identifier for the RSUsingZonalIdentifiers used by this DGGS.		M	1	MD_Identifier
Constraints:	(none)					

Table 40 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DiscreteGlobalGrid

Name:	DiscreteGlobalGrid					
Definition:	Set of Cells at the same refinement level					
Stereotype:	Interface					
Abstract:	true					
Associations:	<i>Association with:</i>			<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
				M	*	cell
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	refinementRatio	Ratio of the number of cells in the parent DiscreteGlobalGrid to the number in this DiscreteGlobalGrid.		M	1	Integer
Constraints:	(none)					

Table 41 — Elements of Core RS using Zonal Identifiers with Structured Geometry::GlobeGeometry

Name:	GlobeGeometry			
Definition:	Parent geometry specifying the geometry, dimensionality and domain of the globe for this DGGs.			
Stereotype:	Interface			
Inheritance from:	ZoneGeometry			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	Cell (feature type)	M	*	comprises
		M	*	tessellation
Public attributes:	(none)			
Constraints:	(none)			

Table 42 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DGG_GridConstraint

Name:	DGG_GridConstraint	
Definition:	CodeList for constraints that are used to define different categories of DGGs. Each constraint is a constraint on the shape, size, or orientation of cells in a DiscreteGlobalGrid.	
Stereotype:	CodeList	
Abstract:	true	
Associations:	(none)	
Values:	<i>Name</i>	<i>Definition</i>
	cellAxisAligned	Cell edges are parallel to the base CRS's coordinate system axes.
	cellConformal	Variation in shape between all the cells in each DiscreteGlobalGrid is minimized.
	cellEquiAngular	Variation in bearing from one cell's representative position to the next neighbouring cell's representative positions in each DiscreteGlobalGrid is minimized.
	cellEquiDistant	Variation in distance from a cell's representative position to all of it's neighbouring cell's representative positions in each DiscreteGlobalGrid is minimized.
	cellEquiSized	Variation in interior size between all cells in each DiscreteGlobalGrid is minimized.

Table 43 — Elements of Core RS using Zonal Identifiers with Structured Geometry::DGG_RefinementStrategy

Name:	DGG_RefinementStrategy	
Definition:	CodeList for strategies that are used to define different categories of DGGs. Each strategy defines the topological relationship of one or more elements of cell geometry belonging to a child cell with one or more elements of geometry of its parent cell.	
Stereotype:	CodeList	
Abstract:	true	
Associations:	(none)	
Values:	<i>Name</i>	<i>Definition</i>
	centredChildCell	parent $\Leftarrow$ zone.representativePosition() = child $\Leftarrow$ zone.representativePosition() for one child.
	nestedChildCell	parent.boundary = <<set of all parent.child>>.boundary.
	nodeCentredChildCell	Each parent cell has a child $\Leftarrow$ zone.representativePosition coincident with each of the parent's <i>nodes</i> (zero-dimensional topological boundary element).
	edgeCentredChildCell	Each parent cell of dimension greater than 1 has a child cell for which the cell $\Leftarrow$ zone.representativePosition lies on each of the parent's <i>edges</i> (one-dimensional topological boundary element).
	faceCentredChildCell	Each parent cell of dimension greater than 2 has a child cell for which the cell $\Leftarrow$ zone.representativePosition lies on each of the parent's <i>faces</i> (two-dimensional topological boundary element).
	solidCentredChildCell	Each parent cell of dimension greater than 3 has a child cell for which the cell $\Leftarrow$ zone.representativePosition lies on each of the parent's <i>solids</i> (three-dimensional topological boundary element).

The following requirements apply:

Requirement 24: www.opengis.net/spec/DGGS/2.0/req/core/rs/harmonised_model

The data model for a DGGS RS and its element definitions shall comply with the DGGS Core RS data model in Figure 13 and definitions in Table 37- Table 43.

Requirement 25: www.opengis.net/spec/DGGS/2.0/req/core/rs/crs

A DGGS RS shall define a CRS, and comply with requirements for provision of coordinate epoch as specified for MD_ReferenceSystem.

7.2.3 Global domain

The domain of the DGGS shall be defined as the entire globe, with cells that “*exhaustively cover the globe without overlapping or underlapping*” (Goodchild^[28]). Applying these criteria to the cells in each discrete global grid, there shall be no gaps between cells and no positions that are covered by more than one cell.

Each cell inherits its dimensionality from the choice of geometry for the GlobalGeometry class, so a reference system that specifies a geometry and domain as the globe's surface will have two-dimensional cells on the surface of the globe, and one that specifies a geometry and domain as a globe's volume will have three-dimensional cells filling the globe. A reference system that specifies a linear geometry and domain, for instance for time, will result in one-dimensional cells.

The following requirements apply:

Requirement 26: www.opengis.net/spec/DGGS/2.0/req/core/rs/global_domain

DGGS RS global domain — the reference system shall specify a global domain, and its spatial, temporal and topological dimensionality.

Requirement 27: www.opengis.net/spec/DGGS/2.0/req/core/rs/global_domain/complete

DGGS RS domain completeness — the level zero discrete global grid shall cover the entire global domain.

Requirement 28: www.opengis.net/spec/DGGS/2.0/req/core/rs/global_domain/unique

DGGS RS location uniqueness — every location in the domain of the reference system shall be in exactly one cell of the level zero discrete global grid.

7.2.4 Cells and zones**7.2.4.1 Cell simple geometry**

Semantically, the terms cell and zone refer to different characteristics of the same region of space-time. Cells in a DGGS shall be geometrically simple. Simple geometries have the following properties:

- a) they do not self-intersect;
- b) they are topologically the same as a circle, or the circle's equivalent in the dimension of the cell, e.g. to a sphere in three-dimensions; and
- c) they enclose a region which is always measurable using a metric of the same dimensionality as the cell.

The following requirement applies:

Requirement 29: www.opengis.net/spec/DGGS/2.0/req/core/rs/cell/simple

For each successive level of grid refinement, a DGGS specification shall define cells with simple geometry.

7.2.4.2 Cell position

Each cell's zone has a fixed representative position in the space of the base CRS, recorded as a direct position.

The following requirement applies:

Requirement 30: www.opengis.net/spec/DGGS/2.0/req/core/rs/cell/direct_position

All zones in each discrete global grid shall be assigned a direct position that is within the zone's boundary.

7.2.4.3 Cell address

Each cell's zone shall be assigned a unique address in the form of a zonal identifier. The value assigned to each address shall be structured on one or more of these four general indexing methods: hierarchy-based, space-filling curve based, coordinate^[35] and encoded address schemas (such as those used for IP addresses^[38]).

The following requirement applies:

Requirement 31: www.opengis.net/spec/DGGS/2.0/req/core/rs/cell/address

All zones in all discrete global grids shall have a globally unique zonal identifier (or cell index) that provides a spatio-temporal reference.

7.2.5 Discrete global grid and its sequence

Cells at the same level in the tessellation hierarchy are aggregated into discrete global grids. The hierarchy of discrete global grids is an ordered sequence, typically also of decreasing cell size, representing the lowest resolution to higher resolutions. The discrete sequence of grids forms a multi-resolution grid hierarchy that is the basis for the DGGs RS.

The following requirements apply:

Requirement 32: www.opengis.net/spec/DGGs/2.0/req/core/rs/discrete_global_grid

A DGGs RS shall define discrete global grids as aggregations of all the cells at the same level in the hierarchy.

Requirement 33: www.opengis.net/spec/DGGs/2.0/req/core/rs/discrete_global_grid/sequence

A DGGs RS shall sort its hierarchy of discrete global grids in order of increasing refinement level.

7.3 DGGs Core functions

7.3.1 Core Quantization Functions module

A DGGs is defined based on the geometry of the globe in a data agnostic manner. Therefore, a DGGs specification shall define quantization methods for assigning data to cells so that the data is accessible for future use. Different quantization strategies may be used for sampling content into cells. For example, a single DGGs may be used as a data structure for integrating multiple datasets of different types (e.g. vector and raster datasets)^[41] and in different ways (e.g. DGGs cells as data tiles, or one raster pixel per DGGs cell or DGGs cell indices as vector coordinate-pairs). This abstract specification makes use of the concepts defined by ISO 19156 to facilitate the association of observations/spatial data to a DGGs cell(s). Some DGGs/polyhedron choices are more efficient for sampling than others (e.g. DGGs based on an icosahedron).

Multiple observation contexts are recognized for quantization, each corresponding to a distinct role for DGGs cells to play. In any particular DGGs specification, one or more (and potentially all) roles may be described for either internal or external use to support interoperability, as follows:

- a) **asDataTiles:** In data tile quantization, spatial feature/observations (e.g. point clouds, images, vectors, etc.) are aggregated and clipped to cell boundaries and stored in tiles without any changes made to the feature type parameters. The cells of the DGGs provide a multi- or single-resolution tiling schema with the cell index used as the identifier in the tile naming convention. In the context of “Big Data Analytics”, ‘asDataTile’ support will likely be the most efficient type of granularity for job submission on HPC/HPD or Cloud ICT infrastructure, particularly for dominantly embarrassingly parallel analyses. It is also likely to be the most efficient granularity for many data transfer requests.
- b) **asDataCells:** In data cell quantization, the spatial features/observations (e.g. point clouds, images, vectors, etc.) are sampled to each DGGs cell by assignment of data value(s) using the cell’s geometry to govern the quantization operation.
- c) **asCoordinates:** In coordinate quantization, each coordinate tuple from the spatial feature/observation is converted to a cell index of an appropriate level of precision. The cell data package will include appropriate vector topology to preserve the structure of the spatial feature in the context of the DGGs.
- d) **asTags:** In tag quantization, cell index values are “tagged” to data objects in a similar fashion to social media records. The refinement level of the cell index is indicative of the precision with which the location of a spatial feature/observation and/or its spatial extent are known. This can be

thought of as a convex hull with the same geometry of the DGGS cell surrounding the objects to be assigned to that cell.

- e) **asGraphicCells:** In graphic cell quantization, data is rendered to cells, and refinement levels are leveraged to support corresponding levels of detail or zoom levels.
- f) **asGraphicTiles:** In graphic tile quantization, graphic cells are tiled, and often cached for delivery to a display system. As with data tiles, the cell index is used as the identifier in the tile naming convention.

The extent of the data assigned at any time to a particular DGGS implementation, defines the DGGS's extent. The extent is likely to vary over the DGGS's lifecycle as the extent of data assigned to it changes. The domain of the DGGS, is however, always fixed and always defined over the entire surface model of the DGGS's globe.

Figure 14 shows the key elements required to perform data quantization operations in a DGGS specification.

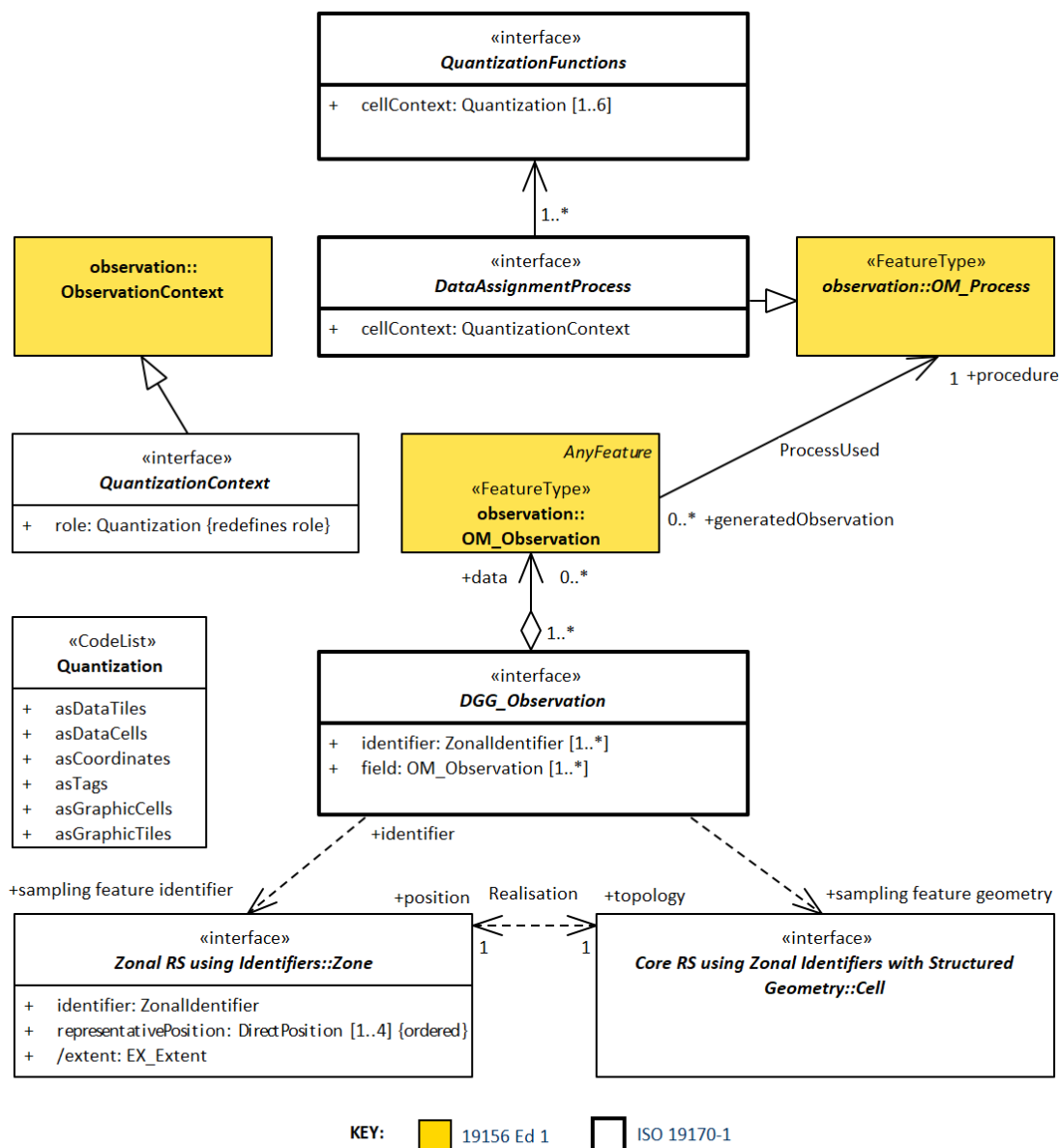


Figure 14 — Components of Core Quantization Functions module

7.3.2 Defining tables

- Table 44 — Elements of Core Quantization Functions::DataAssignmentProcess
- Table 45 — Elements of Core Quantization Functions::DGG_Observation
- Table 46 — Elements of Core Quantization Functions::QuantizationContext
- Table 47 — Elements of Core Quantization Functions::QuantizationFunctions
- Table 48 — Elements of Core Quantization Functions::Quantization

Table 44 — Elements of Core Quantization Functions::DataAssignmentProcess

Name:	DataAssignmentProcess					
Definition:	The class DataAssignmentProcess is a generalization of OM_Process, which represents a feature type. DataAssignmentProcess is abstract, and has no attributes, operations or associations. It serves as the base class for DataAssignment processes. The purpose of a data assignment process is to generate an assignment result. An instance of DataAssignmentProcess is often a data import function to import data from a pre-existing spatial dataset, but as in OM_Process “it may also be an instrument or sensor, a human observer, a simulator, or a process or algorithm applied to more primitive results used as inputs”. [Source ISO 19156:2011, clause 7.2.3]					
Stereotype:	Interface					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	cellContext	Roll that cell provides in this DataAssignmentProcess.		M	1	QuantizationContext
Constraints:	(none)					

Table 45 — Elements of Core Quantization Functions::DGG_Observation

Name:	DGG_Observation					
Definition:	DGG_Observation is an abstract class holding ZonalIdentifier, OM_Observation tuples. In the context of Quantization, DGG_Observation holds records of Observations made with DataAssignmentProcess in assigning values to cells.					
Stereotype:	Interface					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	field	Values that were observed.		M	*	OM_Observation
	identifier	Cells that were observed.		M	*	ZonalIdentifier (data type)
Constraints:	(none)					

Table 46 — Elements of Core Quantization Functions::QuantizationContext

Name:	QuantizationContext					
Definition:	ObservationContext for this DataAssignmentProcess.					
Stereotype:	Interface					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	role	Defines the role or roles that cells play in the quantization.		M	1	Quantization (code list)
Constraints:	(none)					

Table 47 — Elements of Core Quantization Functions::QuantizationFunctions

Name:	QuantizationFunctions					
Definition:	Process for quantizing external data by using a cell's geometry to sample external data and assign the results to zonal identifiers. The quantization code list identifies different potential roles for the cell geometry in the quantization process.					
Stereotype:	Interface					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	cellContext	List of roles that cell geometry is to be used in associated DataAssignmentProcesses.		M	6	Quantization (code list)
Constraints:	(none)					

Table 48 — Elements of Core Quantization Functions::Quantization

Name:	Quantization	
Definition:	CodeList for roles that cell geometries may play in a DataAssignmentProcess.	
Stereotype:	CodeList	
Abstract:	true	
Associations:	(none)	
Values:	<i>Name</i>	<i>Definition</i>
	asDataTiles	Zone assigned features clipped to the boundary of the zone's cell. NOTE Features are clipped to the cell boundary and stored as a feature tile. NOTE The zone's zonal identifier may be used in the naming convention for data tiles.
	asDataCells	Zone assigned a data value, either resampled or remapped, from a feature based on the geometry of the cell.
	asCoordinates	Each coordinate tuple in a vector feature's geometry data is replaced by a zonal identifier. The size of zone is chosen to represent the uncertainty in the knowledge of the position represented by the coordinate tuple.
	asTags	Minimal set of zonal identifiers applied to an object. NOTE The zone operates in this context as a minimum bounding container (similar to a minimum bounding rectangle in 2D) where the boundary of the zone wholly encloses a set of features assigned to that zone. NOTE The refinement level of a zone index used to tag a feature (or set of features) provides an indication of the level of precision and/or the spatial extents of the feature.
	asGraphicCells	Zone assigned the color of a pixel in a map image ready for delivery to a map display system, with the color representing an attribute value, either sampled or mapped, from a feature. NOTE Refinement levels may be aligned with zoom levels or scales in a map display system.
	asGraphicTiles	Tiling scheme used for a map display system using cells to define the tile boundaries. NOTE Graphic tiles may be cached or stored and sent to the display system as a map tile.

The following requirement applies:

Requirement 34:

www.opengis.net/spec/DGGS/2.0/req/core/functions/quantization

A DGGS specification shall define quantization operations for assigning data from external sources to DGGS cells that conform to the data model in Figure 14 and definitions in tables Table 44–Table 48.

7.3.3 Core Topological Query Functions module

7.3.3.1 Overview of topological query functions

The Topological Query Functions module implements the DE9IM^[13] functionality defined in ISO 19107:2019 Geometry::Query2D and Geometry::Query3D for zonal topology. This is achieved through a single interface called ZoneQuery (Figure 16, Table 49). By default, ZoneQuery operates at the dimensionality of the DGGS's zones. Changes in dimensionality are controlled with an optional parameter *projectTo* that constrains ZoneQuery to a specified reference direction, surface or volume.

Two additional operations are provided that are based on the temporal concept of relative position. These are called *relatePosition* and *relativePosition*. These are generalized for use on any single reference direction specified by *projectTo*, not just the temporal direction.

Six additional operations are provided in ZoneQuery that leverage the ZoneClass hierarchy. These are called *parent*, *child* and *sibling* and *parentOf*, *childOf* and *siblingOf*.

ZoneQuery operations are defined in Figure 16 and 7.3.4. The following parameters are shared by many of the operations as specified in Table 49:

<i>another</i>	type ZonalIdentifier, mandatory. Specifies the target region for the query. In zonal query a zone's identifier provides sufficient description of its topology. ZonalIdentifier therefore takes the place of the geometry data used in Query2D and Query3D for both the source and the target.
<i>inheritID</i>	type Boolean, optional, default $\Leftarrow$ <i>False</i> When <i>inheritID</i> has a value of <i>True</i>, the result <<set>> only contains cells for which the IDs have shared inheritance, and a value of <i>False</i> indicates that inheritance is ignored.
<i>projectTo</i>	type directPosition[4], optional, default $\Leftarrow$ (0,0,0,1) for <i>relatePosition</i> and <i>relativePosition</i>, otherwise (1,1,1,1) <i>projectTo</i> specifies an optional reference direction, surface or volume for an operation. Allowed values for each direction are 0 and 1, and spatial directions may also have a value of <i>n</i>. <i>projectTo</i> defines a vector whose starting point is inferred as the point with each <i>projectTo</i> direction whose value is 1 set to 0. It takes one of three forms. In its one-dimensional form for specifying a reference direction, one direction has a value of 1. For example (0,0,0,1) projects to the temporal axis, and (0,0,1,0) projects to the vertical axis. In its two-dimensional form for specifying a reference surface, two directions have a value of 1. For example a surface at height <i>n</i> is specified by a <i>projectTo</i> value of (1,1,<i>n</i>,0) representing the vector [(0,0,<i>n</i>,0), (1,1,<i>n</i>,0)]. In its three-dimensional form for specifying a reference volume, three directions have a value of 1. For example (1,1,1,0) projects to a spatial volume without reference to time, and (1,1,<i>n</i>,1) projects to a surface spanning all time at height <i>n</i>. Only the one-dimensional form is supported by <i>relativePosition</i> and <i>relatePosition</i>. While this construct could be used to implement more complex spatio-temporal queries, that isn't the intent of Query2D, and isn't specified for ZoneQuery either.
<i>rangeRefine</i>	type refinementLevelRange, optional, default $\Leftarrow$ [min(source.refinementLevel, target.refinementLevel) : max(source.refinementLevel, target.refinementLevel)]. Specifies the range of refinement levels to include in the return <<set>>. The lower and upper bounds in the refinementLevelRange datatype are both included in the range.

levels type Integer, optional, default $\Leftarrow 1$
Levels indicates the relative number of levels in the hierarchy to be traversed in assembling the result <<set>> Figure 15 illustrates the parent, child and sibling suite of functions through examples.

7.3.3.2 Summary of operations in ZoneQuery

The following operations have the same topological meaning as their equivalent operations in ISO 19107 Geometry::Query2D and Geometry::Query3D: distance, contains, crosses, disjoint, equals, intersects, overlaps, touches, within, withinDistance, difference, intersection, symDifference, union, and relate.

- a) **relativePosition**: *A.relativePosition(B, projectTo)*, returns the relativePosition enumerator that describes *B*'s relative position to *A* with respect to the direction defined by *projectTo*.
- b) **relatePosition**: *A.relatePosition(B, relation, projectTo)* returns whether *B* has the relative position to *A* given by *relation* with respect to the direction *projectTo*.
- c) **parentOf**: *A.parentOf(B, inheritID, projectTo)*, returns whether *A* is a parent cell of *B*, optionally filtered by *inheritID* and *projectTo*.
- d) **childOf**: *A.childOf(B, inheritID, projectTo)*, returns whether *A* is a child cell of *B*, optionally filtered by *inheritID* and *projectTo*.
- e) **siblingOf**: *A.siblingOf(B, inheritID, projectTo)*, returns whether *A* is a sibling cell of *B*, optionally filtered by *inheritID* and *projectTo*.
- f) **parent**: *A.parent(inheritID, projectTo, levels)*, returns the unique <<set>> of zoneIdentifiers for zones that satisfy *A.parentOf(B, inheritID, projectTo)* applied recursively *levels* times up the parent hierarchy. The <<set>> will have at most one member from each level of the hierarchy if *inheritID* is *True* and may have more than one if the cell refinementStrategy is not nested.
- g) **child**: *A.child(inheritID, projectTo, levels)*, returns the unique <<set>> of zoneIdentifiers for zones that satisfy *A.parentOf(B, inheritID, projectTo)* applied recursively *levels* times down the parent hierarchy.
- h) **sibling**: *A.sibling(inheritID, projectTo, levels)*, returns the unique <<set>> of zoneIdentifiers for zones that satisfy *A.parentOf(B, inheritID, projectTo)* applied recursively *levels* times outward on zones at the same refinement level. Multiple levels of sibling can also be thought of as the children of its parent(s) the specified number of levels up the hierarchy.

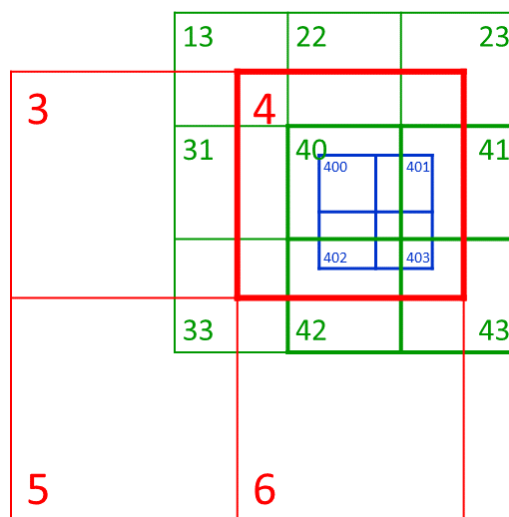


Figure 15 — Examples of parent, child, and sibling query operations

EXAMPLES *Parent, sibling and child queries for zone 40 :*

40.parent() returns {4}

40.sibling(*inheritID=true*) returns {**40, 41, 42, 43**}

40.sibling() returns {**13, 22, 23, 31, 40, 41, 42, 43**}

40.child(*inheritID=true*) returns {**400, 401, 402, 403**}

Parent, sibling and child tests for zone 40 :

40.parentOf(400) returns *true*

40.siblingOf(41) returns *true*

40.siblingOf(31, inheritID=true) returns *false*

40.siblingOf(41) returns *true*

40.childOf(4) returns *true*

Parent and child tests for zones 31 and 33 with multiple parents:

31. `childOf(4, inheritID=true)` returns *false*

31.childOf(4) returns *true*

31. `parent(inheritID=true)` returns **{3}**

31.parent() returns {3, 4}

33.parent() returns {3, 4, 5, 6}

Parent and child queries with levels set to a value greater than 1:

400. `parent(inheritID=true, levels=2)` returns **{40, 4}**

4.child(*inheritID=true, levels=2*) returns {40, 41, 42, 43, 400, 401, 402, 403, 410, 411, 412, 413, 420, 421, 422, 423, 430, 431, 432, 433}

400.sibling(*inheritID=true, levels=2*) returns {**400, 401, 402, 403, 410, 411, 412, 413, 420, 421, 422, 423, 430, 431, 432, 433**}

While some of these results extend to zones that are not drawn in the figure, the location indicated by their zonal identifier should be readily apparent from the pattern.

NOTE In all examples the optional parameters *inheritID* and *levels* take their default values of *false* and *1* respectively, unless they are specified. Since these are two-dimensional examples without any depth or time, *projectTo* has no influence.

Further query and analysis functions may then be applied to the returned data through additional software bindings. This abstract specification does not specify any requirements for the binding or implementation of further, extension, query or analytic functions.

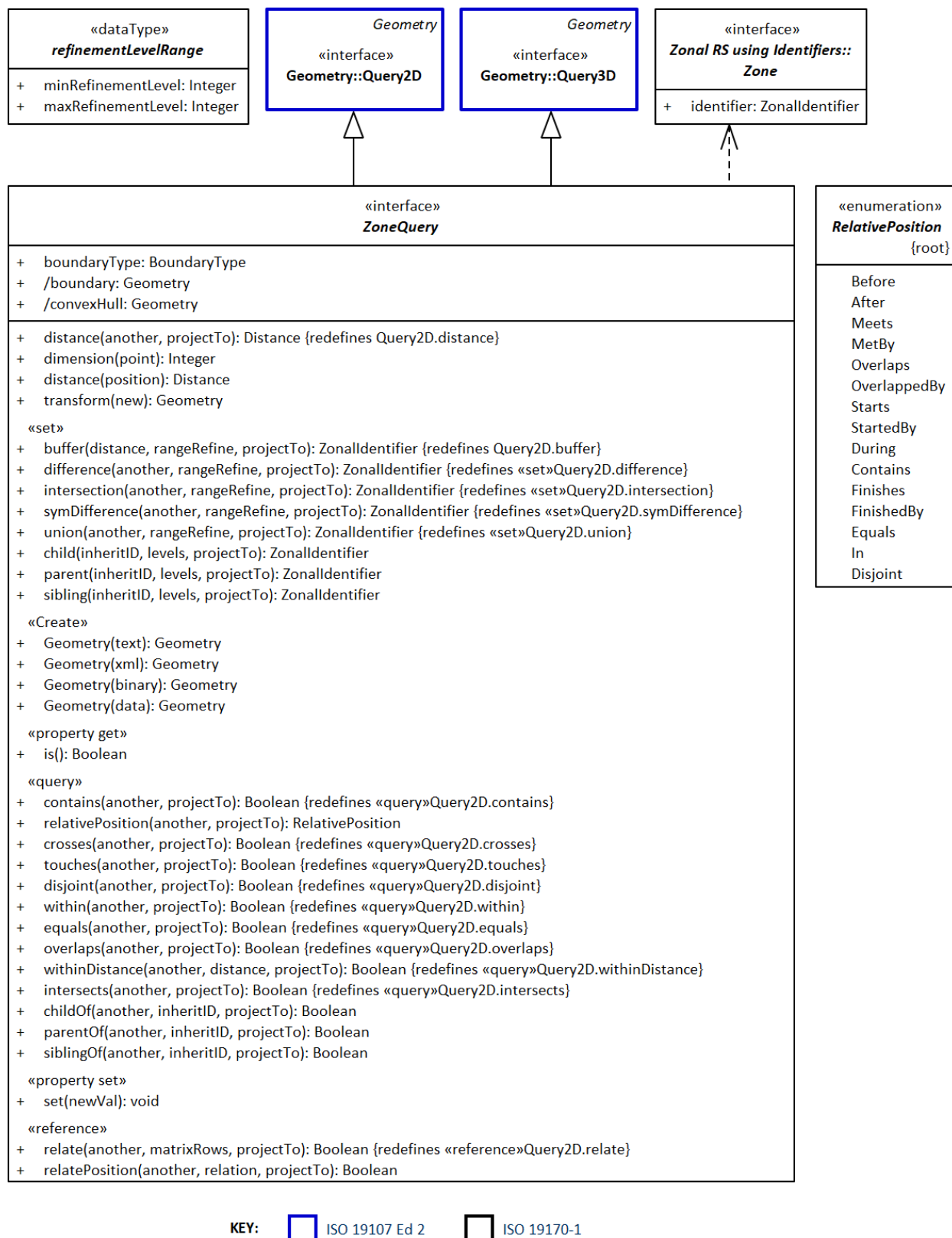


Figure 16 — Components of Topological Zonal Query Functions module

7.3.4 Defining tables

a) Table 49 — Elements of Core Topological Query Functions::refinementLevelRange

b) Table 50 — Elements of Core Topological Query Functions::ZoneQuery

c) Table 51 — Elements of Core Topological Query Functions::RelativePosition

Table 49 — Elements of Core Topological Query Functions::refinementLevelRange

Name:	refinementLevelRange					
Definition:	Datatype to define a range of refinement levels, specified through a lower- and an upper-bound. Both bounds are included within the range. The range acts as a filter on the ZoneClass's refinementLevel attribute.					
Stereotype:	DataType					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	maxRefinementLevel	Upper-bound of the refinement level range.		M	1	Integer
	minRefinementLevel	Lower-bound of the refinement level range.		M	1	Integer
Constraints:	(none)					

Table 50 — Elements of Core Topological Query Functions::ZoneQuery

Name:	ZoneQuery					
Definition:	ZoneQuery redefines the DE9IM operations in Geometry::Query2D and Geometry::Query3D and provides relativePosition and relatePosition operations for the topology of zones.					
Stereotype:	Interface					
Abstract:	true					
Associations :	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	boundary	Boundary of the combined spatial geometries of the zones in the query.	true	M	1	Geometry
	boundaryType	Boundary type of the combined spatial geometries of the zones in the query.		M	1	BoundaryType
	convexHull	Convex hull of the combined spatial geometries of the zones in the query.	true	M	1	Geometry
Operations:	<i>Name</i>	<i>Parameters:ParameterType</i>	<i>Return type</i>	<i>Definition</i>		
	distance	(another:ZonalIdentifier, projectTo:DirectPosition[4])	Distance	A.distance(B)		
<<query>> (1D)	relativePosition	(another:ZonalIdentifier, projectTo:DirectPosition[4])	RelativePosition	A.relativePosition(B,(0,0,0,1))		
<<query>>	contains	(another:ZonalIdentifier, projectTo:DirectPosition[4])	Boolean	A.contains(B) $\Leftrightarrow A \supseteq B$		
	crosses	(another:ZonalIdentifier, projectTo:DirectPosition[4])	Boolean	A.crosses(B)		
	disjoint	(another:ZonalIdentifier, projectTo:DirectPosition[4])	Boolean	A.disjoint(B) $\Leftrightarrow A \cap B = \emptyset$		
	equals	(another:ZonalIdentifier, projectTo:DirectPosition[4])	Boolean	A.equals(B) $\Leftrightarrow A = B$		
	intersects	(another:ZonalIdentifier, projectTo:DirectPosition[4])	Boolean	A.intersects(B) $\Leftrightarrow A \cap B \neq \emptyset$		
	overlaps	(another:ZonalIdentifier, projectTo:DirectPosition[4])	Boolean	A.overlaps(B)		
	touches	(another:ZonalIdentifier, projectTo:DirectPosition[4])	Boolean	A.touches(B)		
	within	(another:ZonalIdentifier, projectTo:DirectPosition[4])	Boolean	A.within(B) $\Leftrightarrow B \text{ contains } A$		
	withinDistance	(another:ZonalIdentifier, dist:Distance, projectTo:DirectPosition[4])	Boolean	A.withinDistance(B) $\Leftrightarrow A \text{ distance } B < \text{dist}$		
	parentOf	(another:ZonalIdentifier, inheritID:Boolean, projectTo:DirectPosition[4])	Boolean	A.parentOf(B)		
	childOf	(another:ZonalIdentifier, inheritID:Boolean, projectTo:DirectPosition[4])	Boolean	A.childOf(B)		
	siblingOf	(another:ZonalIdentifier, inheritID:Boolean, projectTo:DirectPosition[4])	Boolean	A.siblingOf(B)		
	buffer	(dist:Distance, projectTo:DirectPosition[4])	ZonalIdentifier	A.buffer(dist)		

<<set>>	difference	(another:ZonalIdentifier, rangeRefine:refinementLevelRange, projectTo:DirectPosition[4])	ZonalIdentifier	A.difference(B) $\Leftrightarrow$ A-B
	intersection	(another:ZonalIdentifier, rangeRefine:refinementLevelRange, projectTo:DirectPosition[4])	ZonalIdentifier	A.intersection(B) $\Leftrightarrow$ A $\cap$ B
	symDifference	(another:ZonalIdentifier, rangeRefine:refinementLevelRange, projectTo:DirectPosition[4])	ZonalIdentifier	A.symDifference(B) $\Leftrightarrow$ (A-B) $\cup$ (B-A)
	union	(another:ZonalIdentifier, rangeRefine:refinementLevelRange, projectTo:DirectPosition[4])	ZonalIdentifier	A.union(B) $\Leftrightarrow$ A $\cup$ B
	parent	(inheritID:Boolean, levels:Integer, projectTo:DirectPosition[4])	ZonalIdentifier	A.parent(B)
	child	(inheritID:Boolean, levels:Integer, projectTo:DirectPosition[4])	ZonalIdentifier	A.child(B)
	sibling	(inheritID:Boolean, levels:Integer, projectTo:DirectPosition[4])	ZonalIdentifier	A.sibling(B)
<<reference>> (1D)	relatePosition	(another:ZonalIdentifier, relate:RelativePosition, projectTo:DirectPosition[4])	Boolean	A.relatePosition(B,enum,(0,0,1,0))
<<reference>>	relate	(another:ZonalIdentifier, matrix:CharacterString, projectTo:DirectPosition[4])	Boolean	A.relate(B,matrix)
Constraints:		(none)		

Table 51 — Elements of Core Topological Query Functions::RelativePosition

Name:	RelativePosition	
Definition:	Enumeration for the relative position of two geometries projected to a single uni-directional dimension, e.g. time. NOTE In this document the relative position names follow those jointly adopted by W3C and OGC 16-071r3 [54], which is more recent than ISO 19108.	
Stereotype:	Enumeration	
Abstract:	true	
Associations:	(none)	
Values:	<i>Name</i>	<i>Definition:</i> <i>self and another are two ZoneGeometries projected to a single uni-dimensional dimension.</i>
	Before	self.end < another.begin
	After	self.begin > another.end
	Meets	self.end = another.begin
	MetBy	self.begin = another.end
	Overlaps	self.begin < another.begin AND self.end > another.begin AND self.end < another.end
	OverlappedBy	self.begin < another.end AND self.end > another.end
	Starts	self.begin = another.begin AND self.end < another.end
	StartedBy	self.begin = another.begin AND self.end > another.end
	During	self.begin > another.begin AND self.end < another.end
	Contains	self.begin < another.begin AND self.end > another.end
	Finishes	self.end = another.end AND self.begin > another.begin
	FinishedBy	self.begin > another.begin AND self.end = another.end
	Equals	self.begin = another.begin AND self.end = another.end
	In	self.relativePosion(another) IN [Starts, During, Finishes]
	Disjoint	self.relativePosion(another) IN [Before, After]

The following requirement applies:

Requirement 35: www.opengis.net/spec/DGGS/2.0/req/core/functions/query/zonequery

A DGGS specification shall implement query operations that conform to the data model in Figure 16 and definitions in Table 49–Table 51, across its entire domain.

7.3.5 Core Interoperation Functions module

7.3.5.1 Overview of interoperation functions

While the quantization and topological query functions enable a DGGS implementation to successfully operate internally, in order to facilitate connectivity with other spatial data infrastructures, additional interoperation functions are required. As shown in Figure 17, the interoperation functions are split into two modules:

- Interoperation Query: Interpret and translate external data queries sent to the DGGS implementation; and
- Interoperation Broadcast: Convert the result set returned from a DGGS query operation from internal data format(s) (optimized for that DGGS implementation) to format(s) suitable for external data delivery.

This document does not specify the specific interface protocol encodings required to connect a DGGS implementation to an external client and to facilitate the transfer of information into and out of a DGGS. This abstract specification makes use of the tools available in ISO 19156 to facilitate the linkage between

external query operations and the data/observations assigned to the DGGs zone(s) of interest. Specific interface encodings are anticipated to be elaborated as extensions to this abstract specification.

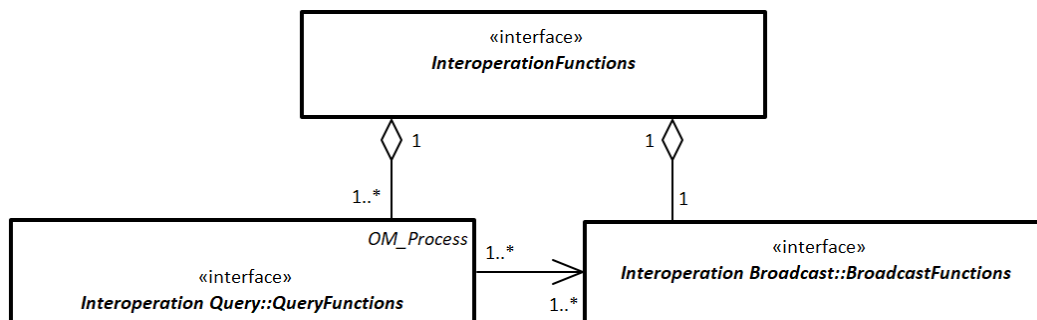


Figure 17 — Components of Core Interoperation Functions module

7.3.5.2 Defining tables

a) Table 52— Elements of Core Interoperation Functions::InteroperationFunctions

Table 52 — Elements of Core Interoperation Functions::InteroperationFunctions

Name:	InteroperationFunctions
Definition:	Interoperation is modelled as receipt of a query from an external service and broadcast of results.
Stereotype:	Interface
Abstract:	true
Associations:	(none)
Public attributes:	(none)
Constraints:	(none)

7.3.5.3 Interoperation Query module

External queries may originate from an external client application and range in syntax from natural language queries (e.g. ‘Where are the gas pipelines in Western Canada located?’, or ‘How has the Murray-Darling Basin in Australia changed over the past 27 years?’, or ‘Compute the watershed area of the Kawarau Catchment in New Zealand’), to an OWS ‘GetCapabilities’ or similar type of query, to an SQL (or similar) statement. To support interoperability, a DGGs specification shall define methods to receive, interpret and translate an external data query (or process) request into a form that can be processed by the internal DGGs data retrieval and query functions.

Figure 18 shows the key functional elements required for DGGs to translate and execute an external query or process operations.

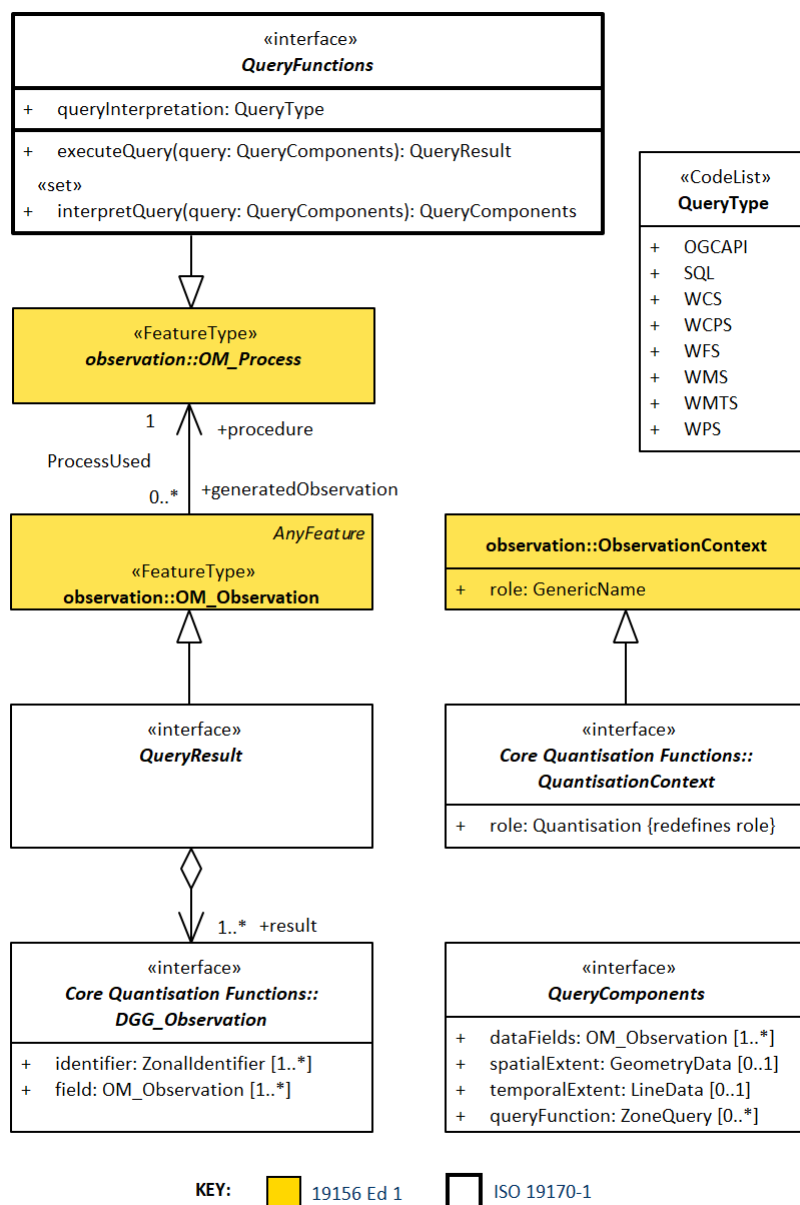


Figure 18 — Components of Interoperation Query module

7.3.5.4 Defining tables

- Table 53 — Elements of Interoperation Query::QueryComponents
- Table 54 — Elements of Interoperation Query::QueryFunctions
- Table 55 — Elements of Interoperation Query::QueryResult
- Table 56 — Elements of Interoperation Query::QueryType

Table 53 — Elements of Interoperation Query::QueryComponents

Name:	QueryComponents					
Definition:	Structure to hold parameters for a query.					
Stereotype:	Interface					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	dataFields	Descriptor of the non-spatial information that is requested from the DGGS.		M	*	OM_Observation
	queryFunction	Spatio-temporal extent of the region of interest for the query, expressed as a ZonalAlgebra expression.		C	*	ZoneQuery
	spatialExtent	Spatial extent of the region of interest for the query, expressed as GeometryData.		C	1	GeometryData
	temporalExtent	Temporal extent of the region of interest for the query, expressed as temporal geometry.		C	1	LineData
Constraints:	(none)					

Table 54 — Elements of Interoperation Query::QueryFunctions

Name:	QueryFunctions					
Definition:	QueryFunctions is an interface to receive, interpret, and execute queries from external services. Queries for broadcast are modelled as OM_Process, which makes an OM_Observation of a <<set>> of Cells and their associated DGG_Observations to create a QueryResult. The ObservationContext:role is selected from the Quantization CodeList.					
Stereotype:	Interface					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	queryInterpretation	Identifies the language type for query.		M	1	QueryType (code list)
Operations:	<i>Name</i>	<i>Parameters:ParameterType</i>	<i>Return type</i>	<i>Definition</i>		
	interpretQuery	(query:QueryComponents)	QueryComponents	Transform query components from an external structure to a <<set>> of one or more query components structured for execution by the DGGS.		
	executeQuery	(query:QueryComponents)	QueryResult	Execute query to generate a result.		
Constraints:	(none)					

Table 55 — Elements of Interoperation Query::QueryResult

Name:	QueryResult			
Definition:	Abstract placeholder for a query result.			
Stereotype:	Interface			
Abstract:	true			
Associations:	<i>Association with:</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	DGG_Observation (feature type)	M	*	result
Public attributes:	(none)			
Constraints:	(none)			

Table 56 — Elements of Interoperation Query::QueryType

Name:	QueryType	
Definition:	CodeList for the structure of an interoperation query.	
Stereotype:	CodeList	
Abstract:	true	
Associations:	(none)	
Values:	<i>Name</i>	<i>Definition</i>
	OGCAPI	OGC API query.
	SQL	Structured Query Language query.
	WCS	Web Coverage Service query.
	WCPS	Web Coverage Processing Service query.
	WFS	Web Feature Service query.
	WMS	Web Map Processing Service query.
	WMTS	Web Map Tile Service query.
	WPS	Web Processing Service query.

The following requirement applies:

Requirement 36: www.opengis.net/spec/DGGS/2.0/req/core/functions/interoperation/query

A DGGS specification shall implement operations to read, interpret and execute external data queries that conform to the data model in Figure 17 and Figure 18 and definitions in Table 52–Table 56.

7.3.5.5 Interoperation Broadcast module

Just as it is necessary for DGGS to be able to interpret and execute external data queries, DGGS shall also define methods to broadcast results from data queries to external client(s) or data infrastructure(s). External clients are anticipated to be web-based client(s), software client(s) on the same ICT infrastructure as the DGGS, or other DGGS.

Figure 19 shows basic elements required to translate the result set(s) returned from a DGGS data query into a suitable data format for transfer and broadcast the reformatted result set via one or a number of data or information transfer protocols.

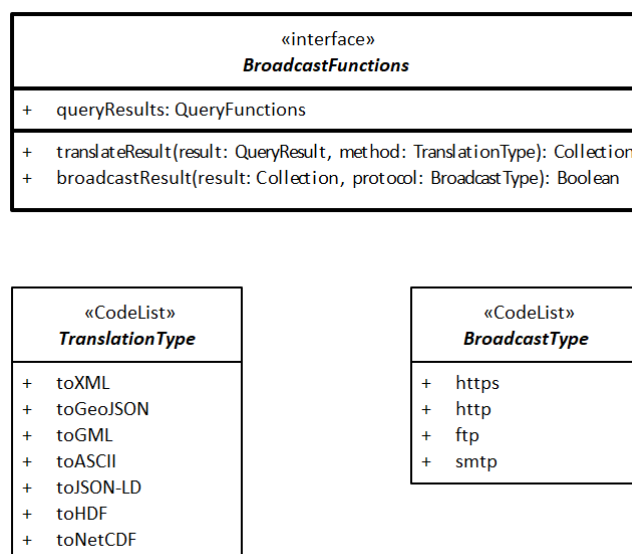


Figure 19 — Components of Interoperation Broadcast module

7.3.5.6 Defining tables

a) Table 57 — Elements of Interoperation Broadcast::BroadcastFunctions

b) Table 58 — Elements of Interoperation Broadcast::TranslationType

c) Table 59 — Elements of Interoperation Broadcast::TranslationType

Table 57 — Elements of Interoperation Broadcast::BroadcastFunctions

Name:	BroadcastFunctions					
Definition:	An interface to translate the results from an Interoperation Query::QueryFunctions into the requested format and return it to the client.					
Stereotype:	Interface					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	queryResults	Result received from the QueryFunctions ready for processing for export.		M	1	QueryFunctions
	resultBroadcast			M	1	BroadcastMethod
	resultTranslation			M	1	ResultTranslationMethod
Operations:	<i>Name</i>	<i>Parameters:ParameterType</i>	<i>Return type</i>	<i>Definition</i>		
	translateResult	(result:QueryResult)	Collection	Reformat query result from internal structure to requested format for broadcast.		
	broadcastResult	(result:Collection)	Boolean	Broadcast reformatted result to client using designated protocol and return acknowledgement of success.		

Constraints:	(none)
---------------------	--------

Table 58 — Elements of Interoperation Broadcast::BroadcastType

Name:	BroadcastType	
Definition:	CodeList for DGGS interoperation data broadcast protocols.	
Stereotype:	CodeList	
Abstract:	true	
Associations:	(none)	
Values:	<i>Name</i>	<i>Definition</i>
	https	Broadcast over Hypertext transfer secure protocol.
	http	Broadcast over Hypertext transfer protocol.
	ftp	Broadcast over File transfer protocol.
	smtp	Broadcast over Simple mail transfer protocol.

Table 59 — Elements of Interoperation Broadcast::TranslationType

Name:	TranslationType	
Definition:	CodeList for DGGS interoperation data broadcast translation formats.	
Stereotype:	CodeList	
Abstract:	true	
Associations:	(none)	
Values:	<i>Name</i>	<i>Definition</i>
	toASCII	Translate to ASCII format.
	toGeoJSON	Translate to GeoJSON format.
	toGML	Translate to GML format.
	toHDF	Translate to HDF format.
	toJSON-LD	Translate to JSON-LD format.
	toNetCDF	Translate to NetCDF format.
	toXML	Translate to XML format.

The following requirement applies:

Requirement 37:

www.opengis.net/spec/DGGS/2.0/req/core/functions/interoperation/broadcast

A DGGS specification shall implement operations to translate data results from interoperation queries to standard data formats and broadcast the reformatted result set that conform to the data model in Figure 17 and Figure 19, and definitions in Table 52 and Table 57–Table 59.

8 Equal-area Earth DGGS

8.1 Equal-Area Earth DGGS package

8.1.1 Equal-Area Earth RS module

This clause specifies the Equal-Area Earth RS module.

For a DGGS RS that is conformant with the DGGS Core to be an EAERS, it shall satisfy all the requirements for the Equal-Area Earth DGGS package.

The data model supports DGGS EAERS based on either static or dynamic datums. Care shall be taken when implementing DGGS with static datums. Static CRS are by their nature only intended for use on one tectonic plate. However, the definition for a DGGS always has a global domain. This apparent conundrum is resolved in two ways:

- a) **Orientation:** Noting that some static CRS have one or more points on the Earth's surface where the underlying mathematics is poorly behaved, orient the EA_BaseUnitPolyhedron so that areas, centroids, vertices, and edges can be computed; and
- b) **Precision:** On the tectonic plate where the reference frame is static choose the level of DGGs precision to suit the intended use of the DGGs (typically in the range of millimetres to 10s of metres), and in areas of the Earth on plates that are moving with respect to the static reference frame choose the level of DGGs precision to reflect the larger of the constraints imposed by the mathematics and by plate tectonics (typically in the of range 10s to 100 000s of metres).

Dynamic datums present problems of a different form. The most frequently used is WGS 84, which is a datum ensemble. Care shall be taken to ensure that the error budget for EA_Cell's area is set at a value that caters to the level of approximation in the WGS 84 definition.

Figure 20, Figure 21 and Figure 22 show the data models for modules in the Equal-Area Earth DGGs package.

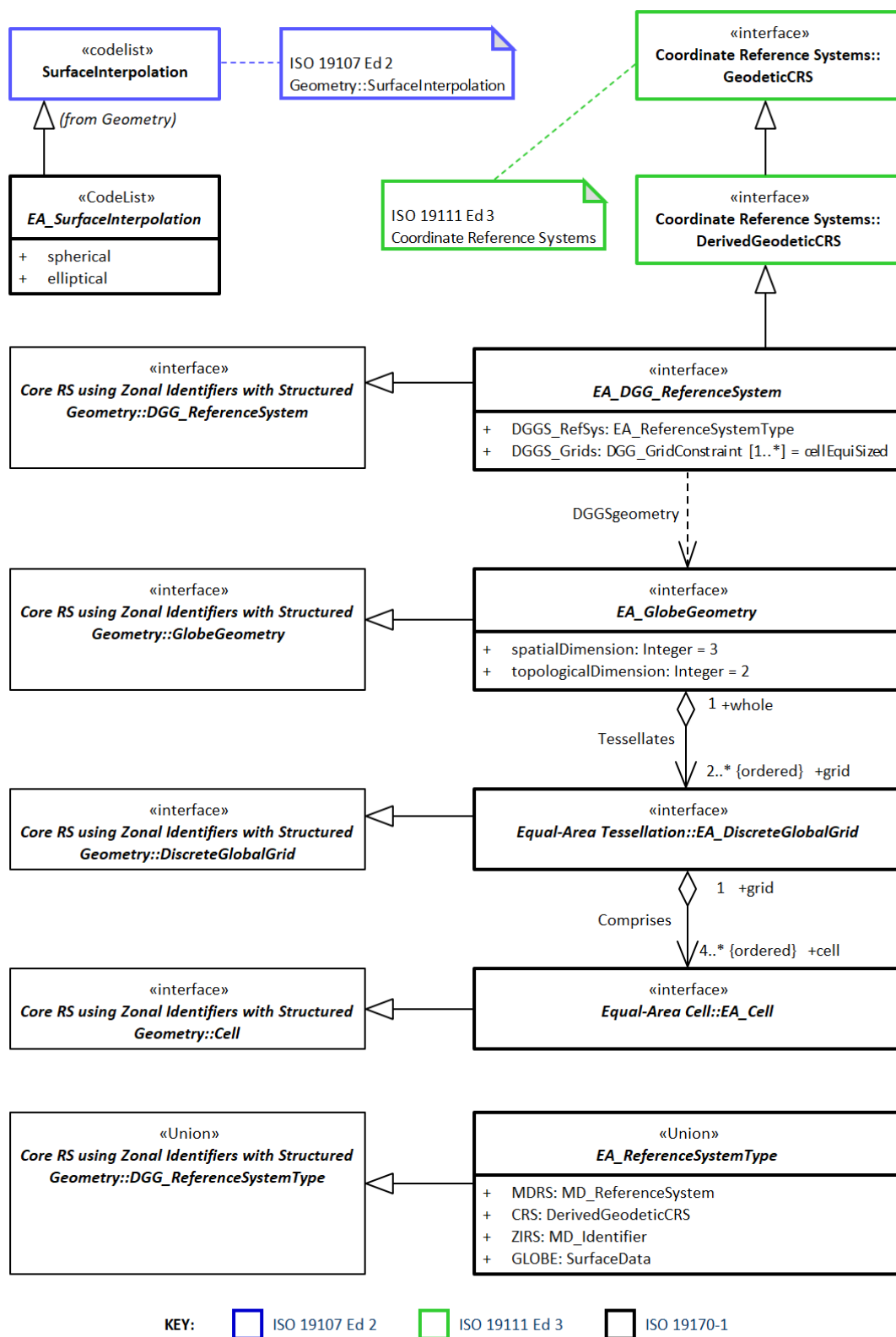


Figure 20 — Components of Equal-Area Earth RS module

See [8.1.2](#) for definitions of elements in this Figure.

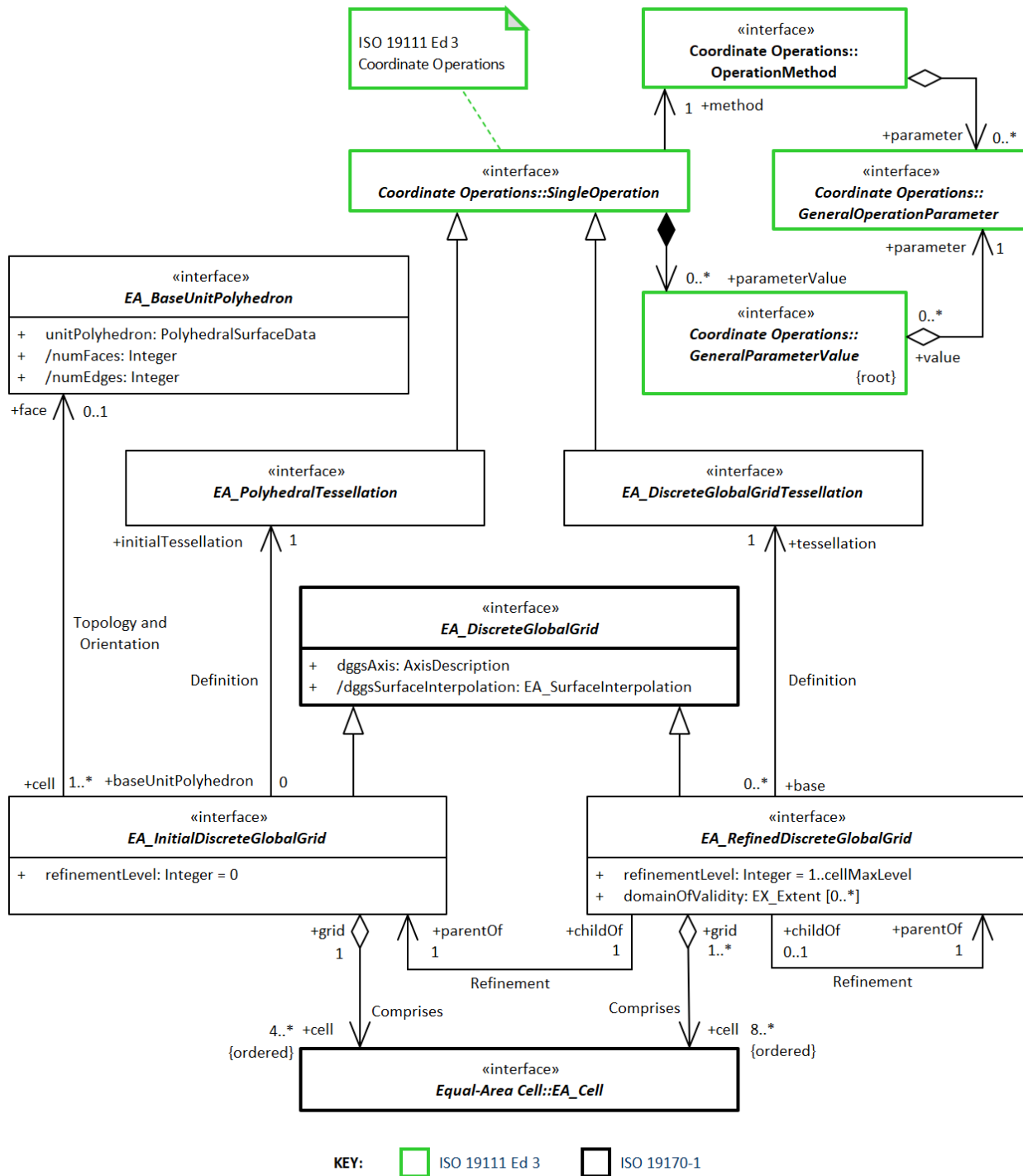


Figure 21 — Components of Equal-Area Tessellation module

See [8.1.4.5](#) for definitions of elements in this Figure.

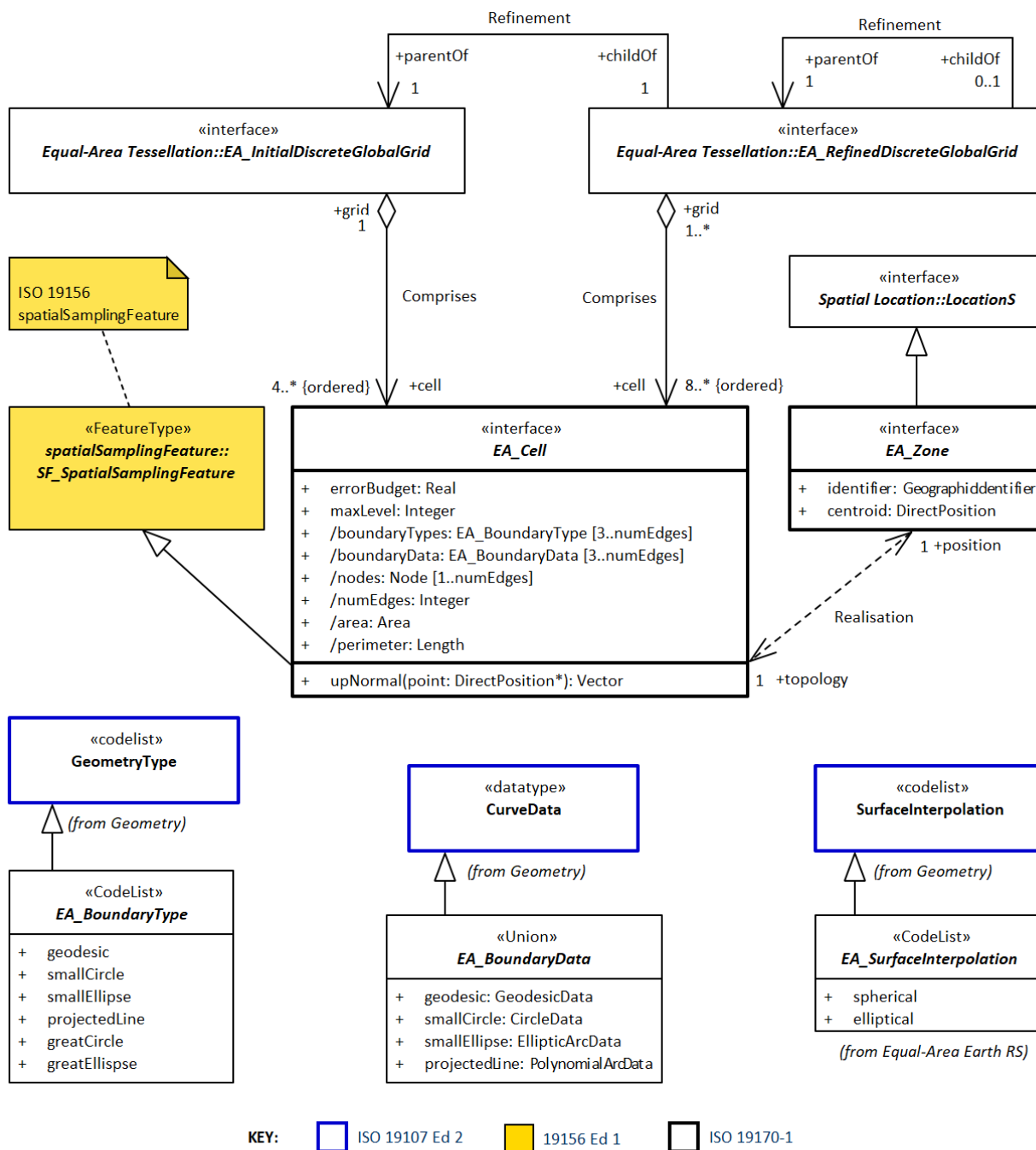


Figure 22 — Components of Equal-Area Cell module

See 8.1.5.4 for definitions of elements in this Figure.

8.1.2 Defining tables

- Table 60 — Elements of Equal-Area Earth RS::EA_DGG_ReferenceSystem
- Table 61 — Elements of Equal-Area Earth RS::EA_GlobeGeometry
- Table 62 — Elements of Equal-Area Earth RS::EA_ReferenceSystemType
- Table 63 — Elements of Equal-Area Earth RS::EA_SurfaceInterpolation

Table 60 — Elements of Equal-Area Earth RS::EA_DGG_ReferenceSystem

Name:	EA_DGG_ReferenceSystem					
Definition:	Defining characteristics of a RS using Zonal Identifiers with Structured Geometry for an Equal-Area Earth DGGs.					
Stereotype:	Interface					
Inheritance from:	DGG_ReferenceSystem					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	DGGS_Grids	List of characteristics that constrain the grid cells in this DGGs in decreasing order of priority. cellEquiSized shall be the first value.		M	*	DGG_GridConstraint (code list)
	DGGS_RefSys	Reference system metadata.		M	1	EA_ReferenceSystemType (union data type)
Constraints:	(none)					

Table 61 — Elements of Equal-Area Earth RS::EA_GlobeGeometry

Name:	EA_GlobeGeometry					
Definition:	Parent geometry specifying the geometry, dimensionality and domain of the globe for this DGGs. Geometry of the surface of an earth reference model.					
Stereotype:	Interface					
Inheritance from:	GlobeGeometry					
Abstract:	true					
Associations:	<i>Association with:</i>				<i>Obligation</i>	<i>Maximum occurrence</i>
	EA_DiscreteGlobalGrid (feature type)				M	*
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	spatialDimension	EA_GlobeGeometry shall have a spatialDimension of 3.		M	1	Integer
	topologicalDimension	EA_GlobeGeometry shall have a topologicalDimension of 2, corresponding to the surface of the Earth.		M	1	Integer
Constraints:	(none)					

Table 62 — Elements of Equal-Area Earth RS::EA_ReferenceSystemType

Name:	EA_ReferenceSystemType					
Definition:	Defining metadata elements of the base CRS for a DGGS Equal-Area Earth RS					
Stereotype:	Union					
Inheritance from:	DGG_ReferenceSystemType					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	CRS	Metadata required to reference coordinates, Includes CRS ID and coordinate Epoch for dynamic CRS.		M	1	DerivedGeodeticCRS
	GLOBE	SurfaceData for the chosen EA_GlobeGeometry that specifies geometry, spatial, and topological dimensionality and domain of the globe for this DGGS.		M	1	SurfaceData
	MDRS	Reference system information describing this whole DGGS.		M	1	MD_ReferenceSystem
	ZIRS	Identifier for the spatial RSUsingZonalIdentifiers used by the DGGS.		M	1	MD_Identifier
Constraints:	(none)					

Table 63 — Elements of Equal-Area Earth RS::EA_SurfaceInterpolation

Name:	EA_SurfaceInterpolation	
Definition:	Subset of Geometry::SurfaceInterpolation (code list) providing permitted interpolation methods for EA_Cell.	
Stereotype:	CodeList	
Abstract:	true	
Associations:	(none)	
Values:	<i>Name</i>	<i>Definition</i>
	spherical	The EA_Cell surface is a section of a spherical surface. NOTE For EA_Cells of sufficiently small extent, linear interpolation is sufficient to meet the EA_Cell.errorBudget for area.
	elliptical	The EA_Cell surface is a section of an elliptical surface. NOTE For EA_Cells of sufficiently small extent, spherical interpolation is sufficient to meet the EA_Cell.errorBudget for area. NOTE For EA_Cells of sufficiently small extent, linear interpolation is sufficient to meet the EA_Cell.errorBudget for area.

The following requirement applies:

Requirement 38: www.opengis.net/spec/DGGS/2.0/req/ea/ers/harmonised_model

An EAERS specification shall comply with the data model in Figure 20–Figure 22 and definitions in Table 60–Table 73.

8.1.3 Global domain

For a DGGS RS to be an EAERS, the domain shall be defined as the entire surface of the Earth.

The following requirement applies:

Requirement 39: www.opengis.net/spec/DGGS/2.0/req/ea/ers/global_domain

EAERS global domain — the domain of an EAERS shall be the whole surface of the reference frame's Earth model and the DGG_ReferenceSystem shall specify cellEqualSized as one of the DGGS_Grids constraint values.

8.1.4 Equal-Area Tessellation module**8.1.4.1 Tessellation overview**

A multiresolution hierarchical tessellation of cells is created by constructing a sequence of discrete global grids, each with successively finer cell resolutions. First an initial discrete global grid is constructed as described in subclause [8.1.4.2](#). The cells of this initial tessellation are then iteratively refined by application of cell refinement method(s) [\[34\]](#) to create finer resolution child cells. The initial tessellation, the cell shape, the refinement methods and indexing methods may all vary for different DGGSs.

8.1.4.2 Initial tessellation

The entire surface of the Earth is partitioned to a finite/discrete set of regions. Most methods initially approximate the Earth's surface using a simple base unit polyhedron which is scaled so that all vertices are located on the surface model of the Earth, and the edges are warped so they also lie on the surface model. The resulting edges may be any of the types listed in EA_CurveType. These include geodesics, small circles, small ellipses and lines that project to a straight line on a plane. These all result from intersections of a plane and an ellipsoid. The initial discrete global grid tessellation has the same form as the base unit polyhedron. Each EA_Cell of the initial tessellation represents one face of the chosen base unit polyhedron mapped to the chosen surface model of the Earth. This document refers to the initial tessellation as a "polyhedral tessellation". The most common choices for an initial base unit polyhedron are discussed in subclause [C.4](#) [\[34\]](#).

The following requirement applies:

Requirement 40: www.opengis.net/spec/DGGS/2.0/req/ea/ers/tessellation/initial

An EAERS specification shall include an initial tessellation that is defined by equal area cells produced by mapping the faces of a base unit polyhedron to the surface model of the Earth.

8.1.4.3 Tessellation sequence

DGGS EAERS comprise a discrete sequence of global grids formed from recursive application of a tessellation method to refine the grid cells, so that each global grid has a progressively finer spatial resolution.

The following requirements apply:

Requirement 41: www.opengis.net/spec/DGGS/2.0/req/ea/ers/tessellation/sequence

An EAERS specification shall have tessellation operations that generate a sequence of discrete global grids with progressively smaller cells.

Requirement 42: www.opengis.net/spec/DGGS/2.0/req/ea/ers/tessellation/sequence/max

An EAERS specification shall specify a limit to the number of iterations in its sequence of discrete global grids, to ensure that the error budget for EA_Cell's area is not exceeded.

8.1.4.4 Global area preservation

Preservation of total surface area throughout the range of hierarchical tessellations is a necessary property of DGGSs in order to represent information consistently at successive resolutions. This

requirement ensures that each level of grid refinement completely covers the Earth's surface without cell overlaps.

The following requirement applies:

Requirement 43:

www.opengis.net/spec/DGGS/2.0/req/ea/ers/tessellation/global_area_preservation

For each successive discrete global grid of an EAERS specification one of the following two statements shall apply:

Dynamic Datum	If the base CRS has a dynamic datum the sequence of discrete global grids shall preserve global domain completeness and position uniqueness throughout the sequence.
Static Datum	If the base CRS has a static datum the sequence of discrete global grid shall preserve domain completeness and position uniqueness throughout the sequence for all EA_Cells within their respective discrete global grids.

8.1.4.5 Defining tables

- a) Table 64 — Elements of Equal-Area Tessellation::EA_BaseUnitPolyhedron
- b) Table 65 — Elements of Equal-Area Tessellation::EA_DiscreteGlobalGrid
- c) Table 66 — Elements of Equal-Area Tessellation::EA_DiscreteGlobalGridTessellation
- d) Table 67 — Elements of Equal-Area Tessellation::EA_InitialDiscreteGlobalGrid
- e) Table 68 — Elements of Equal-Area Tessellation::EA_PolyhedralTessellation
- f) Table 69 — Elements of Equal-Area Tessellation::EA_RefinedDiscreteGlobalGrid

Table 64 — Elements of Equal-Area Tessellation::EA_BaseUnitPolyhedron

Name:	EA_BaseUnitPolyhedron					
Definition:	EA_BaseUnitPolyhedron Polyhedron with circumsphere radius of one, specified by the number and faces and edges and the collection of boundary curves that make up each polygonal face.					
Stereotype:	Interface					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	numEdges	Number of edges in the EA_BaseUnitPolyhedron,	true	M	1	Integer
	numFaces	Number of faces on the EA_BaseUnitPolyhedron, corresponds to the number of EA_Cells in the EA_InitialDiscreteGlobalGrid.	true	M	1	Integer
	unitPolyhedron	PolygonData for each of the unit Polyhedron's segment Polygons, expressed in spherical coordinates (theta, phi) with unit radius.		M	1	PolyhedralSurfaceData
Constraints:	self.vertex.r = 1					

Table 65 — Elements of Equal-Area Tessellation::EA_DiscreteGlobalGrid

Name:	EA_DiscreteGlobalGrid					
Definition:	Super class for EA_InitialDiscreteGlobalGrid and EA_RefinedDiscreteGlobalGrid					
Stereotype:	Interface					
Inheritance from:	DiscreteGlobalGrid					
Generalization of:	EA_InitialDiscreteGlobalGrid, EA_RefinedDiscreteGlobalGrid					
Abstract:	true					
Associations :	<i>Association with:</i>			<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	EA_Cell (feature type)			M	*	cell
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	dggsAxis	A dggsAxis typically follows a space-filling curve designed to recursively traverse all cells in each tessellation, Cell::identifiers are ordered along the path of the dggsAxis.		M	1	AxisDescription
	dggsSurfaceInterpolation	EA_SurfaceInterpolation corresponding to the form of the specified EA_GlobeGeometry.	true	M	1	EA_SurfaceInterpolation (code list)
Constraints:	(none)					

Table 66 — Elements of Equal-Area Tessellation::EA_DiscreteGlobalGridTessellation

Name:	EA_DiscreteGlobalGridTessellation
Definition:	The EA_DiscreteGlobalGridTessellation method implements the DGGS_Grids constraint, DGGS_Refinement strategy and DGGS_RefinementRatio, to create a child EA_RefinedDiscreteGlobalGrid from a parent EA_DiscreteGlobalGrid.
Stereotype:	Interface
Abstract:	true
Associations:	(none)
Public attributes:	(none)
Constraints:	(none)

Table 67 — Elements of Equal-Area Tessellation::EA_InitialDiscreteGlobalGrid

Name:	EA_InitialDiscreteGlobalGrid					
Definition:	The EA_InitialDiscreteGlobalGrid is formed by applying the EA_PolyhedralTessellation method to a EA_BaseUnitPolyhedron.					
Stereotype:	Interface					
Inheritance from:	EA_DiscreteGlobalGrid					
Abstract:	true					
Associations :	<i>Association with:</i>			<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	EA_Cell (feature type)			M	*	cell
	EA_BaseUnitPolyhedron (feature type)			C	1	face
	EA_PolyhedralTessellation (feature type)			M	1	initialTessellation
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	refinementLevel	EA_InitialDiscreteGlobalGrid has a refinementlevel of 0.		M	1	Integer
Constraints:	(none)					

Table 68 — Elements of Equal-Area Tessellation::EA_PolyhedralTessellation

Name:	EA_PolyhedralTessellation					
Definition:	The EA_PolyhedralTessellation method transforms the EA_BaseUnitPolyhedron in such a way that: 1) the surface area of each cell belonging to the EA_InitialDiscreteGlobalGrid is the same, 2) domain completeness is preserved by the EA_InitialDiscreteGlobalGrid, and 3) location uniqueness is preserved by the EA_InitialDiscreteGlobalGrid.					
Stereotype:	Interface					
Abstract:	true					
Associations:	(none)					
Public attributes:	(none)					
Constraints:	(none)					

Table 69 — Elements of Equal-Area Tessellation::EA_RefinedDiscreteGlobalGrid

Name:	EA_RefinedDiscreteGlobalGrid					
Definition:	EA_DiscreteGlobalGrid formed by an EA_DiscreteGlobalGridTessellation, is a EA_RefinedDiscreteGlobalGrid.					
Stereotype:	Interface					
Inheritance from:	EA_DiscreteGlobalGrid					
Abstract:	true					
Associations:	<i>Association with:</i>			<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Provides:</i>
	EA_Cell (feature type)			M	*	cell
	EA_RefinedDiscreteGlobalGrid (feature type)			M	1	parentOf
	EA_InitialDiscreteGlobalGrid (feature type)			M	1	parentOf
	EA_DiscreteGlobalGridTessellation (feature type)			M	1	tessellation
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	domainOfValidity	For DGGs with a dynamic datum the domainOfValidity is always global.		C	*	EX_Extent
	refinementLevel	The child EA_RefinedDiscreteGlobalGrid has a refinementlevel of one greater than its parent.		M	1	Integer
Constraints:	(none)					

8.1.5 Equal-Area Cell module

8.1.5.1 Cells are simple polygons

EA_Cells are simple polygons formed from an ordered set of boundary curves adhering to the geometric reference surface of the Earth model. EA_Cells are defined in three-dimensional space and are topologically two-dimensional. Different cell shapes can be used, typically triangle, quadrilateral, pentagon, hexagon, and octagon. Cells formed from faces of the five (5) Platonic solids (tetrahedron-triangle, cube-quadrilateral, octahedron-triangles, dodecahedron-pentagons, icosahedron-triangles) all satisfy the requirements for simple cells. Larger numbers of faces and therefore cells at the top of the hierarchy of tessellations, increases the uniformity of the cell shape. The truncated icosahedron, with thirty-two (32) faces is often used for DGGs. It produces mostly hexagons augmented by twelve (12) pentagons in each tessellation. Each cell shape has its own advantages and disadvantages^[34] and it is usually desirable for each refined discrete global grid to have a majority of cells with the same shape^{[37],[41]}. Triangular, quadrilateral and hexagonal cells are common choices used in DGGs on the surface of the Earth. These shapes provide regular tiling of the plane^[37], which can be mapped to a curved surface such as a spherical or ellipsoidal Earth surface model.

The cell structures in each successive level of cell refinement are constrained by the properties of the initial tessellation, but do not necessarily have the same geometry as the initial tessellation. Simple two-dimensional cells have the following properties:

- a) edges meet only at the vertices;
- b) exactly two edges meet at each vertex;
- c) exactly the same number of edges and vertices; and,
- d) enclose a region which always has a measurable area.

The following requirement applies:

Requirement 44: www.opengis.net/spec/DGGS/2.0/req/ea/ers/cell/simple/2d_polygon

For each successive discrete global grid, an EAERS specification shall define EA_Cells that are simple polygons.

8.1.5.2 Cells referenced at their centroid

Each EA_Cell shall be referenced at its centroid. This is because the centroid is the only location that provides a representative point that behaves consistently with shape and is invariant under orientation. The representative point for an EA_Cell shall lie on the surface of the cell. For curved surfaces, the “centre of gravity” computed in three-dimensions cannot actually lie on the surface (see ISO 19107:2019, clause [6.4.4.8](#)). If, however, the “centre of gravity” is computed using distances computed along geodesic arcs on the curved surface, then the centroid is constrained to lie on the surface. This is a centroid calculated as the “geodesic centre of surface area” of an EA_Cell.

The centroid enables a dual representation of a DGGS tessellation as both two-dimensional areal cell grids and as point-based lattices of cell reference locations.

The following requirement applies:

Requirement 45: www.opengis.net/spec/DGGS/2.0/req/ea/ers/cell/direct_position/centroid

An EAERS specification shall define the DirectPosition of an EA_Cell to be the centroid of the EA_cell, computed as the geodesic centre of surface area.

8.1.5.3 Cells of equal area

This document defines an EAERS based on a hierarchy of equal area tessellations. Cells of equal area provide global grids with spatial units that (at multiple resolutions) have an equal probability of contributing to an analysis. Equal area cells also help to minimize the confounding effects of area variations in spatial analyses where the curved surface of the earth is the fundamental reference frame.

In an EAERS the unit of measure is a unit of area, not length as in a cartesian XYZ coordinate system or angle as in an ellipsoidal coordinate system. For angular measures the degree is defined as one 360th integer fraction of a full circle, and by analogy the areal unit of measure of a DGGS coordinate reference system is an integer fraction of the surface area of the chosen ellipsoidal surface model for the earth. For DGGSs the integer fraction is the number of cells in the initial discrete global grid. Continuing the angular analogy with minutes being 1/60th of a degree and seconds being 1/60th of a minute, for DGGSs, recursive use of the refinement ratio generates a sequence of smaller areal units, one for each refined discrete global grid.

Standard units of measure are defined through a reference measure with defined precision. The meter unit of length has been redefined a number of times as technology has improved. For example:

- a) **From 1793:** 1/10 000 000 of the meridian through Paris between the North Pole and the Equator (+/- $\sim 10^{-4}$ m); and
- b) **From 1983:** The length of the path travelled by light in a vacuum in 1/299 792 458th of a second (+/- 10^{-10} m).

To address the need for transparency of the precision in its units of area, this document uses the concept of a specified error budget. The error budget takes into account all sources of variation that are relevant to the particular DGGS, its derivation, and its expected use. For most day to day uses, most of these sources contribute errors that are significantly smaller than the precision required of the DGGS. However, as technology pushes the limits of available precision, use-cases demand combining data from highly

disparate sources, and users push their expectations, it becomes increasingly important to know when limits of use are reached.

The sources considered for inclusion in the error budget can include:

- a) **spatial variation:** whether the available precision of each source of error is uniform or variable across the DGGS's domain;
- b) **datum:** precision of the underlying measurements for the datum;
- c) **static datum:** precision of the assertion that the coordinates are static both on the tectonic plate the datum is tied to, and away from the static plate;
- d) **earth model:** differences between the chosen ellipsoidal or spherical earth model and the real earth's surface. Spheres lead to faster and more precise computations for the tessellations but have a less precise fit to the real earth's surface.

While implementation issues are beyond the scope of this document, the following sources may contribute to increases in error budgets for an implementation:

- a) **spherical maths:** exact solutions are available for solving the required mathematics on the surface of a sphere;
- b) **ellipsoidal maths:** solving the required mathematics on the surface of an ellipsoid requires the use of iterative numerical methods which result in approximate solutions with an uncertainty determined by both the method and the number of iterations used to perform the computation;
- c) **data-type precision:** most will probably use 64-bit double precision for location, anything less will have a significant impact on the error budget;
- d) **cell edge type:** geodesics, small circles, small ellipses, and projected lines each have different solutions with different consequences for their precision and performance. At finer resolutions it may be possible to implement a simpler edge type and still stay within the implementation error budget;
- e) **error propagation:** the choice of strategy for implementing the sequence of tessellations.

The error budget puts a limit on the number of iterations in the sequence of refined discrete global grids. This is acknowledged in the requirements.

DGGSs may validly comprise more than one cell geometry. This most typically arises for systems based on truncated polyhedra such as the cuboctahedron — with both square and triangular faces, and the truncated icosahedron — with pentagonal and hexagonal faces. In these situations, equal area is interpreted to mean that all of the cells of a particular geometry are equal area, and that the ratio of the areas of the two geometries is preserved through the tessellations. For example, in the truncated icosahedron used by ISEA, the ratio of pentagonal to hexagonal areas within a tessellation level is always 5/6.

The following requirements apply:

Requirement 46: www.opengis.net/spec/DGGS/2.0/req/ea/ers/cell/equal_area/error_budget

An EAERS shall specify error budget(s) for cell area of 1% or less that represents the maximum ratio of a cells area to the theoretical average cell area of all cells in a discrete global grid computed from the number of cells in the discrete global grid and the discrete global grid's surface area. One of the following two statements shall apply:

Dynamic Datum	If the base CRS has a dynamic datum, for each successive level of grid refinement, an EAERS specification shall specify one error budget value.
Static Datum	If the base CRS has a static datum, for each successive level of grid refinement, an EAERS specification shall specify at least one error budget value for the area of the globe that it is static, and at least one error budget value for the area of the globe that is not static.

Requirement 47: www.opengis.net/spec/DGGS/2.0/req/cell/equal_area

For each discrete global grid, and for each cell geometry, an EAERS specification shall define EA_Cells that are equal area within the specified error budget.

8.1.5.4 Defining tables

a) Table 70 Elements of Equal-Area Cell::EA_BoundaryData

b) Table 71 Elements of Equal-Area Cell::EA_Cell

c) Table 72 Elements of Equal-Area Cell::EA_Zone

d) Table 73 Elements of Equal-Area Cell::EA_BoundaryType

Table 70 — Elements of Equal-Area Cell::EA_BoundaryData

Name:	EA_BoundaryData					
Definition:	Curve data for the permitted boundary types. GreatCircle and greatEllipse boundary types use the same data types as smallCircle and smallEllipse respectively.					
Stereotype:	Union					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	geodesic	Curve data for a geodesic boundary.		M	1	GeodesicData
	projectedLine	Curve data for a projected line boundary.		M	1	PolynomialArcData
	smallCircle	Curve data for a small circle boundary.		M	1	CircleData
	smallEllipse	Curve data for a small ellipse boundary.		M	1	EllipticArcData
Constraints:	(none)					

Table 71 — Elements of Equal-Area Cell::EA_Cell

Name:	EA_Cell					
Definition:	Reference system unit of geometry associated with an EA_Zone. As part of EA_GlobeGeometry, it has the same spatial, temporal and topological dimensionality as GlobeGeometry. NOTE As an EA_Cell on the surface of the Earth, its topologicalDimension is 2.					
Stereotype:	Interface					
Inheritance from:	Cell					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	area	area of the cell's surface	true	M	1	Area
	boundaryData	List of EA_BoundaryData that make up the cells' boundary, starting with the curve connecting node_0 to node_1, and continuing in a clockwise sequence.	true	M	1	EA_BoundaryData (union data type)
	boundaryTypes	List of EA_CurveTypes that make up the cells' boundary, starting with the curve connecting node_0 to node_1, and continuing in clockwise sequence.	true	M	1	EA_BoundaryType (code list)
	errorBudget	For DGGs referencing a dynamic datum, cellEqualAreaPrecision will typically be a single value for each tessellation, and therefore most efficiently realised as an attribute of each RefinedDiscreteGlobalGrid.		M	1	Real
	maxLevel	For DGGs referencing a dynamic datum, cellMaxLevel will typically be a single value for each tessellation, and therefore most efficiently realised as an attribute of each RefinedDiscreteGlobalGrid. For DGGs referencing a static datum, cellMaxLevel will have different values in different locations, primarily dependent on whether the location is on or off the tectonic plate the datum is tied to. Under these circumstances the cellMaxLevel may be realised as an attribute of a parent cell one or more refinement levels above the cell.		M	1	Integer
	nodes	Ordered sequence of vertices, clockwise round the cell's boundary.	true	M	1	Node

	numEdges	Number of edges that make up the cell's boundary.	true	M	1	Integer
	perimeter	Length of the cell's boundary.	true	M	1	Length
Constraints:	(none)					

Table 72 — Elements of Equal-Area Cell::EA_Zone

Name:	EA_Zone					
Definition:	An EA_Cell's location is an EA_Zone					
Stereotype:	Interface					
Inheritance from:	LocationS					
Abstract:	true					
Associations:	(none)					
Public attributes:	<i>Name</i>	<i>Definition</i>	<i>Derived</i>	<i>Obligation</i>	<i>Maximum occurrence</i>	<i>Data type</i>
	centroid	Cell's representative position calculated as the cell's geodesic centre of surface area, held by the cell's LocationS.		M	1	DirectPosition
	identifier	EA_Zone's unique GeographicIdentifier.		M	1	GeographicIdentifier
Constraints:	(none)					

Table 73 — Elements of Equal-Area Cell::EA_BoundaryType

Name:	EA_BoundaryType	
Definition:	CodeList for permitted curve types as constructors of an EA_Cell boundary. NOTE All EA_BoundaryType curves can be constructed as an intersection of a plane and an ellipsoid. So, each of these curve types is a straight line on a designated plane.	
Stereotype:	CodeList	
Abstract:	true	
Associations:	(none)	
Values:	<i>Name</i>	<i>Definition</i>
	geodesic	Shortest path between two points on the spherical or ellipsoidal DGGS's Earth reference model. Geodesic curves are defined using the GeodesicData constructor.
	smallCircle	Curves that are the intersection of a plane and an ellipsoid, where the plane is perpendicular to the axis of rotation of an ellipsoid are in small circles, see greatCircle. Lines of latitude are small circles.
	greatCircle	The great circle is a special case of small circle where the two focal points of the ellipse are also on the defining plane. On a non-spherical ellipsoid this is the only circle that is also a geodesic.
	smallEllipse	Curves that are the intersection of a plane and an ellipsoid, where the plane is parallel to the axis of rotation of the ellipsoid, are small ellipses, see greatEllipse.
	greatEllipse	A greatEllipse is a special case of smallEllipse where the axis of rotation is on the defining plane. GreatEllipses are geodesics. Lines of longitude are greatEllipses.
	projectedLine	A curve on the surface of an ellipsoid, whose equal-area projection on the projection's reference plane is a straight line.

Annex A (normative)

Abstract test suite

A.1 General

This annex specifies an Abstract test suite for the conformance categories in this document. The requirement tests associated with each conformance category are listed in Table A.1–Table A.3. Tests identifiers below are relative to <http://www.opengis.net/spec/DGGS/2.0/>

A.2 Common Spatio-temporal Classes package conformance categories

The requirement tests that apply to each conformance category in the Common Spatio-temporal Classes package are listed in Table A.1.

Table A.1 — Categories of conformance

Category	Requirements
Temporal geometry and topology	Requirement Test A.1
Temporal reference systems using period identifiers	Requirement Test A.4
Spatial zone geometry and topology	Requirement Test A.2
Spatial reference systems using zonal identifiers	Requirement Test A.3, & Requirement Test A.5
Spatio-temporal zone geometry and topology	Requirement Test A.1, & Requirement Test A.2
Spatio-temporal reference systems using zonal identifiers	Requirement Test A.3, Requirement Test A.4, & Requirement Test A.5

Requirement Test A.1: Common Spatio-temporal Classes — Temporal — Geometry

Abbreviation conf/cc/temporal/geometry

Type Basic

Requirement 6.2.1.2, Requirement 19:
<http://www.opengis.net/spec/DGGS/2.0/req/cc/temporal/geometry>

Reference
subclause [6.2.1](#)

Test purpose To verify the common classes for temporal geometry and topology conform to the data model in Figure 3 and Figure 4 and defining tables in Table 2–Table 13.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.2: Common Spatio-temporal Classes — Zone — Geometry

Abbreviation	conf/cc/zone/geometry
Type	Basic
Requirement	6.2.2.2, Requirement 20: http://www.opengis.net/spec/DGGS/2.0/req/cc/zone/geometry
Reference subclause	6.2.2
Test purpose	To verify the common classes for zonal geometry and topology conform to the data model in Figure 5 and defining tables in Table 14–Table 19.
Test method	Inspect documentation of the DGGS specification.

Requirement Test A.3: Common Spatio-temporal Classes — Spatial — Location

Abbreviation	conf/cc/spatial/location
Type	Basic
Requirement	6.3.1.2, Requirement 21: http://www.opengis.net/spec/DGGS/2.0/req/cc/spatial/location
Reference subclause	6.3.1
Test purpose	To verify the common classes for spatial location conform to the data model in Figure 6 and defining tables in Table 20.
Test method	Inspect documentation of the DGGS specification.

Requirement Test A.4: Common Spatio-temporal Classes — Temporal — Reference system using period identifiers

Abbreviation	conf/cc/temporal/rsupi
Type	Basic
Requirement	6.3.2.2, Requirement 22: http://www.opengis.net/spec/DGGS/2.0/req/cc/temporal/rsupi
Reference subclause	6.3.2
Test purpose	To verify the common classes for reference systems using period identifiers conform to the data model in Figure 6 and defining tables in Table 21–Table 24.
Test method	Inspect documentation of the DGGS specification.

Requirement Test A.5: Common Spatio-temporal Classes — Zone — Reference system using zonal identifiers

Abbreviation conf/cc/zone/rsuzi

Type Basic

Requirement 6.3.3.2, Requirement 23: <http://www.opengis.net/spec/DGGS/2.0/req/cc/zone/rsuzi>Reference
subclause [6.3.3](#)

Test purpose To verify the common classes for reference systems using zonal identifiers conform to the data model in Figure 8-Figure 11 and defining tables in Table 25–Table 36.

Test method Inspect documentation of the DGGS specification.

A.3 DGGS Core package conformance categories**Table A.2 — Categories of conformance**

Category	Requirements
Spatial DGGS Core	Requirement Test A.2, Requirement Test A.3, Requirement Test A.5, and all Core requirement tests in Requirement Test A.6–Requirement Test A.19.
Spatio-temporal DGGS Core	Requirement Test A.1, Requirement Test A.2, Requirement Test A.3, Requirement Test A.4, Requirement Test A.5, and all Core requirement tests in Requirement Test A.6–Requirement Test A.19.

NOTE The requirement tests that apply to each conformance category in the DGGS Core package are in Table A.2.

A.3.1 Core — Reference system**Requirement Test A.6: Core — Reference system — Harmonized model**

Abbreviation conf/core/rs/harmonized_model

Type Basic

Requirement 7.2.2, Requirement 24:
http://www.opengis.net/spec/DGGS/2.0/req/core/rs/harmonized_modelReference
subclause [7.2](#)

Test purpose To verify that all reference system classes comply with classes in the Core reference system data model in Figure 13 and definitions in Table 37–Table 43.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.7: Core — Reference system — CRS

Abbreviation conf/core/rs/crs

Type Basic

Requirement 7.2.2, Requirement 25: <http://www.opengis.net/spec/DGGS/2.0/req/core/rs/crs>

Reference [7.2](#)

subclause

Test purpose To verify that the DGGS RS defines a CRS and complies with coordinate epoch requirements as specified for MD_ReferenceSystem.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.8: Core — Reference system — Global domain

Abbreviation conf/core/rs/global_domain

Type Basic

Requirement 7.2.3, Requirement 26:
http://www.opengis.net/spec/DGGS/2.0/req/core/rs/global_domain

Reference [7.2.3](#)
subclause

Test pmrpose To verify a reference system specifies a global domain, and its spatial, temporal and topological dimensionality.

Test Method Inspect documentation of the DGGS specification.

Requirement Test A.9: Core — Reference system — Global domain — Complete

Abbreviation conf/core/rs/global_domain/complete

Type Basic

Requirement 7.2.3, Requirement 27:
http://www.opengis.net/spec/DGGS/2.0/req/core/rs/global_domain/complete

Reference [7.2.3](#)
subclause

Test purpose To verify reference system domain completeness, with the level zero discrete global grid covering the entire global domain.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.10: Core — Reference system — Global domain — Unique

Abbreviation conf/core/rs/global_domain/unique

Type Basic

Requirement 7.2.3, Requirement 28:
http://www.opengis.net/spec/DGGS/2.0/req/core/rs/global_domain/unique

Reference subclause [7.2.3](#)

Test purpose To verify reference system domain uniqueness, with every location in the domain of the DGGS located in exactly one cell of the level zero discrete global grid.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.11: Core — Reference system — Cell — Simple

Abbreviation conf/core/rs/cell/simple

Type Basic

Requirement 7.2.4.1, Requirement 29:
<http://www.opengis.net/spec/DGGS/2.0/req/core/cell/simple>

Reference subclause [7.2.4.1](#)

Test purpose To verify that all the cells of a DGGS specification have shapes that are simple geometry, where the geometry of the cell: does not self-intersect; is topologically the same as the equivalent shape of a circle with the cell's dimensionality; and encloses a region that is measurable in the cell's metric.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.12: Core — Reference system — Cell — Direct position

Abbreviation conf/core/rs/cell/direct_position

Type Basic

Requirement 7.2.4.2, Requirement 30:
http://www.opengis.net/spec/DGGS/2.0/req/core/cell/direct_position

Reference subclause [7.2.4.2](#)

Test purpose To verify that all zones in each discrete global grid are assigned a direct position that is within the zone's boundary.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.13: Core — Reference system — Cell — Address

Abbreviation	conf/core/rs/cell/address
Type	Basic
Requirement	7.2.4.3, Requirement 31: http://www.opengis.net/spec/DGGS/2.0/req/core/cell/address
Reference subclause	7.2.4.3
Test purpose	To verify that all zones in all discrete global grids have a globally unique zonal identifier (or cell index) that provides a spatio-temporal reference.
Test method	Inspect documentation of the DGGS specification.

Requirement Test A.14: Core — Reference system — Discrete global grid

Abbreviation	conf/core/rs/discrete_global_grid
Type	Basic
Requirement	7.2.5, Requirement 32: http://www.opengis.net/spec/DGGS/2.0/req/core/rs/discrete_global_grid
Reference subclause	7.2.5
Test purpose	To verify that a DGGS RS defines discrete global grids as aggregations of all the cells at the same level in the hierarchy.
Test method	Inspect documentation of the DGGS specification.

Requirement Test A.15: Core — Reference system — Discrete global grid — Sequence

Abbreviation	conf/core/rs/discrete_global_grid/sequence
Type	Basic
Requirement	7.2.5, Requirement 33: http://www.opengis.net/spec/DGGS/2.0/req/core/rs/discrete_global_grid/sequence
Reference subclause	7.2.5
Test purpose	To verify a DGGS RS orders its discrete global grids in a sequence of increasing refinement level.
Test method	Inspect documentation of the DGGS specification.

A.3.2 Core — Functions

Requirement Test A.16: Core — Functions — Quantization

Abbreviation conf/core/functions/quantization

Type Basic

Requirement 7.3.2, Requirement 34:
<http://www.opengis.net/spec/DGGS/2.0/req/core/functions/quantization>

Reference [7.3.1](#)
subclause

Test purpose To verify that a DGGS specification has operations to assign data from external sources to cells that conform to the data model in Figure 14 and definitions in Table 44–Table 48.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.17: Core — Functions — Query — ZoneQuery

Abbreviation conf/core/functions/query/zonequery

Type Basic

Requirement 7.3.4, Requirement 35:
<http://www.opengis.net/spec/DGGS/2.0/req/core/functions/query/zonequery>

Reference [7.3.3](#)
subclause

Test purpose To verify that a DGGS specification implements query operations that conform to the data model in Figure 16 and definitions in Table 49–Table 51, across its entire domain.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.18: Core — Functions — Interoperation — Query

Abbreviation conf/core/functions/interoperation/query

Type Basic

Requirement 7.3.5.4, Requirement 36:
<http://www.opengis.net/spec/DGGS/2.0/req/core/functions/interoperation/query>

Reference [7.3.5.3](#)
 subclause

Test purpose To verify that a DGGS specification implements operations to read, interpret and execute external data queries that conform to the data model in Figure 17 and Figure 18 and definitions in Table 52–Table 56.

Test method Inspect documentation of the DGGS specification.

Requirement Test A.19: Core — Functions — Interoperation — Broadcast

Abbreviation conf/core/functions/interoperation/broadcast

Type Basic

Requirement 7.3.5.6, Requirement 37:
<http://www.opengis.net/spec/DGGS/2.0/req/core/functions/interoperation/broadcast>

Reference [7.3.5.5](#)
 subclause

Test purpose To verify that a DGGS specification implements operations to translate data results from interoperation queries to standard data formats and broadcast the reformatted result set that conform to the data model in Figure 17 and Figure 19 and definitions in Table 52 and Table 57–Table 59.

Test method Inspect documentation of the DGGS specification.

A.4 Equal-Area Earth DGGS package conformance categories

The requirement tests that apply to each conformance category in the Equal-Area Earth DGGS package are in Table A.3.

Table A.3 — Categories of conformance

Category	Requirements
Equal-Area Earth DGGS	Requirement Test A.2, Requirement Test A.3, and Requirement Test A.5, and all Core requirement tests in Requirement Test A.6–Requirement Test A.19, and all EAERS requirement tests in Requirement Test A.20–Requirement Test A.29.

Requirement Test A.20: Equal area — Earth reference system — Harmonised model

Abbreviation conf/ea/ers/harmonised_model

Type Basic

Requirement 8.1.2, Requirement 38:
http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/harmonised_model

Reference subclause [8.1](#)

Test purpose To verify an EAERS specification complies with the data model in Figure 20, Figure 21 and Figure 22 and definitions in Table 60–Table 73

Test method Inspect documentation for the EAERS specification.

Requirement Test A.21: Equal area — Earth reference system — Global domain

Abbreviation conf/ea/ers/global_domain

Type Basic

Requirement 8.1.3, Requirement 39:
http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/global_domain

Reference subclause [8.1.3](#)

Test purpose To verify the domain of an EAERS is the whole surface of the reference frame's earth model and the DGG_ReferenceSystem cellEqualSized is specified as a DGGS_Grids constraint.

Test method Inspect documentation of the EAERS specification.

Requirement Test A.22: Equal area — Earth reference system — Tessellation — Initial

Abbreviation conf/ea/ers/tessellation/initial

Type Basic

Requirement 8.1.4.2, Requirement 40 :
<http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/tessellation/initial>

Reference subclause [8.1.4.2](#)

Test purpose To verify that an EAERS specification has an initial tessellation comprising equal area cells produced by mapping the faces of a base unit polyhedron to a surface model of the Earth.

Test method Inspect documentation of the EAERS specification.

Requirement Test A.23: Equal area — Earth reference system — Tessellation — Sequence

Abbreviation	conf/ea/ers/tessellation/sequence
Type	Basic
Requirement	8.1.4.3, Requirement 41 : http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/tessellation/sequence
Reference subclause	8.1.4.3
Test purpose	To verify an EAERS defines tessellation operations that generate a sequence of discrete global grids with progressively smaller cells.
Test method	Inspect documentation of the EAERS specification.

Requirement Test A.24: Equal area — Earth reference system — Tessellation — Sequence — Max

Abbreviation	conf/ea/ers/tessellation/sequence/max
Type	Basic
Requirement	8.1.4.3, Requirement 42 : http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/tessellation/sequence/max
Reference subclause	8.1.4.3
Test purpose	To verify that an EAERS specifies a limit in its sequence of discrete global grids that ensures the error budget for EA_Cell area cannot be exceeded.
Test method	Inspect documentation of the EAERS specification.

Requirement Test A.25: Equal area — Earth reference system — Tessellation — Global area preservation

Abbreviation conf/ea/ers/tessellation/global_area_preservation

Type Basic

Requirement 8.1.4.4, Requirement 43 :
http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/tessellation/global_area_preservation

Reference subclause [8.1.4.4](#)

Test purpose To verify for EA_Cells in each successive discrete global grid, that domain completeness and location uniqueness are preserved, with total area of those EA_Cells the same as the initial global grid and no overlapping DGGS cells.

Test method Inspect documentation of the EAERS specification.

Requirement Test A.26: Equal area — Earth reference system — Cell — Simple — 2D polygon

Abbreviation conf/ea/ers/cell/simple/2d_polygon

Type Basic

Requirement 8.1.5.1, Requirement 44:
http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/cell/simple/2d_polygon

Reference subclause [8.1.5.1](#)

Test purpose To verify that all of the cells of an EAERS specification have shapes that are simple polygons on the surface model of the Earth where: edges only meet at vertices; exactly two edges meet at each vertex; the number of edges and vertices are the same; and the region enclosed always has a measurable area.

Test method Inspect documentation of the EAERS specification.

Requirement Test A.27: Equal area — Earth reference system — Cell — Direct position — Centroid

Abbreviation conf/ea/ers/cell/direct_position/centroid

Type Basic

Requirement 8.1.5.2, Requirement 45:
http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/cell/direct_position/centroid

Reference [8.1.5.2](#)
 subclause

Test purpose To verify that the cells defined by an EAERS are referenced at the centroid of each cell. This test requires verification that the attribute EA_Zone(centroid) returns a direct position on the surface of the cell.

Test method Inspect documentation of the EAERS specification.

Requirement Test A.28: Equal area — Earth reference system — Cell — Equal area — Error budget

Abbreviation conf/ea/ers/cell/equal_area/error_budget

Type Basic

Requirement 8.1.5.3, Requirement 46:
http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/cell/equal_area/error_budget

Reference [8.1.5.3](#)
 subclause

Test purpose To verify that an EAERS specification defines error budget(s) of 1% or less that represents the maximum ratio of a cell's area to the theoretical cell area computed from the number of cells and the surface area of the Earth model.

Test method Inspect documentation of the EAERS specification.

Requirement Test A.29: Equal area — Earth reference system — Cell — Equal area

Abbreviation conf/ea/ers/cell/equal_area

Type Basic

Requirement 8.1.5.3, Requirement 47:
http://www.opengis.net/spec/DGGS/2.0/req/ea/ers/cell/equal_area

Reference [8.1.5.3](#)
subclause

Test purpose To verify that the cells in each discrete global grid, and of each cell geometry in a DGGS specification have equal area within the specified error budget.

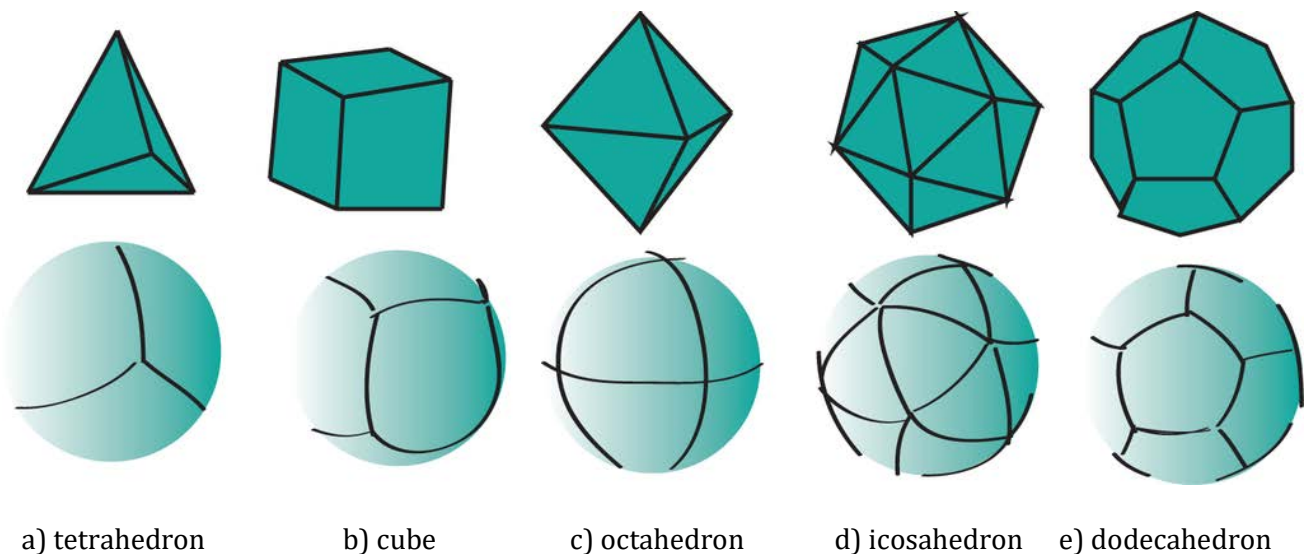
Test method Inspect documentation of the EAERS specification, and for each discrete global grid, compare the area of each cell defined by its geometry with the average area of all cells of the same geometry (triangle, quadrangle, pentagon or hexagon).

Annex B (informative)

Equal area DGGS theory

All Discrete Global Grid Systems (DGGS) are structured for information as distinct from conventional coordinate reference systems originally designed for navigation. For a grid based global spatial information system to operate effectively as an analytical system it should be constructed using cells that represent the surface of the Earth in a uniform way. This ensures that, at each resolution, all cells have the same probability of contributing to an analysis. An Equal Area DGGS is a spatial reference system that uses a hierarchy of equal area tessellations to partition the surface of the Earth into grid cells or their analogous lattice points. In this way, information recorded about phenomena at a location can be easily referenced to the explicit area of the associated cell, integrated with other cell values, and provides statistically valid summaries based on any chosen selection of cells. With equal area partitioning, spatial analysis can be replicated consistently anywhere on the Earth, independent of resolution or scale.

Equal Area Earth DGGS reference systems are polyhedral reference systems on the surface of a base unit polyhedron's circumscribed ellipsoid. The base unit polyhedron's location and orientation is defined in Earth Centered (EC) coordinates. The initial equal area tessellation of the chosen ellipsoidal Earth model is constructed by scaling a unit polyhedron of defined orientation until its vertices all touch the ellipsoid and connecting adjoining vertices with arcs selected from the set of permitted arcs, the simplest of which are geodesic, small circle or small ellipse arcs. Appropriate differential scaling is applied to the unit polyhedron to ensure an equal area initial tessellation. For the simple case of regular polyhedra and geodesic (i.e. great circle) arcs on its circumscribed spheroid, the scaling is uniform. Figure B.1 illustrates their simplest form using a regular spherical polyhedron with a spheroidal circumscribing ellipsoid and geodesic arcs. Small circle arcs are typically used to construct arcs along lines of latitude for both ellipsoids and spheroids. Both small circle and small ellipse arcs are formed from the intersection of a defined plane with the ellipsoid, and in that sense, they can be considered equivalent to the "straight" lines of two-dimensional cell boundaries. More complex forms of straight line, such as arcs that project to a straight line in an equal area projection are also allowed.



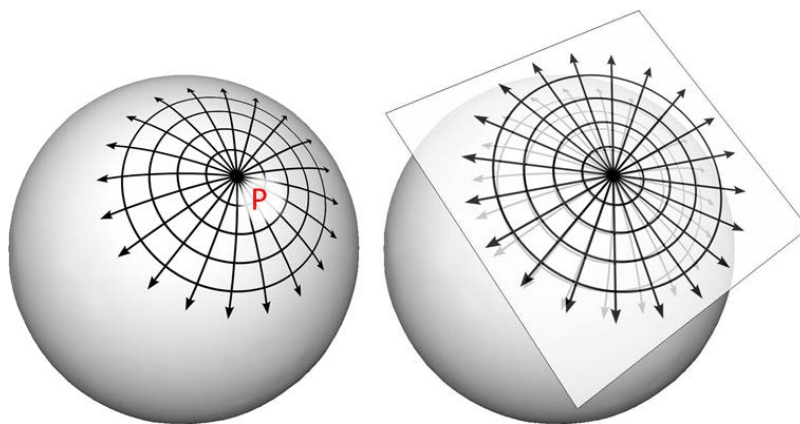
NOTE [after Figure 2 in Mahdavi-Amuri et. al.[\[35\]](#)].

Figure B.1 — Regular polyhedra (top) and their corresponding initial equal area tessellation (bottom)

There is a gap between conventional coordinate reference systems and the reference system needed to define DGGs. This document fills the gap in existing ISO standard reference systems and establishes requirements for globally interoperable equal-area cell- or lattice-based information frameworks.

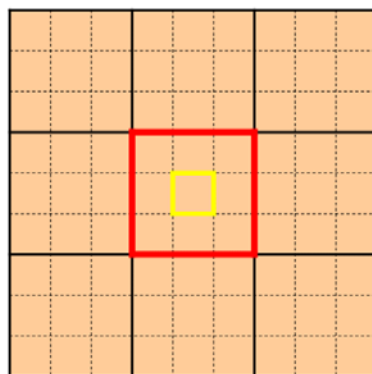
Existing spatial CRS (e.g. ECEF [Earth Centered Earth Fixed], WGS 84 or Web Mercator) build grids from projected Cartesian or ellipsoidal coordinate axes. Rectangular planar grids are typically formed by establishing a set of regular ticks on a pair of linear axes with grids cells being formed by the intersection of straight lines drawn normal to the ticks on each axis. Analogous construction techniques can be used to create triangular or hexagonal grids. The properties of grids built this way arise from the premise of planar geometry and not the curved geometry of the surface of a sphere or ellipsoid. While these properties hold true at local scales, in curved geometries they increasingly fail at progressively larger regions of interest (see Figure B.2). Take for example the assumption that a grid cell's geometric properties are independent of its size or resolution, which is implicit in constructing sets of planar aligned (or 'nested') 10 m, 30 m and 90 m grids. As shown in Figure B.3, a 90 m square cell formed from nine 30 m square child cells has the following properties:

- a) It is also square;
- b) Its edges are three times the edge length of its 30 m child cells, which in turn all are three times the edge length of their 10 m child cells;
- c) Its interior angles are all right angles and identical to the interior angles of all of the child cells;
- d) Its edges follow the shortest linear path between neighbouring cell vertices; and,
- e) The angles or bearings from centroid to centroid between cells are preserved irrespective of the direction of travel.



NOTE With increasing distance away from the point P there is an increasing deviation between the two representations of the grid [after Figure 15 in Mahdavi-Amuri et. al. [\[34\]](#); and Figure 3 in Schmidt et. al. [\[42\]](#)].

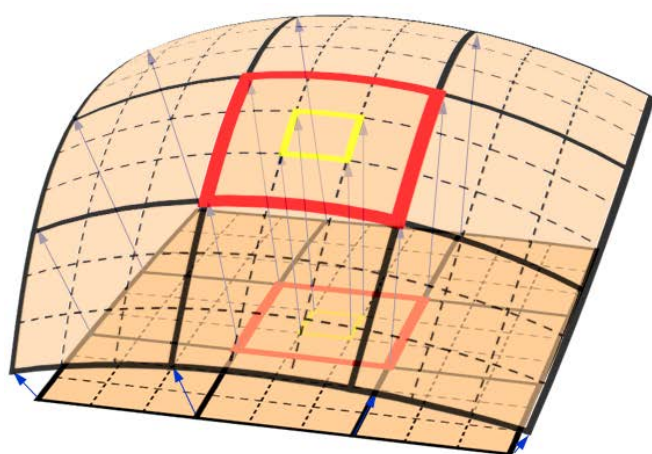
Figure B.2 — Comparison of a grid (in this case radial) represented on both (a) curved and (b) planar surfaces



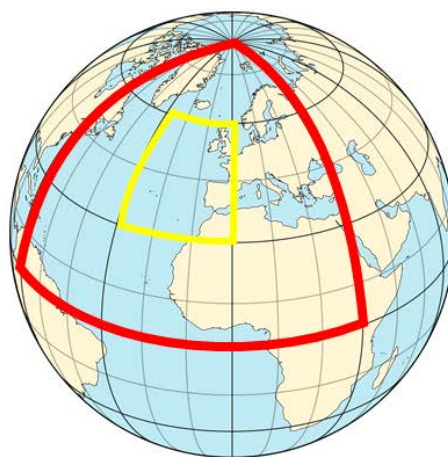
NOTE The two highlighted cells – outlined with a wide red line and a narrower yellow line – have identical geometry and in each case the geometry is also shared with all other cells of the same size.

Figure B.3 — Planar square grid with nested child cells

On a curved surface, however, this is never the case. Yet we often make the same assumption; that all cells are geometrically identical in, for example, a country- or continental-wide mosaic comprising many satellite images. Consequently, under this paradigm assumption, choosing a fixed cell size for a global grid whose cells represent equal areas and seamlessly fit the earth's surface is problematic. When this is required, conventional spatial standards enforce latitude-longitude axes to be used and these grids are therefore described in these spherical coordinates. But the cells of these types of (equal-angular) grids do not have the same properties of planar grids. Figure B.4 shows a similar consideration to that of Figure B.3, only the grids are constructed using spherical instead of planar Cartesian coordinates. In this scenario, the largest (parent) cell does not necessarily have the same shape or internal angles as the child cells. Also, its edges do not follow the shortest linear path from corner to corner. Bearing directions between cell centroids, however, are preserved in both planar and curved geometry spaces.



a) Square grid with nested child cells on a portion of a sphere (projected from the planar grid shown in Figure B.3)

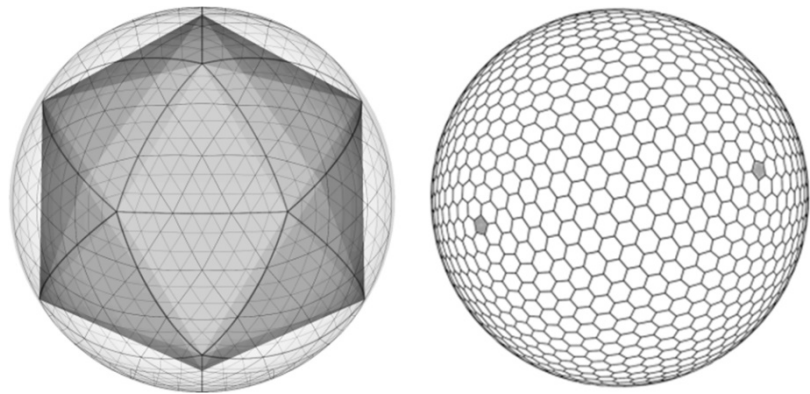


b) Latitude-longitude (equal angular) grid, the red cell is $90^\circ \times 90^\circ$ and has nine $30^\circ \times 30^\circ$ child cells (the central child cell is shown in yellow)

Figure B.4 — Geometries and spatial properties of cells on curved surfaces.

In an attempt to address this dichotomy, conventional spatial standards therefore support either small, local, well-behaved planar grids or global grids that preserve bearings and angular lengths, and do not preserve area, but not both at the same time. This document fills this gap by providing a formal specification for area preserving reference systems based on the surface model of the Earth that respect the accuracy and precision of spatial data at all scales from local to global. These systems use a hierarchical tessellation of the entire Earth to produce equal-area grids. Figure B.5 shows two examples.

We anticipate that future extensions of the specifications in this document will support higher dimensions, such as the volume of the Earth and its atmosphere, and the Earth through time.



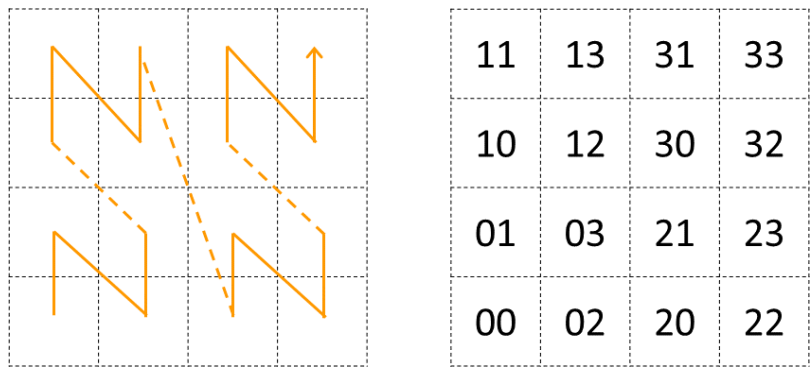
- a) Triangular cells starting with an icosahedron. Then refining each cell recursively into 9 smaller cells. Shown after two iterations
- b) Hexagonal cells with twelve pentagonal cells at the vertices of the initial tessellation

Figure B.5 — Tessellations of the Earth to equal-area cells.

The language and foundations of current geospatial standards are deeply rooted in planar thinking, so while this document leverages as much as it can from existing standards, it also introduces new concepts that are subtly and yet fundamentally, different from those described by the standards that it draws from. These subtle differences challenge our thinking. As a consequence, this document is an evolution of both existing raster processing practice and past usage of discrete global grids.

As a specification for an area preserving earth reference system, this document defines more than just grids and lattices. The underlying geometry of the cells and the topological relationships between neighbouring cells can be used to define GUIDs for the cells across all resolution.

Earlier, we noted that planar grids are formed from the pairs of axes each with regular ticks corresponding to the cell dimension, facilitating a simple topological referencing schema for each cell (usually via a matrix style index for each cell along the axes of the grid, i.e. rows and columns for a two-dimensional grid). With DGGs, we introduce a more sophisticated set of cell referencing schemas, such as space filling curves which traverse all of the cells in a manner that is functionally equivalent to the axes. As shown in Figure B.6, cell indices are assigned to cells along the path of the space filling curve. These indices, together with the geometry of the space filling curve, carry the metrics of the curved surface and the topological relationships between neighbouring cells. The cell indices are explicitly treated as GUIDs.



NOTE Labels of 4×4 square cells. [after Figure 25 in Mahdavi-Amuri et. al.^[34]]

Figure B.6 — Using Morton space filling curve for defining

The mathematical properties of integers and real numbers on axis pairs in a plane are known implicitly and are therefore not part of any ISO document concerning planar grids. The theoretical basis on which the separate disciplines for space filling curves, GUIDs, grids, spatial topology and discrete global grids are also well founded. However, their roles in DGGs are not implicitly understood. This document therefore defines these roles and relationships explicitly. This is a necessary departure from previous DGGs work that is needed to ensure a robust spatial reference frame standard. A brief history of DGGs is provided in [Annex C](#) for reference.

Annex C (informative)

Background to DGGs

C.1 DGGs as a digital information medium

Conventional coordinate reference systems address the globe with a continuous field of points suitable for repeatable navigation and analytical geometry. While this continuous field is represented on a computer in a digitized and discrete fashion by tuples of fixed-precision floating point values, it is a non-trivial exercise to relate point observations spatially referenced in this way to areal features on the surface of the Earth. In contrast, a DGG is designed to be an information grid, not a navigation grid. DGGs provide a fixed areal based geospatial reference frame for the persistent location of measured Earth observations, feature interpretations, and modelled predictions. DGGs address the entire planet by partitioning it into a discrete hierarchical tessellation of progressively finer resolution cells. The geometry and location of the cell is the principle aspect of a DGG. Data integration, decomposition, and aggregation is optimized in the DGG's hierarchical structure and can be exploited for efficient multi-source data processing, storage, discovery, transmission, visualization, computation, analysis, and modeling.

C.2 History

The concept of using polyhedra to model the surface of the Earth is by no means new. In 1509 Luca Pacioli published “De Divina Proportione”^[36] a treatise, illustrated by Leonardo Da Vinci, exploring the mathematical characteristics of the “golden ratio” (also referred to as the “divine proportion”) which included a consideration of the properties of the five platonic solids circumscribed within the sphere and the eminent role of the “golden ratio” in the construction of two of them (the icosahedron and dodecahedron). It is likely that his time studying with Pacioli influenced Da Vinci's later thinking regarding spherical geometry; evidenced in 1515 by his derivation of the octahedral analysis of the volume of a sphere with various forms of segmentation^[51]. This work is suggested to have led to the development of the Reuleaux triangular formulation of the world map (or *mappamundi*), attributed to Da Vinci^[50], and can be considered a precursor to differential calculus, formally developed by Newton and Leibniz nearly two centuries later.

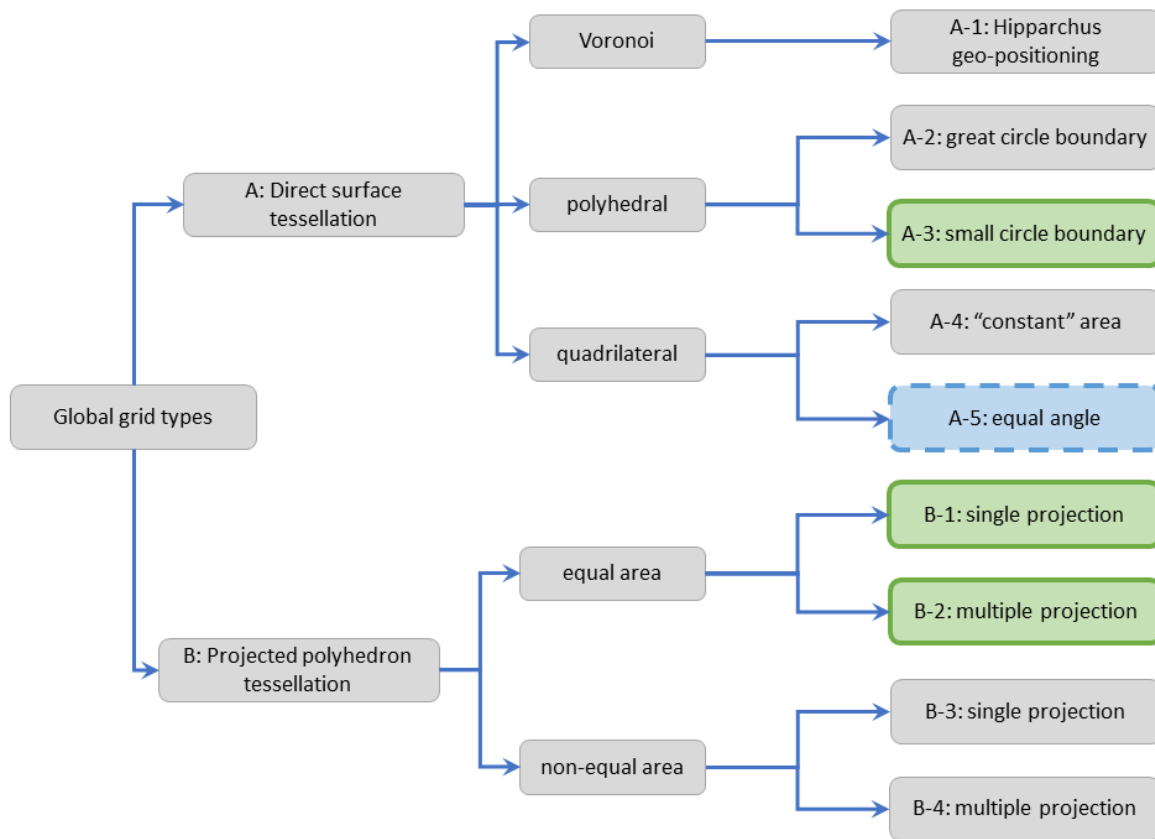
In the 1940's, a similar approach was used by R. Buckminster Fuller in the development of the Dymaxion map of the world^[5], a physical model of the Earth mapped onto the planar faces of a polyhedron (first presented as a cuboctahedron^[25] and then later as an icosahedron^[24]). The aim of the Dymaxion map was to depict the spherical world as a flat surface with true scale, true direction and correct configuration, all at the same time. Although a physical model of the Earth, and not strictly a DGG, it inspired later researchers to produce digital Earth models, which in turn has led to the development of DGGs.

Formal development of DGGs began in the 1950s with the promising value of global analysis coinciding with the increased use of geographic information systems and the availability of global mapping data and positioning systems. Perhaps the first published instance of formalized discrete global grids with application to numerical analysis was described by Vestine et. al.^[48] in 1955, where they define and use an equal-area grid based on the mapping of a spherical icosahedron onto the surface of the Earth as a framework to conduct areal based integral and spherical-harmonic analyses of the geomagnetic field. This grid was later used (and re-described) by Sadourny et. al.^[40] in 1968 to model equations of atmospheric motion without distortion across the entire globe. Another style of discrete global grid, and perhaps the first application of hierarchical indexing schemas as an analytic cell referencing tool was implemented by Geoffrey Dutton in 1984^{[15],[18],[14]} at the Laboratory for Computer Graphics and Spatial Analysis at Harvard Graduate School of Design. Dutton's first global grid was designed for assembling and managing global terrain data on a triangular global grid. His global GEM^{[15],[18],[14],[17]} started with a cuboctahedron connected into a rhombic dodecahedron (which is its dual polyhedron where the vertices

of one corresponds to the centre of the faces of the other) and recursively divided the initial 12 triangular faces into refinements of 9 partially nested equilateral triangles. Dutton refined GEM to use only an octahedral basis in the QTM DGGs^{[15],[18],[14],[19]}. QTM is a fourfold hierarchical decomposition of facets of an octahedron into triangles whose edges follow small circles. Elevations were assigned to the centroids of child triangles and to the vertices that coincided with them. Waldo Tobler and Zi-tan Chen^[47] imagined the primary purpose for a formal discrete global grid standard would be information exchange and storage. Tobler argued that as a generalized information medium *“coverage must be uniform and that every element of area must have an equal probability of entering the system. This suggests that the world should be partitioned into chunks of equal size”*^[47]. Tobler’s global grid started with a cube as a base unit polyhedron and divided into rectilinear quad-trees to create successive subdivisions with unlimited resolution. Dennis White, Scott Overton, and Jon Kimerling, driven by a need for a statistically valid sampling to integrate aquatic and terrestrial monitoring for the US-EPA, designed a global grid in 1989 using closely packed hexagonal cells that started with a truncated icosahedron as the base unit polyhedron^[49].

C.3 Global grid taxonomy

There have been numerous methods proposed for achieving a tessellation of the Earth, each with different distortion characteristics^[29]. These tessellations can be organized into a limited set of categories that describe a hierarchical taxonomy of global grids Figure C.1^{[29],[16]}. Only two groups of classes of global grid achieve an equal area solution^[29]: those based on equal area mapping of a base unit polyhedron (such as the ISEA projection^[44]) and those based on direct surface tessellations using small circle subdivision (e.g. References ^{[45],[46]}).



Key

A Direct surface tessellations

- A-1 Voronoi — Hipparchus geo-positioning[32];
- A-2 Polyhedral — great circle boundary[21];
- A-3* Polyhedral — small circle boundary[21];
- A-4 Quadrilateral — "constant" area[8];
- A-5† Quadrilateral — equal angle[7],[39],[9],[30].

B Projected polyhedron tessellations

- B-1*Equal area — single projection[47],[31];
- B-2*Equal area — multiple projection[44],[27],[33];
- B-3 Non-equal area — single projection[43];
- B-4 Non-equal area — multiple projection[22],[26]

NOTE Tessellations marked in the key as suitable for use with this document are:

*: Equal-area DGGs (Section 8 in this document), and

†: Axis-aligned DGGs (planned additional part to ISO 19170 series).

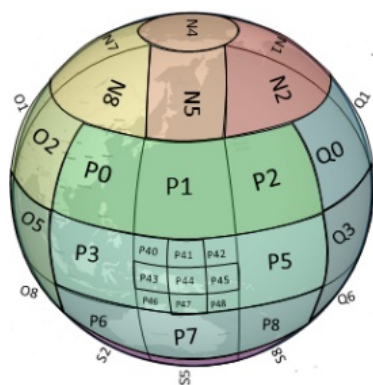
Figure C.1 — Global grid taxonomy (based on Figure 4 in [29]).

C.4 Criterion

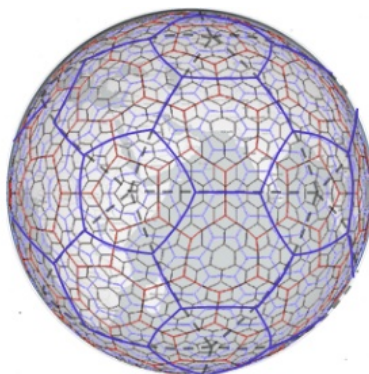
There are many possible DGGs, each with their own advantages and disadvantages. Criteria for a discrete global grid are well developed by both Michael F. Goodchild[28] and Jon Kimerling[29], the foremost requirements being a tessellation of cells that exhaustively cover the globe with each cell having an equal area, and a centroid representing a single point. The points and cells of the various resolution grids which constitute the grid system form a hierarchy which displays a high degree of regularity[10]. Choices for an appropriate tessellation include properties of shape, adjacency, connectivity, orientation, self-similarity, decomposability, and packing properties. Cell choices are generally taken from the three shapes that uniformly tile a plane — rectilinear, triangular, and hexagonal cells.

While it is possible to map any polyhedral solid to the surface of the earth, the Platonic solids (tetrahedron, cube, octahedron, dodecahedron and icosahedron; see Figure B.1) are the only polyhedral solids that perfectly partition the surface of a sphere into regular, equal area cells[23]. As a result, the Platonic solids are used in the construction of most equal area DGGs, often via a mapping of the

polyhedral faces to the surface model of the Earth (some examples are shown in Figure C.2). This method of mapping the faces of a base unit polyhedron to the surface model of the Earth creates a coordinate reference system that is based on a curved geometric framework. GIS and image analysis packages that assume flat earth geometries need to adapt to support this new construct, which more closely represents the Earth.



a) Quadrilateral cells on rHEALPix projected hexahedron, levels 0–2 with refinement ratio of 9.



b) Hexagonal cells on ISEA projected icosahedron, levels 0–4 with refinement ratio of 3.



c) Triangular cells on QTM of an octahedron, levels 0–3 with refinement ratio of 4.
(courtesy of Geoffrey Dutton)

Figure C.2 — Examples of DGGs based on the mapping of the faces of Platonic solids to the surface model of the Earth

Any tessellation of the Earth does not necessarily produce a DGGs. Single resolution computational grids are not sufficient to constitute a DGGs. Spatial data structures used to organize map tiles or optimize rapid spatial search cannot be considered to qualify as a DGGs in and of themselves. Although DGGs often utilize hierarchical indices to identify a cell, the primary feature of the DGGs is the cell geometry, not the optimization of a spatial query. Further, DGGs have data independent geometry — their geometry is not formed to optimize a balanced search like R-Trees or maximal spacing of data as generated by Voronoi diagrams.

C.5 A digital spatial reference system

One way to understand the important difference between a DGGs and a conventional spatial reference system is to consider that a DGGs provides a digital framework for geospatial information. Geospatial information is essentially a signal, that is, a variable (e.g. measurement of phenomena), which changes subject to another independent variable (e.g. spatial location, time, some physical interaction etc.). Conventional geospatial data are analogue signals, as they reference to a continuous space: geographic coordinates on an ellipsoidal datum. Even the discrete pixels of a satellite Earth observation image reference this continuous analogue model of Earth. However, these pixels do not observe precisely the same locational area for successive observations. Spatial reference by geographic identifier is described in ISO 19112. DGGs provide this globally in a structured form which is analogous to the ellipsoidal coordinate system described in ISO 19111, but is based on discrete cells rather than continuous point locations (e.g. Li, Cheng, Chen & Meng [30]).

Sampling and quantization are necessary for a signal to be considered digital. As the name implies, the DGGs provides the regular discrete intervals or cell partitioning to which location information (e.g. signal values) are sampled. A well-designed quantization strategy is also an important component of a DGGs which should maintain the fidelity of the original information in the values assigned to each cell. The discrete data values can be sampled from any geospatial data source, regardless of the original spatial reference, scale, format, type, frequency or time. A DGGs is a discrete “digital” model of the Earth.

C.6 Application

As each cell in a DGGS is fixed in location, and the location provides an explicit area representation, basic geospatial enquiries, such as "Where is it?", "What is here?", and "How has it changed?", are simplified into set theory operations. As any data values referenced to a particular DGGS are, by the nature of the grid, aligned, the high costs of integrating data in traditional systems are dramatically reduced.

A DGGS can even be designed for lossless encoding of vector geometry such that cells, and their integer addressing, predictably converge to the real number coordinate pairs of each observation with each successive refinement: an essential property of a conventional coordinate system.

DGGSs are designed to eliminate requirements for complex data fusion processes. Reducing the reliance on an intermediary integrator or analyst is a key requirement for distributed participatory digital-Earth information systems. "[Digital-Earth] *can clearly benefit from developments in discrete global grid, which can provide the georeferencing, the indexing, and the discretization needed for geospatial data sets. They have properties, in particular hierarchical structure, uniqueness, explicit representation of spatial resolution, and consistency, that make them superior to any single alternative.*"^[28].

A DGGS provides a uniform environment to integrate, aggregate and visualize both vector/point cloud geometries and raster-based geospatial data sources in much the same way that information within a computer graphics pipeline becomes the pixels on a computer screen. Efficiencies are gained through implementing the DE-9IM set of fundamental spatial operations^{[11]-[13]-[20]} directly on the DGGS cell structure. This allows for higher order analytics (via bindings to external analytic libraries) to be created on the DGGS structure itself, independent of the data sources.

Annex D (informative)

Temporal geometry, topology, and temporal referencing by named periods — Context for modelling

D.1 General

This document builds on the spatio-temporal definitions in ISO 19111:2019 to achieve a broader integration of spatio-temporal concepts. In addressing alignment with ISO 19108, the reader is directed to the discussion in ISO 19111:2019, Annex D, as a starting point which is adopted in full in this document.

D.2 Geometry and topology

Time can be represented as an ordered, one-dimensional geometry with topology. The only significant difference between one-dimensional spatial and one-dimensional temporal is the importance of direction, and the topological relationships that explicitly address direction. ISO 19107 and ISO 19108 define terms for geometric and topological primitives and their complexes that are functionally equivalent but different in structure. To achieve spatio-temporal uniformity this document aligns its definitions with ISO 19107:2019. When compared with equivalent terms in ISO 19108 this primarily results in differences in class inheritance rather than in underlying meaning. Comparing ISO 19108 terms to this document's terms, while putting the structural differences aside:

- TM_GeometricPrimitive and TM_TopologicalPrimitive map to this document's TemporalGeometricPrimitive, TemporalTopologicalPrimitive respectively;
- TM_TopologicalComplex maps to this document's TemporalTopologicalComplex;
- this document introduces TemporalGeometricComplex and TemporalGeometricCollection;
- the super classes of TM_Primitive, TM_Complex and TM_Object are not implemented and instead this document introduces TemporalGeometry and TemporalTopology;
- TM_Instant and TM_Period map to this document's Instant and Interval respectively;
- TM_Node and TM_Edge map to this document's NodeT and EdgeT respectively;
- TM_Duration, and its subclasses TM_PeriodLength and TM_IntervalLength map to this document's Duration, which encompasses any valid unit on a TemporalCS ([ISO 19111:2019](#)); and
- TM_RelativePosition maps to this document's RelativePosition, which is defined to reflect modern usage by SDWIG and OGC as defined in OWL-time.

D.3 Referencing by named periods

ISO 19108 includes the concepts of a named Ordinal Era, and Ordinal reference systems which address the needs of geological time. While the topology of Ordinal Era are known, their extent is in general ill-defined. To achieve spatio-temporal uniformity this document aligns itself with [ISO 19112:2019](#). Named Periods are introduced as the temporal equivalent of named Locations [ISO 19112:2019](#). Periods have well-defined extents as well as well-defined topology. Comparing the terms of ISO 19108 with this document's terms, while acknowledging this difference:

- TM_OrdinalEra maps to both Period and PeriodClass in this document depending on context; and

- TM_OrdinalReferenceSystems maps to TemporalReferenceSystemUsingPeriodIdentifiers in this document.

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⁷ <https://escholarship.org/uc/item/9492q6sm>

⁸⁾OGC Best Practice Papers are available from <http://www.opengeospatial.org/docs/as>

⁹ <https://www.w3.org/TR/2020/CR-owl-time-20200326/>

¹⁰⁾OGC Interface Standards are available from <https://www.opengeospatial.org/standards/>

[63] ISO 19117:2012, *Geographic information – Portrayal*